

CS 410/510

Languages & Low-Level Programming

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Fall 2018

Week 10: Abstractions and Performance

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The CEMLaBS Project

- "Using a Capability-Enhanced Microkernel as a Testbed for Language-Based Security"
- Started October 2014, Funded by The National Science Foundation
- Three main questions:
 - **Feasibility**: Is it possible to build an inherently "unsafe" system like seL4 in a "safe" language like Habit?
 - **Benefit**: What benefits might this have, for example, in reducing verification costs?
 - **Performance**: Is it possible to meet reasonable performance goals for this kind of system?

Chipping away ...

based on seL4

HaL4: A CapabilityEnhanced Microkernel
Implemented in Habit

Chipping away ... HaL4:A CapabilityEnhanced Microkernel Implemented in Habit based on Haskell

Opportunities for high-level abstractions?

- Are there good uses for higher-level abstractions in bare metal programming?
 - Algebraic datatypes?
 - First class and higher-order functions?
 - Classes and objects?
 - ...
- And with concerns about performance, can we afford to use them?

Algebraic Datatypes

Sums types and product types

• A **sum type** allows us to capture alternatives:

• A **product type** allows us to package multiple values up as a single, composite value:

(tuples, arrays, records, structures, etc. are also examples of of product type)

Algebraic datatypes

• **Algebraic datatypes** provide a unified framework for sum and product types as well as arbitrary sums of products:

```
-- Haskell
data Maybe a = Nothing | Just a
data Either a b = Left a | Right b

// Rust
enum Option<T> { None, Some(T) }
enum Result<T, E> { Ok(T), Err(E) }
```

- These examples are taken from the standard libraries of the respective languages
- They are also examples of **parameterized types**, allowing reuse over many type parameter combinations

Constructing values of algebraic datatypes

 To make a value of an algebraic datatype, just write the constructor followed by an appropriate list of arguments:

In Haskell:

- Nothing and Just 12 are values of type Maybe Int
- Left True and Right "hello" are values of type Either Bool String

In Rust:

- None and Some(12) are values of type Option<i32>
- Ok(true) and Err("hello") are values of type Result<bool, String>

0

Using values of algebraic datatypes

• We use **pattern matching** constructs to inspect and extract data from values of algebraic datatypes:

In Haskell, assuming val has type Maybe String:

```
case val of
    Nothing -> "I don't know your name"
    Just name -> "hello " ++ name

In Rust, assuming val has type Option<String>:
    match val {
        None => "I don't know your name"
        Some(name) => "hello " + name
```

Representing values of algebraic datatypes

- Language definitions typically do not specify exactly how values of algebraic datatypes are represented
- Two common approaches:

Boxed representations: Every value is described by a pointer to a block of memory:



Union representations: Every value is described by a block of memory big enough to store any value of that type:



Algebraic datatypes + recursion

 Algebraic datatypes become even more powerful when combined with **recursion**:

```
-- Haskell
data List a = Nil | Cons a (List a)
// Rust
enum List<A> { Nil, Cons(Box<(A, List<A>)>)}
```

- (Box<T> is the Rust type for boxed values of type T)
- Example: Cons 1 (Cons 2 (Cons 3 (Cons 4 Nil))) is a value of type List Int (might also be written [1, 2, 3, 4])
- Unsurprisingly, we can define recursive functions to work with recursive types like these ...

Algebraic datatypes using classes

• We can simulate algebraic datatypes with OO classes:

```
abstract class List<A> {
   Cons isCons() { return null; }
}
class Nil<A> extends List<A> { }
class Cons<A> extends List<A> { }
A head;
List<A> tail;
Cons(A head, List<A> tail) {
   this.head = head;
   this.tail = tail;
}
Cons isCons() { return this; }
}
```

- More verbose, but also more extensible
- Combines/tangles type and code definitions in classes

14

Habit's bitdata types

 The Habit programming language provides special syntax for defining bitdata types:

- A crucial feature of definitions like these is the ability to specify bit-level representations/layout
- In other respects, bitdata types are like algebraic datatypes:
 - Construct and update values without use of <<, &, |, etc.

