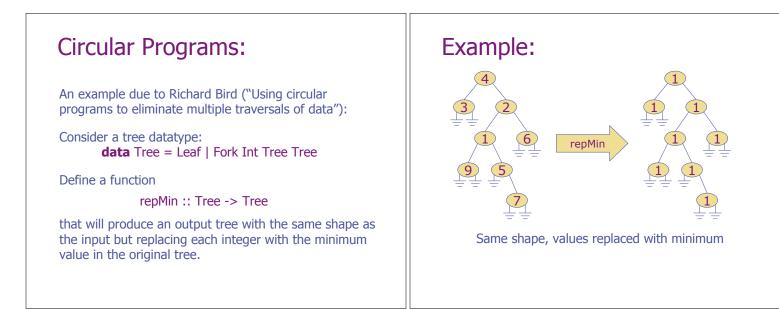
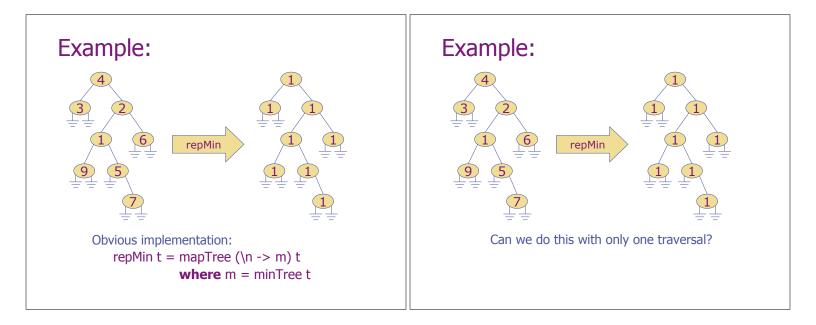
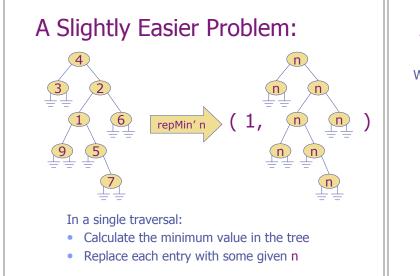
CS 457/557: Functional Languages	Lazy Evaluation:         With a lazy evaluation strategy:         - Don't evaluate until you have to         - When you do evaluate, save the result so that you can	
Leveraging Laziness	use it again next time Why use lazy evaluation?	
Mark P Jones Portland State University	<ul> <li>Why use lazy evaluation?</li> <li>Avoids redundant computation</li> <li>Eliminates special cases (e.g., &amp;&amp; and   )</li> <li>Facilitates reasoning</li> <li>Lazy evaluation encourages: <ul> <li>Programming in a compositional style</li> <li>Working with "infinite data structures"</li> <li>Computing with "circular programs"</li> </ul> </li> </ul>	

Compositional Style:	"Infinite" Data Structures:	
Separate aspects of program behavior separated into independent componentsfact n= product [1n]sumSqrs n= sum (map (\x -> x*x) [1n])minimum= head . sort	Data structures are evaluated lazily, so we can specify "infinite" data structures in which only the parts that are actually needed are evaluated: powersOfTwo = iterate (2*) 1 twoPow n = powersOfTwo !! n fibs = 0 : 1 : zipWith (+) fibs (tail fibs) fib n = fibs !! n	

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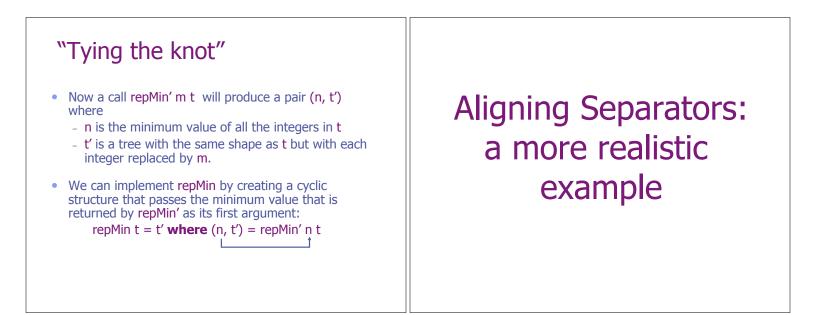
# A Single Traversal:

