## Introduction to ODEs

Download the odeEuler.m, demoEuler.m and demoEulerPlot.m files from the class web site.

- 1. Determine whether  $y = \frac{1}{4} \left[ 2t 1 + 5e^{-2t} \right]$  is the exact solution to  $\frac{dy}{dt} = t 2y$  with the initial condition y(0) = 1. *Hint*: Take the easy way by evaluating the derivative and testing the initial condition.
- 2. Determine whether  $y = \frac{1}{2} \left[ 64 12t^2 \right]^{1/3}$  is the exact solution to

$$\frac{dy}{dt} = \frac{t}{y^2} \qquad y(0) = 2 \tag{1}$$

- 3. Download the demoEuler.m file from the class web site and rename the file as demoEuler2.m. Make the necessary modifications to demoEuler2.m in order to find the numerical solution to Equation (1) for  $0 \le t \le 2$ . Test your solution with h = 0.2 and h = 0.05.
- 4. (a) Modify your demoEuler2 function so that it computes and returns the global error

$$e_h = \|y - y_{\text{exact}}\|_{\infty}$$

where the subscript h reminds us that the error is a function of the stepsize, h.

(b) Create another m-file, say eulerErrorPlot, that calls your modified demoEuler2 function for a sequence of steps sizes, h = 0.2, 0.1, 0.05, 0.025, 0.0125, 0.00625, and stores the global error in a vector, say errh. Create a log-log plot of errh as a function of h.