15

Pattern match to deconstruct values

Example: IA32 Paging Structures

31 30 29 21	3 27 26 25 24 23 22	21 20 19 18 17	16 15 14 13	12	11 10 9	8	7	6	5	4	3	2	1	0	
Address of page directory ¹						Ignored				PCD	PW T	N Ignored			CR3
	1:22 of address MB page frame	Reserved (must be 0)	Bits 39:32 of address ²	P A T	Ignored	G	1	D	Α	P C D	PW T	U / S	R / W	1	PDE: 4MB page
	Address of page table Ignored Q G A C PW U R T S Y Y Y X Y Y X Y Y X Y Y								1	PDE: page table					
Ignored									Q	PDE: not present					
Address of 4KB page frame Ignored G A T D A C P PW J A C D T S W								1	PTE: 4KB page						
Ignored								<u>o</u>	PTE: not present						

Figure 4-4. Formats of CR3 and Paging-Structure Entries with 32-Bit Paging

16

Example: IA32 Paging Structures

Here is how we describe page directory entries in Habit:

```
bitdata PDE /WordSize -- Page Directory Entries

= UnmappedPDE [ unused=0 :: Bit 31 | B0 ] -- Unused entry (present bit reset)

| PageTablePDE [ ptab :: Phys PageTable | -- physical address of page table | unused=0 | :: Bit 4 | -- signals PageTablePDE | attrs=readWrite :: PagingAttrs | -- paging attributes | -- present bit set

| SuperPagePDE [ super | :: Phys SuperPage | unused=0 | :: Bit 1 | -- physical address of superpage | unused=0 | :: Bit 1 | -- signals SuperPagePDE | super | -- physical address of superpage | unused=0 | :: Bit 1 | -- paging attributes | -- pag
```

Example: IA32 Paging Structures

And here is how we might write functions that use these definitions to implement useful operations on paging structures:

```
mapPage pdir virt phys
= case<- readRef (pdir @ virt.dir) of

UnmappedPDE -> ... add page table and map page ...
SuperPagePDE[] -> ... superpage already mapped ...
PageTablePDE[ptab] ->

case<- readRef (fromPhys ptab @ virt.tab) of

MappedPTE[] -> ... page already mapped ...
UnmappedPTE -> ... map the page ...
```

There are no messy bit-level operations to worry about here: all of that is handled automatically by bitdata mechanisms ...

First-class Functions and Higher-order Functions

First-class functions

• A lot of modern programming languages provide mechanisms for writing down anonymous functions / lambda expressions:

Haskell	\x -> x + 1
LISP	(lambda (x) (+ x 1))
Python	lambda x: x + 1

	Javascript	function (x) x + 1
	C++ 11	[] (int x) -> int { return x + 1; }
	Rust	x (x + 1)

- These expressions construct functions as **first class** values:
 - they can be passed as arguments to other functions
 - · returned as results
 - · stored in data structures

Higher-order functions

- Higher-order functions are functions that take other functions as inputs or return functions as outputs
- compose and map are classic examples of higher-order functions

```
map = \f xs \rightarrow
        case xs of
                     -> Nil
          Nil
          Cons y ys -> Cons (f y) (map f ys)
```

For example:

```
map (\x -> x + 1) [1,2,3,4] == [2,3,4,5]
map (\x -> 2 * x) [1,2,3,4] == [2,4,6,8]
```

· Good for capturing recurring patterns as reusable functions

22

Simple examples

• The identity function:

id has a polymorphic type: lt can be treated as a function of type t -> t for any type t

add has type Int -> Int -> Int

succ has type Int -> Int

 $id = \langle x - \rangle x$

• The "successor" function $succ = \langle x -> x + 1 \rangle$

• The "add" function

add = $\x -> (\y -> x + y)$

• The "compose" function

compose has type (b -> c) -> (a -> b) -> (a -> c)

compose = $f \rightarrow g \rightarrow x \rightarrow f (g x)$

First-class functions using classes

• We can use OO classes to represent first-class functions:

```
abstract class Func<A, B> {
   abstract B applyTo(A arg);
class Id<A> extends Func<A, A> {
    A applyTo(A arg) { return arg; }
class Succ extends Func<int, int> {
   int applyTo(int arg) { return arg + 1; }
```

- Objects that represent first-class functions are called closures
- Some language descriptions even use the term "closure" instead of "first-class function"

First-class functions using classes, continued

• We can build closures for functions with multiple arguments:

```
class Add1 extends Func<int, int> {
   private int n;
   new Add1(int n) { this.n = n: }
   int applyTo(int arg) { return arg + n; }
class Add extends Func<int, int> {
   Func<int, int> applyTo(int arg) { return new Add1(n); }
```

• Sample use:

```
new Add().applyTo(1).applyTo(2) ===> returns 3
```

- A single class can have many methods, which might require multiple functions
- But the verbose notation can discourage users ...

Functions vs procedures

- In many languages, the terms "function" and "procedure" are used almost interchangeably
- In Habit, they are different!
- A function is a value of type a -> b for some input type a and output type b

For any given input value, a function always produces the same output value

A procedure is a value of type Proc a for some result type a
 Every time it is executed, a procedure can have a side effect
 and produce a result of type a (both which could be different
 every time ...)

