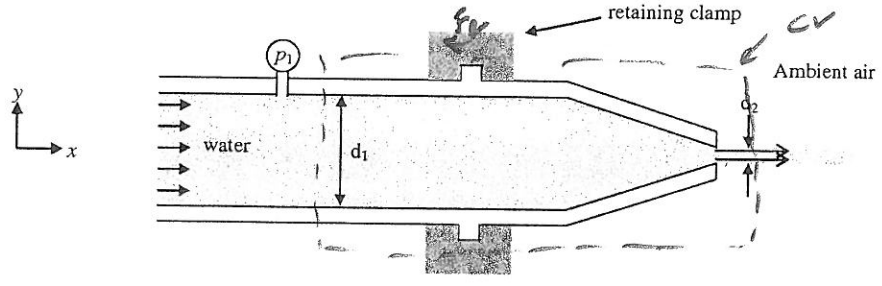


Final Exam

Closed book, closed lecture notes. 2-page cheat sheets, equation sheets, and calculator allowed.

1. (35pts) Water from a pipeline flows through the axisymmetric nozzle depicted in the sketch. The jet of the water leaving the nozzle flows into the ambient air. A ridge around the external circumference of the nozzle provides a surface for attaching an annular retaining clamp that holds the nozzle in place. The volumetric flow rate Q , the dimensions d_1 and d_2 , and the reading on the pressure gage p_1 are known. Neglect the weight of the water.

- a) (15pts) Derive a formula (of known terms) for the horizontal force on the retaining ring.
- b) (5pts) Under what conditions would the nozzle move to the right if the clamps were removed?
- c) (10pts) Derive a formula (of known terms) for the head loss for the flow through the nozzle.
- d) (5pts) Is there a value of p_1 that would make the head loss zero? If so, what is it?



A) Apply linear momentum in x direction - assume steady flow

$$\sum \vec{F}_x = \int_{CS} \rho \vec{V}_x (\vec{V} \cdot \vec{n}) dA$$

$$Q = V_1 A_1 = V_2 A_2$$

$$A_1 = \frac{\pi d_1^2}{4}$$

$$A_2 = \frac{\pi d_2^2}{4}$$

without velocity profile lets use average velocities.

RHS $\rho (V_1)(-V_1)A_1 + \rho V_2(V_2)A_2 = -\rho \frac{Q^2}{A_1} + \rho \frac{Q^2}{A_2} = \rho Q^2 \left[\frac{1}{A_2} - \frac{1}{A_1} \right]$

LHS $P_1 A_1 - P_2 A_2 - F_R = P_1 A_1 - F_R$ since A_2 is ambient

so

$$P_1 A_1 - F_R = \rho Q^2 \left[\frac{1}{A_2} - \frac{1}{A_1} \right]$$

$$F_R = -\rho Q^2 \left[\frac{1}{A_2} - \frac{1}{A_1} \right] + P_1 A_1$$

B) moves to right if $F_R > 0 \Rightarrow P_1 A_1 > \rho Q^2 \left[\frac{1}{A_2} - \frac{1}{A_1} \right]$