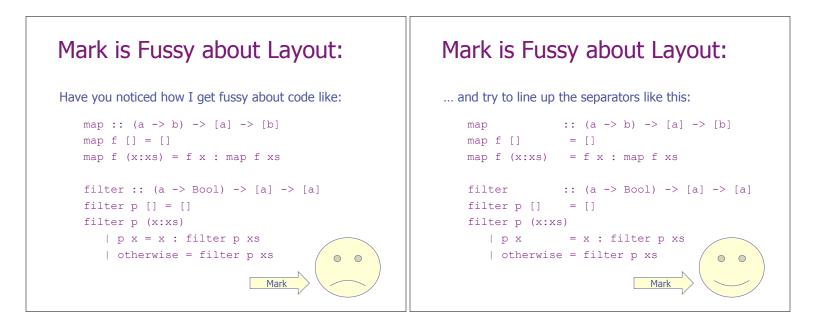
We can code this algorithm fairly easily:

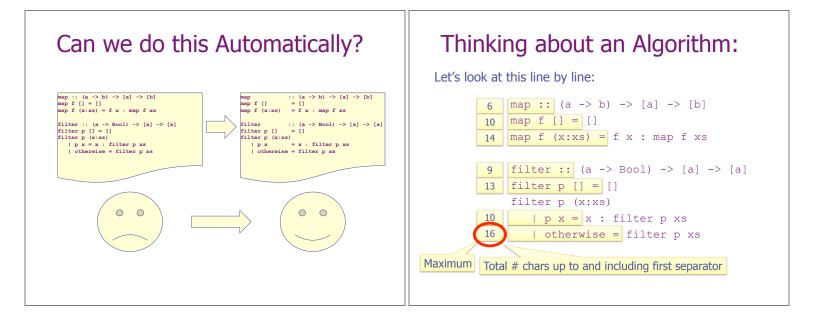
repMin' :: Int -> Tree -> (Int, Tree) repMin' n Leaf = (maxInt, Leaf) repMin' n (Fork m l r) = (min nl nr, Fork n l' r') where