Combining functions and procedures

• We can use these together to describe procedures with arguments

a pure function.

• Compare:

 $A_1 \rightarrow A_2 \rightarrow \dots \rightarrow R$ $A_1 \rightarrow A_2 \rightarrow \dots \rightarrow R$ $A_1 \rightarrow A_2 \rightarrow \dots \rightarrow Proc R$ a parameterized procedure, may have side effects

no side effects

• A typical C prototype for a function like this:

R f(A₁ arg₁, A₂ arg₂, ...)

no guarantees, could do almost anything!

26

Why is this useful?

I. We can distinguish between procedures that can have side effects and pure functions that do not

Useful documentation; simplifies reasoning; enables optimizations

2. We can generalize to support multiple procedure types:

Proc a for regular procedures

Init a for procedures that can only run during kernel initialization

Now we can enforce restrictions on the use of functions that should only be called during initialization (e.g., allocPage() in the capabilities lab) via compile-time type checking

Talk to me for further details; this is related to "Monads" in functional programming

27

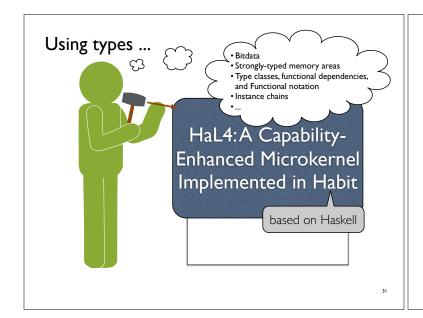
Opportunities for high-level abstractions?

- Are there good uses for higher-level abstractions in bare metal programming?
 - Algebraic datatypes?
 - First class and higher-order functions?
 - Classes and objects?
 - ...
- And with concerns about performance, can we afford to use them?

28

A small case study:
The Multiboot Information Structure



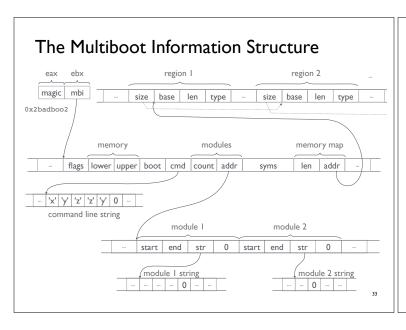


Booting a PC via GRUB

When you turn on a PC:

- The CPU initializes itself and performs a self test, before jumping to a known address in the BIOS ROM
- The BIOS searches for a "bootable device" and loads a 446 byte program into memory from its first sector (the MBR)
- The MBR code uses BIOS functions to load a full featured boot loader (GRUB) in to memory
- GRUB searches the disk for a configuration file and interprets the commands there to load a full featured OS in to memory
- The OS configures itself using information passed in from GRUB via a "Multiboot Information Structure"

32

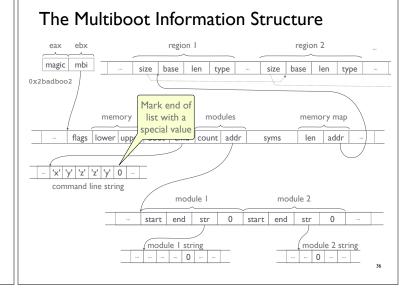


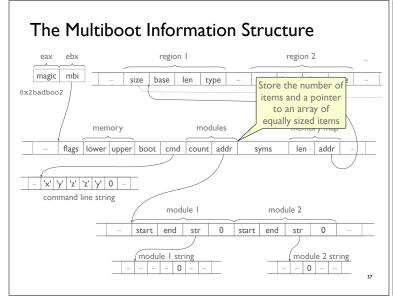
The Multiboot Information Structure, in C

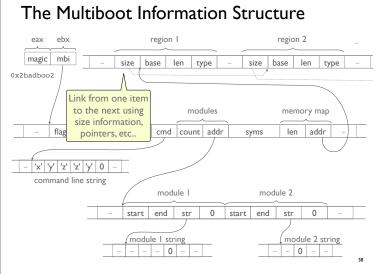
```
struct MultibootModule
extern struct MultibootInfo* mbi;
                              mbi_magic;
extern unsigned
                                              unsigned modStart:
#define MBI_MAGIC 0x2BADB002
                                              unsigned modEnd;
                                                       modString;
struct MultibootInfo {
                                              unsigned reserved;
 unsigned
                           flags;
                                            };
# define MBI_MEM_VALID
                           (1 << 0)
                           (1 << 2)
# define MBI_CMD_VALID
# define MBI MODS VALID
                                            struct MultibootMMap {
                           (1 << 3)
                                              unsigned size:
# define MBI_MMAP_VALID
                                              unsigned baseLo;
                                              unsigned baseHi;
  unsigned
                           memLower:
                                              unsigned lento:
  unsigned
                           memUpper;
                                              unsigned lenHi;
  unsigned
                           bootDevice;
                                              unsigned type;
  char*
                           cmdline:
                                            };
  unsigned
                           modsCount;
                                             Intentionally or otherwise,
  struct MultibootModule*
                           modsAddr;
  unsigned
                           syms[4];
                                              the multiboot designers
                           mmapLength:
  unsigned
                                             used multiple techniques
                           mmapAddr;
  unsigned
                                               to represent variable-
                                                length components
```

