



What does P_1 need to be for $Q_{\text{exit}} = 0.09 \frac{\text{ft}^3}{\text{s}}$

$\rho_{\text{gas}}, \rho_{\text{H}_2\text{O}}$ given

Incompressible fluids $Q = AV$ V is uniform

$$Q_{\text{exit}} = Q_3 = \frac{\pi d_3^2}{4} V_3$$

Assume steady, inviscid, no losses, no work, assume $d_3 \ll dz$

Bernoulli's Eqn.

$$\frac{P_2}{\gamma_w} + \frac{V_2^2}{2g} + z_2 = \frac{P_3}{\gamma_w} + \frac{V_3^2}{2g} + z_3$$

$$\frac{P_2}{\gamma_w} = \frac{P_3}{\gamma_w} + \frac{V_3^2 - V_2^2}{2g} + z_3 - z_2$$

hydrostatic across gas

$$P_2 = P_1 + \gamma_g h_g$$

h_g - height of gasoline

plugging in

$$\frac{P_1}{\gamma_w} + \frac{\gamma_g h_g}{\gamma_w} = \frac{P_3}{\gamma_w} + \frac{V_3^2 - V_2^2}{2g} + z_3 - z_2$$

$P_3 = 0$ at atm

rearrange

$$P_1 = P_3 + \gamma \left(\frac{v_3^2}{2g} - z_2 \right) - \gamma_s h_s$$

$$P_1 = \gamma_w \left(\frac{v_3^2}{2g} - z_2 \right) - \gamma_s h_s$$

$$v_3 = \frac{Q}{\pi d_3^2}$$

$$\gamma_w = 62.4 \frac{\text{lb}}{\text{ft}^3}$$

$$\gamma_s = 42.5$$

$$P_1 = 746 \frac{\text{lb}}{\text{ft}^2} = 5.18 \text{ psi}$$

$u = V_0(1 - e^{-cx})$

$\rightarrow u = V_0\left(\frac{1}{2}\right)(1 - e^{-cx})$

Centerline velocity is ~~at the center~~ $\vec{v} = \hat{i} V_0(1 - e^{-cx})\left(1 - \frac{x}{l}\right)$

if $V_0 = 10 \text{ ft/s}$ and $l = 5 \text{ ft}$

what value of C is the fluid acceleration equal to zero for any x at time $t = 1 \text{ s}$

$$a = \frac{d\vec{v}}{dt} = \frac{D\vec{v}}{Dt}$$

$$u = V_0(1 - e^{-cx})\left(1 - \frac{x}{l}\right)$$

$$v = 0$$

$$w = 0$$

$$a_x = \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z}$$

$$= V_0(c e^{-cx})\left(1 - \frac{x}{l}\right)$$

$$u \frac{\partial u}{\partial x} = V_0(1 - e^{-cx})\left(1 - \frac{x}{l}\right) \left(V_0(1 - e^{-cx})\left(-\frac{1}{l}\right) \right)$$

$$a_x = v_0 \left(1 - \frac{x}{l}\right) \left[c e^{-cx} - \frac{v_0}{l} (1 - e^{-cx})^2 \right]$$

at $x=l$ $a_x = 0$

$$c e^{-c} - \frac{v_0}{l} (1 - e^{-c})^2 = 0$$

expression for c

$$c = 0.49040396465$$