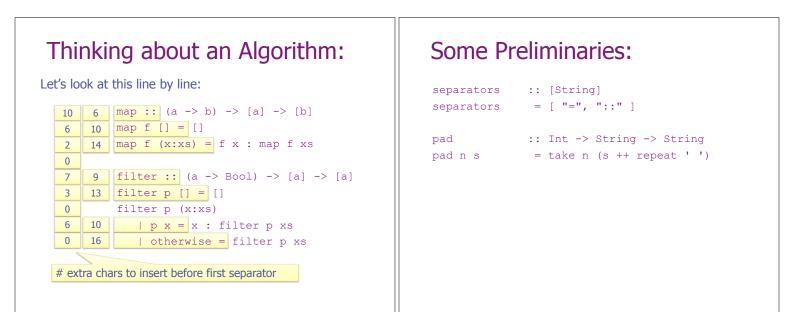
#### (nl, l') = repMin' n l

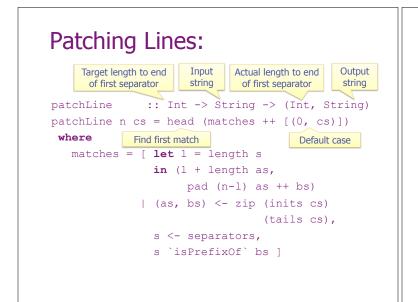
(nr, r') = repMin' n r



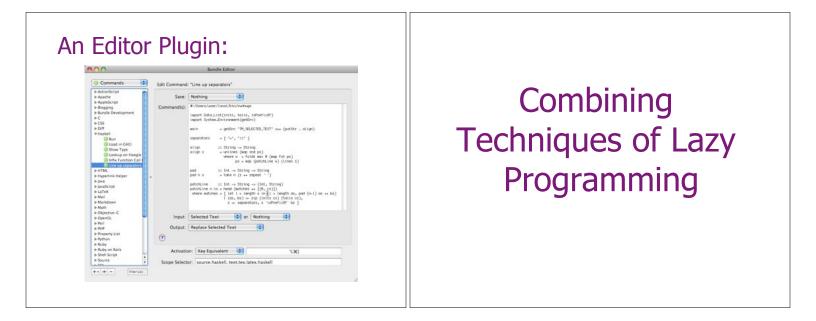




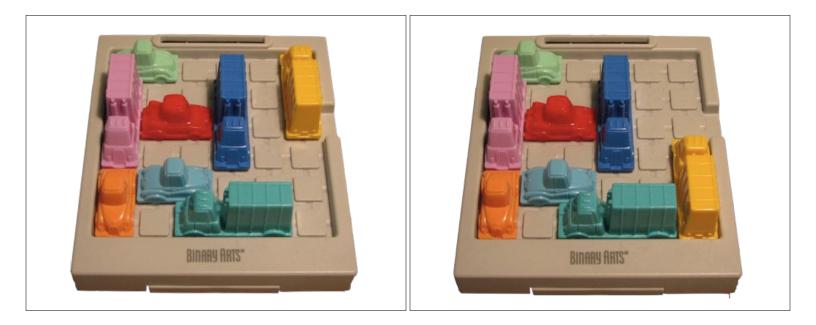


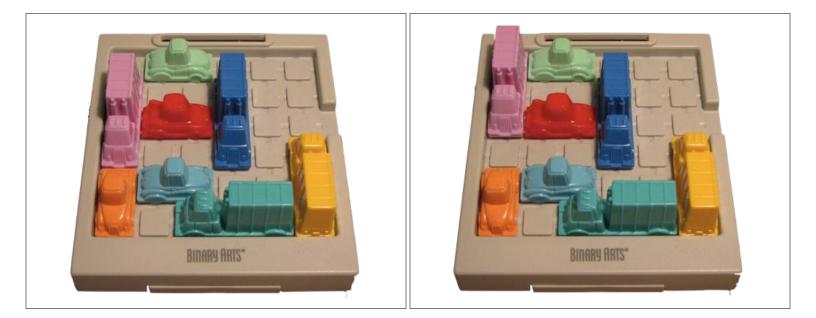


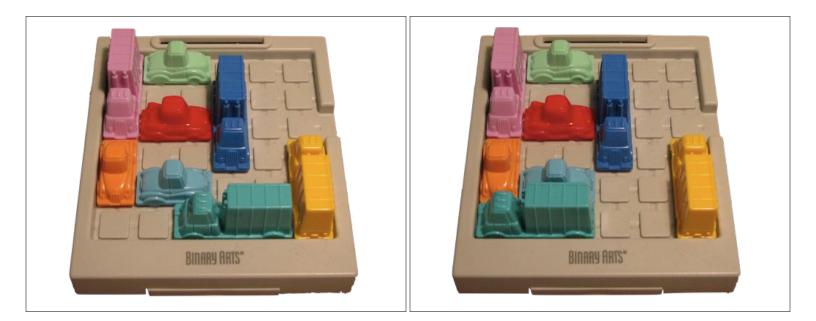
Tying the Knot (again):				
main :: main =	IO () getEnv "TM_SELECTED_TEXT" >>= (putStr . align)			
align s =	<pre>String -&gt; String unlines (map snd ps) w = foldr max 0 (map fst ps) ps = map (patchLine w) (lines s)</pre>			