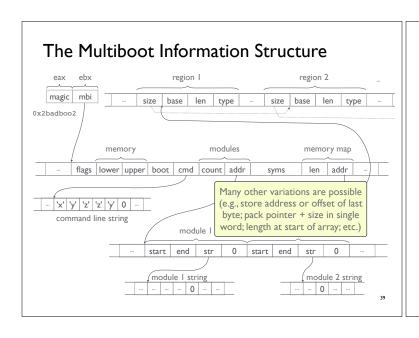
Representing variable length components

- Intentionally or otherwise, the multiboot designers used multiple techniques to represent variable-length components:
 - Mark end of list with a special value, no need to store the length explicitly
 - $^{\circ}$ Store the number of items and a pointer to the first (0th) entry in an array of equally sized items
 - Store the size (in bytes) of the array with a pointer to (some known position in) the first item; access later items by an offset (or pointer) to allow for varying item sizes
- Many other variations are possible (e.g., store address or offset of last byte; pack pointer + size in single word; ...)









Programming challenges

- What could go wrong if we're writing C programs to work with a Multiboot Information Structure?
 - How do we enforce checking for the magic number?
 - · How do we identify/access individual flag bits?
 - How do we find the start of a variable length component?
 - How do we move to the next component?
 - How do we determine when we have reached the end?
 - How do we prevent access to adjacent regions of memory that are not part of the Multiboot Information Structure?
- Current practices to avoid/minimize errors: Disciplined programming; Code reviews; Extensive testing; Limit revisions.
- Do modern language designs have anything to offer here?

40

Abstract types

- Instead of exposing the underlying pointer type, with full (and unsafe) pointer arithmetic, we could use an *abstract type*
 - Key idea: separate specifications from implementations
- **Specification**: We can work with null-terminated strings by introducing a type AsciiZ with a single operation:

next :: AsciiZ -> Proc (Maybe (Char, AsciiZ))

- **Implementation**: An AsciiZ value is a (non-null) pointer to a null-terminated string of characters
 - next s returns Just (c, s1) if s points to character c and the remainder of the string is s1
 - Otherwise next s returns Nothing

Notes

- The next operation encapsulates checking for null, reading a character, and incrementing the pointer in a single operation
- In general, an abstract type's design should:
 - ensure safety (leverage types)
 - avoid redundant computation (e.g., repeated tests)
 - allow for an efficient implementation ...
- Don't underestimate the challenges of figuring out a good design!

Cursors

 This approach generalizes quite easily to handle other components of the MultiBoot Information Structure as well as other table and tree structures in low-level code

```
next :: Cursor -> Proc (Maybe (Val, Cursor))
```

- For example, we could traverse an array using a Cursor that encapsulates two components:
 - The number of remaining elements
 - A pointer to the current element

A sample consumer of Asciiz strings

• Using some notation from Habit:

- A simple implementation of next would construct a value of the form Just (c,s1) for every character in the string
 - ⇒ Significant heap allocation, performance will suffer
 - ⇒ Garbage collection; predictability will be compromised
 - ⇒ Heavyweight approach: a single pointer is all you need ...
- It might be hard to get good performance out of this ...

43

45

A sample consumer of Asciiz strings

• Using some notation from Habit:

• putStr immediately consumes values produced by next

A sample consumer of Asciiz strings

• Using some notation from Habit:

putStr immediately consumes values produced by next
 a whole program optimizer should be able to fuse the code
 for the two functions to eliminate the overhead ...

46

The compiled version of putStr

```
putStr <- k54{}</pre>
                                   b102[t555, t556] =
                                     t557 <- incAsciiz((t555))
k54{} t564 = k53{} t564{}
                                     [] <- putChar((t556))
                                     t558 <- readChar((t557))
                                     t559 <- nullChar((t558))
k53\{t563\} [] = b97[t563]
                                     if t559
b97[t560] =
                                       then b96[]
                                       else b102[t557, t558]
  t561 <- readChar((t560))
  t562 <- nullChar((t561))
                                  b96[] = return Unit
  if t562
    then b96[]
    else b102[t560, t561]
                                  Unit <- Unit()</pre>
```

Key details:

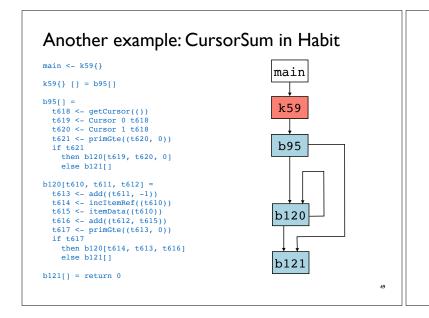
- No allocation in the main putStr loop (i.e., in block b102)!
- Simple pointers

Another example: CursorSum in Habit

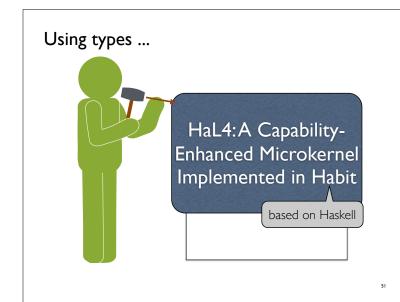
Add a collection of items accessed via a cursor:

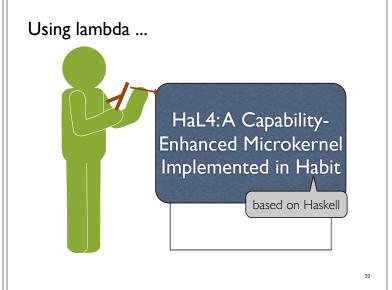
Things to note: higher-order functions, pattern matching, monads, polymorphic types, etc...

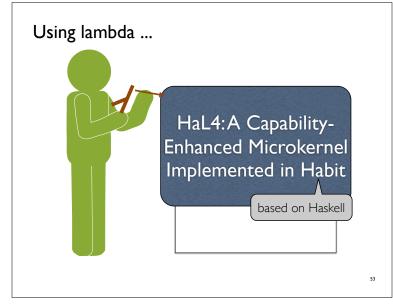
Things to ignore: everything else!



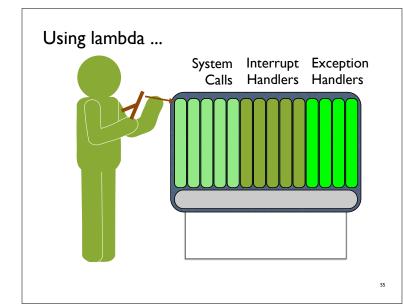
Another Case Study: System Call Validators

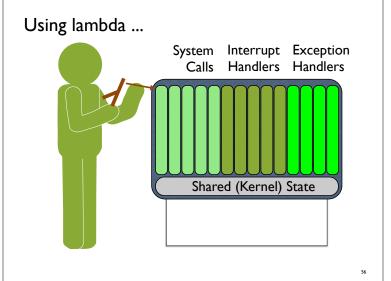


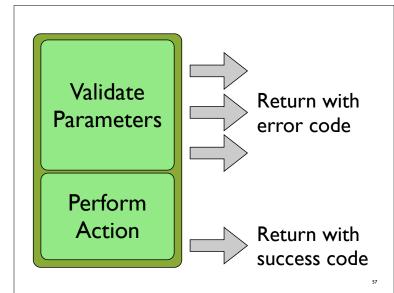


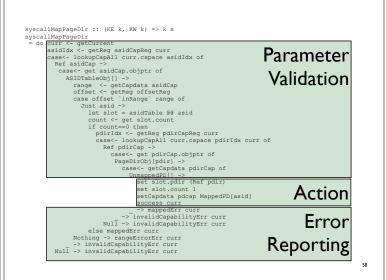












Imperative Functional Programming

• Traditional sequential control flow

```
do f <- openFile "file.txt"
  l<sub>1</sub> <- readLine f
  l<sub>2</sub> <- readLine f
  out (l<sub>1</sub>, l<sub>2</sub>)
  closeFile f
```

- How to deal with errors? multiple results?
 - Make functions return error codes (and hope that callers will check those codes)?
 - · Add the ability to throw and catch exceptions?
 - Use continuations ...

Programming with continuations

• Instead of

```
openFile :: String -> Proc FileHandle

• Try:

openFile :: String

-> (ErrorCode -> Proc a)

-> (FileHandle -> Proc a)

-> Proc a
```

 It's as if we've given openFile two return addresses: one to use when an error occurs, and one to use when the call is successful.

Programming with continuations

• Our original program using continuations:

```
openFile "file.txt"

(\error -> ...)

(\f -> do l_1 <- readLine f

l_2 <- readLine f

out (l_1, l_2)

closeFile f)
```

• Could we do the same for readLine?