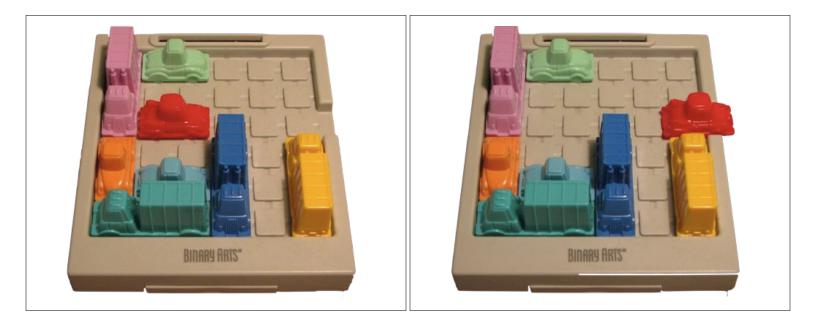






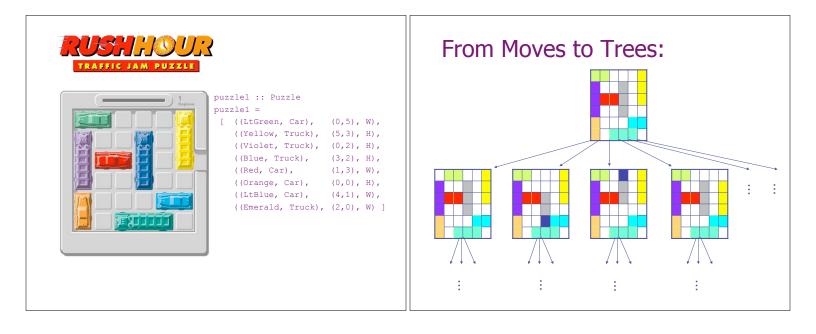






A Rush Hour Solver:	Representing the Board:	
Uses lazy evaluation in three important ways:	<pre>type Position = (Coord, Coord) type Coord = Int</pre>	
<ul> <li>Written in compositional style</li> <li>Natural use of an infinite data structure (a search tree that is subsequently pruned to a finite tree that eliminates duplicate puzzle positions)</li> <li>Cyclic programming techniques used to implement breadth-first pruning of the search tree.</li> </ul>	<pre>maxw, maxh :: Coord maxw = 6 maxh = 6</pre>	

Representing the Pieces:		Representing Puzzles:	
type Vehicle	e = (Color, Type)	<b>type</b> Puzzle <b>type</b> Piece	
<b>data</b> Color	= Red     Emerald <b>deriving</b> (Eq, Show)	<b>data</b> Orientation	= W   H
		vehicle	:: Piece -> Vehicle
data Type	= Car   Truck	vehicle (v, p, o)	= V
	deriving (Eq, Show)		:: Piece -> Bool = p == ((Red, Car), (4,3), W)
len	:: Type -> Int	r	
len Car	= 2		
len Truck	= 3		



# Checking for Obstructions:

## Calculating Moves:

moves :: Puzzle -> Piece -> [Piece] moves puzzle piece = step back piece ++ step forw piece where back :: Piece -> Maybe Piece back (v, (x, y), W)| x>0 && free p = Just (v, p, W)where p = (x-1, y). . . free = not . puzzleObstructs puzzle ::  $(a \rightarrow Maybe a) \rightarrow a \rightarrow [a]$ step = case dir p of step dir p Nothing -> [] Just p' -> p' : step dir p'

#### Forests and Trees:

## Making Trees:

splits :: [a] -> [([a], a, [a])]
splits xs = ... exercise to the reader ...

## Pruning the Tree:

- We want to avoid puzzle solutions in which the same piece is moved in two successive turns
- The generated tree may contain many instances of this pattern
- We can prune away repetition using: trimRel :: (a -> a -> Bool) -> Tree a -> Tree a trimRel rel (Node x cs) = Node x (filter (\(Node y \_) -> rel x y) cs)

# Eliminating Duplicate Puzzles:

- We don't want to explore any single puzzle configuration more than once
- We want to find shortest possible solutions (requires breadth-first search of the forest)