Programming with continuations

• Our original program using continuations:

• Hmm, not so pretty ...

62

Programming with continuations

• Name the error handlers:

```
openFile "file.txt"
  err1
  (\f -> readLine f
      err2
      (\l1 -> readLine f
        err3
        (\l2 <- do out (l1, l2)
        closeFile f)))</pre>
```

Programming with continuations

• Reformat:

```
openFile "file.txt" err1 (\f -> readLine f err2 (\lambda l_1 -> do out (l_1, l_2) closeFile f)))
```

• Looking better ...

64

Programming with continuations

• Add an infix operator: $f \ x = f x$

```
openFile "file.txt" err1 $ \f -> readLine f err2 $ \lambda \lambda_1 -> do out (l_1, l_2) closeFile f
```

- Fewer parentheses ...
- Easier to add or remove individual lines ...
- ... still a little cluttered by error handling behavior

Programming with continuations

• Continuation-based control flow, integrated error handlers:

- Not always applicable ...
- ... but a good choice for HaL4 where the response to a particular type of invalid parameter is always the same (typically, returning an error code to the caller)
- ... and this also encourages consistent API behavior

6

63

"Validators"

The implementation of prototype HaL4 includes a small library of validator functions:

```
getCurrent
                       :: KR k \Rightarrow (TCBRef \rightarrow k a) \rightarrow k a
getRegCap
                       :: KE k => #r -> TCBRef
                                         \rightarrow (CapRef \rightarrow k a) \rightarrow k a
emptyCapability
                       :: KE k => TCBRef -> CapRef -> k a -> k a
cdtLeaf
                       :: KE k => TCBRef -> CapRef -> k a -> k a
                       :: KE k => TCBRef -> CapRef -> k a -> k a
notMaxDepth
                      :: KE k => TCBRef -> CapRef
untypedCapability
                                    \rightarrow (UntypedRef \rightarrow k a) \rightarrow k a
pageDirCapability :: KE k => TCBRef -> CapRef
                      -> (PageDirRef -> PDMapData -> k a) -> k a
pageTableCapability :: KE k => TCBRef -> CapRef
                      -> (PageTableRef -> MapData -> k a) -> k a
```

"Validators"

- In effect, we have built an embedded domain specific language, just for validating parameters in HaL4
- Benefits include:
 - · Ease of reuse
 - Consistency
 - Clarity
 - Ability to pass multiple results on to continuation

```
syscallMapPageDir :: (KE k, KW k) => k a
syscallMapPageDir
  getCurrent
                                        \curr
   getMapPageDirASIDTab curr
                                       \asidcap
                                                   ->
   asidTableCapability curr asidcap
                                       \range
   getMapPageDirOffset curr
                                     $ \offset
                                                   ->
   asidInRange curr offset range
                                     Ś
                                       \asid
                                                   ->
   asidNotUsed curr asid
                                       \slot
                        Validators
                                     $ \pdcap
   getMapPageDirPDir curr
                                                   ->
   pageDirCapability curr pdcap
                                       \pdir pdmd ->
   unmappedPD curr pdmd
  do set slot.pdir (Ref pdir)
                                            Action
      set slot.count 1
      setCapdata pdcap MappedPD[asid]
      success curr
```

syscallMapPageDir :: (KE k, KW k) => k a syscallMapPageDir \$ \curr = getCurrent -> getMapPageDirASIDTab curr \$ \asidcap asidTableCapability curr asidcap \$ \range getMapPageDirOffset curr \$ \offset -> asidInRange curr offset range \$\asid -> asidNotUsed curr asid \$ \slot -> getMapPageDirPDir curr \$ \pdcap -> pageDirCapability curr pdcap \$ \pdir pdmd -> unmappedPD curr pdmd do set slot.pdir (Ref pdir) "clear" and set slot.count 1 setCapdata pdcap MappedPD[asid] "concise" success curr

70

```
syscallMapPageDir :: (KE k, KW k) => k a
syscallMapPageDir
  getCurrent
                                      $\curr
                                                   ->
   getMapPageDirASIDTab curr
                                        \asidcap
                                                   ->
   asidTableCapability curr asidcap
                                        \range
                                                   ->
   getMapPageDirOffset curr
                                      $ \offset
                                                   ->
   asidInRange curr offset range
                                        \asid
                                                   ->
   asidNotUsed curr asid
                                      Ś
                                        \slot
                                                   ->
   getMapPageDirPDir curr
                                      $ \pdcap
                                      Ś
   pageDirCapability curr pdcap
                                        \pdir pdmd ->
  unmappedPD curr pdmd
   do set slot.pdir (Ref pdir)
     set slot.count 1
                                          reusable
      setCapdata pdcap MappedPD[asid]
      success curr
```

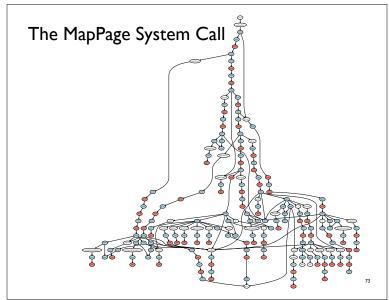
```
syscallMapPageDir :: (KE k, KW k) => k a
syscallMapPageDir
 = getCurrent
                                     $\curr
   getMapPageDirASIDTab curr
                                       \asidcap
                                                   ->
                                     $ \range
   asidTableCapability curr asidcap
                                                   ->
   getMapPageDirOffset curr
                                      $ \offset
                                                   ->
   asidInRange curr offset range
                                      $ \asid
                                                   ->
   asidNotUsed curr asid
                                     $\slot
                                                   ->
   getMapPageDirPDir curr
                                     $ \pdcap
                                        \pdir pdmd ->
   pageDirCapability curr pdcap
   unmappedPD curr pdmd
   do set slot.pdir (Ref pdir)
```

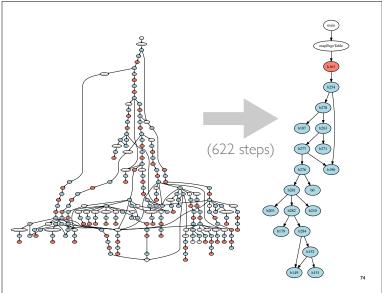
set slot.count 1

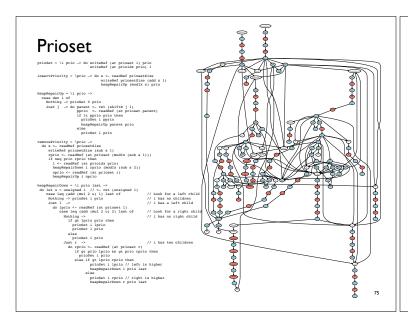
success curr

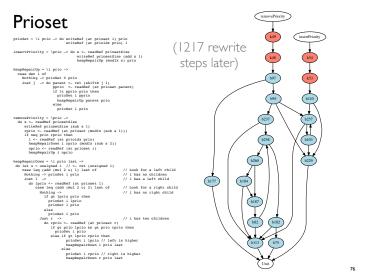
setCapdata pdcap MappedPD[asid]

performance concerns?









Wrapping Up ...

Current status

- For the three main questions for CEMLaBS:
 - **Feasibility**: Still chipping away ... but getting closer!
 - **Benefit**: Good evidence that we will benefit from the use of functional language features
 - +Types
 - +Higher-order functions
 - **Performance**: acceptable performance may be within reach
 - +We can generate good quality code, even when lambdas are used in fundamental ways
 - +Some code duplication (but, so far, this is entirely tolerable for our specific use case ...)

Acknowledgement (likely incomplete!)

Numerous people at PSU (and beyond) have contributed to the design and implementation of Habit, including:

- Michael Adams
- Aaron Altman
- Justin Bailey
- Tim Chevalier
- Lewis Coates
- Ted Cooper
- Dan Cristofani
- lavor Diatchki
- Thomas DuBuisson

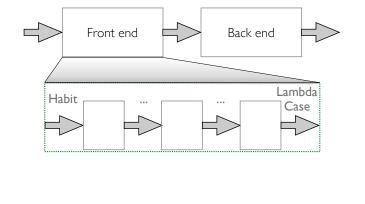
- Thomas Hallgren Andrew
- Tom Harke
- Caylee Hogg
- Jim Hook
- Brian Huffman
- Mark Jones
- Rebekah Leslie-
- Dick Kieburtz
- Hurd

- Kenneth Graunke John Matthews

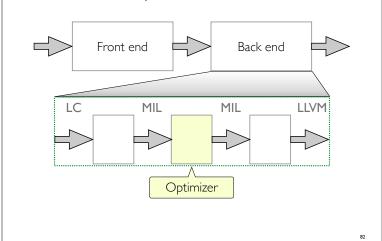
 - McCreight
 - Garrett Morris
 - Ryan Niebur
 - Andrew
 - Sackville-West
 - Andrew Tolmach
 - Peter White
 - ...

Some Words about the Habit Implementation

The Habit Compiler



The Habit Compiler



Why MIL?

- If we want a good optimizer, we need to work in a language that exposes key implementation details/sources of overhead
- Constructing a closure: k{x₁, ..., x_n}
 - code pointer: k
 - stored fields: x₁, ..., x_n
- Entering a closure: If f is a closure, then we write f @ x for the result of entering f with argument x
- Defining a closure: $k\{x_1, ..., x_n\}$ a = t
 - The code in t describes the result that is produced when you enter the closure with argument a

From Functional Source Code ...

... to MIL Programs

```
compose \leftarrow k_1\{\}
          \leftarrow k_0\{\}
                                  k_1\{\}\ f = k_2\{f\}
k_0\{\} x = b_0[x]
                                  k_2\{f\} g = k_3\{f,g\}
b_0[x] = return x
                                  k_3\{f,g\} x = b_1[f,g,x]
                \leftarrow k_4\{\}
                                  b_1[f,g,x] = y \leftarrow g @ x
k_4\{\} f
                = k_5\{f\}
k_5\{f\} xs
                = b_2[f,xs]
b_2[f,xs]
                = case xs of
                      Nil() \longrightarrow b_3[]
                      Cons(y,ys) \rightarrow b_4[f,y,ys]
                = Nil()
b_4[f,y,ys] = z \leftarrow f @ y
                                         Intuition: arguments are like
                                         registers that have been
                 m ← map @ f
                                         loaded with values on entry
                   zs ← m @ ys
                                         to a basic block of code
                   Cons(z,zs)
```

... to Optimized MIL Programs

... to Optimized MIL Programs

```
\begin{array}{lll} \text{map} & \leftarrow k_4 \{ \} \\ k_4 \{ \} \ f & = k_5 \{ f \} \\ k_5 \{ f \} \ xs & = b_2 [ f, xs ] \\ b_2 [ f, xs ] & = \text{case } xs \text{ of } \\ & & \text{Nil}() \longrightarrow b_3 [ ] \\ & & \text{Cons}(y,ys) \longrightarrow b_4 [ f,y,ys ] \\ b_3 [ ] & = \text{Nil}() \\ b_4 [ f,y,ys ] & = z \leftarrow f @ y \\ & & \text{m} \leftarrow \text{map } @ f \\ & & \text{zs} \leftarrow m @ ys \\ & & \text{Cons}(z,zs) \\ \end{array}
```

... to Optimized MIL Programs

... to Optimized MIL Programs

```
\begin{array}{lll} \text{map} & \leftarrow k_4 \{ \} \\ k_4 \{ \} \ f & = k_5 \{ f \} \\ k_5 \{ f \} \ xs & = b_2 [ f, xs ] \\ b_2 [ f, xs ] & = \text{case } xs \text{ of } \\ & \text{Nil}() \longrightarrow b_3 [ ] \\ & \text{Cons}(y,ys) \longrightarrow b_4 [ f,y,ys ] \\ b_3 [ ] & = \text{Nil}() \\ b_4 [ f,y,ys ] & = z \leftarrow f @ y \\ & \text{m} \leftarrow k_5 \{ f \} \\ & \text{zs} \leftarrow \text{m} @ ys \\ & \text{Cons}(z,zs) \end{array}
```

... to Optimized MIL Programs

```
\leftarrow k_4\{\}
map
k_4\{\} f
                = k_5\{f\}
k_5\{f\} xs = b_2[f,xs]
b_2[f,xs]
             = case xs of
                      Nil() \longrightarrow b_3[]
                       Cons(y,ys) \longrightarrow b_4[f,y,ys]
                = Nil()
b<sub>3</sub>[]
b_4[f,y,ys] = z \leftarrow f @ y
                                            pure, dead code
                    m \leftarrow k_5\{f\}
                    zs \leftarrow b_2[f,ys]
                    Cons(z,zs)
```

... to Optimized MIL Programs

```
\begin{array}{lll} \text{map} & \leftarrow k_4 \{ \} \\ k_4 \{ \} \ f & = k_5 \{ f \} \\ k_5 \{ f \} \ xs & = b_2 [ f, xs ] \\ b_2 [ f, xs ] & = \text{case } xs \text{ of } \\ & & \text{Nil}() \longrightarrow b_3 [ ] \\ & & \text{Cons}(y,ys) \longrightarrow b_4 [ f,y,ys ] \\ b_3 [ ] & = \text{Nil}() \\ b_4 [ f,y,ys ] & = z \leftarrow f @ y \\ & & zs \leftarrow b_2 [ f,ys ] \\ & & \text{Cons}(z,zs) \end{array}
```

MIL Optimization

- Basic strategy:
 - many small rewrites
 - combined in large numbers
- Sources of rewrites:
 - algebraic laws
 - simple data flow
 - specialization and derived blocks

92