

# Quantum Dots and Quantum Dot Cellular Automata

- **SOURCES:**

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# 2.1 What are Quantum Dots?

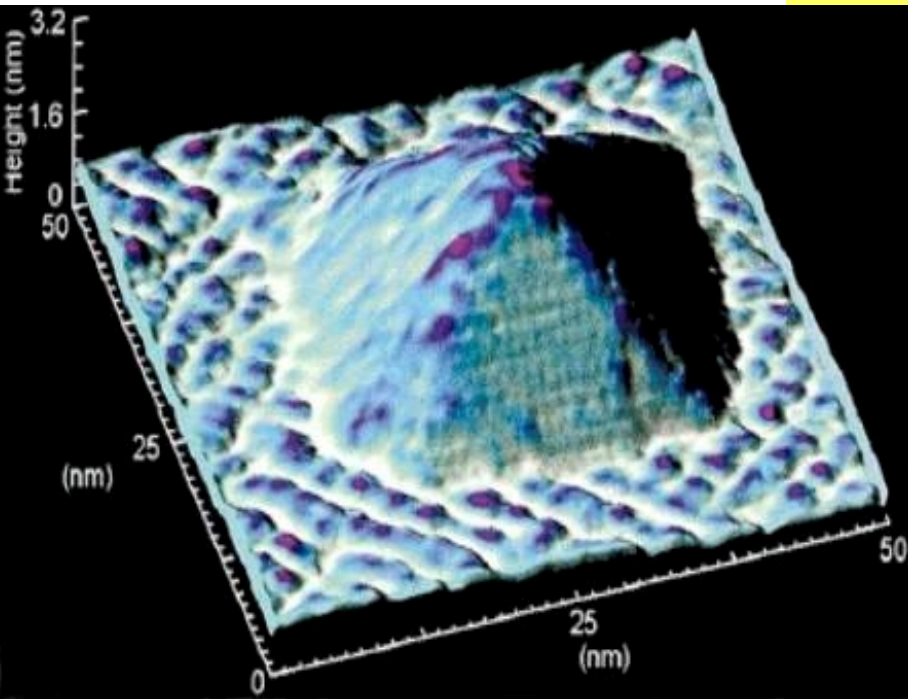
- In order to implement a system that encodes information in the form of electron position it becomes necessary to construct a vessel in which an electron can be trapped and "counted" as there or not there.
- A quantum dot does just this by establishing a region of low potential surrounded by a ring of high potential.
- See Figure 1.
- Such rings are able to trap electrons of sufficiently low energies/temperature and are sometimes called **potential wells**.
- There are several ways to implement quantum dots but apparently the most common, and the ones used in [1] are metal.
- Nanometer-scale dots are constructed from Aluminum using electron beam lithography techniques.

# WHAT ARE QUANTUM DOTS?

- The logic unit in QCA is the QCA cell which was proposed by researchers at the University of Notre Dame.
- The QCA cell is composed of 4 or 5 quantum dots.
- Before we examine the potential functionality of these cells we need to know a few basic facts about quantum dots.
- A **quantum dot** is a nanometer sized structure that is capable of **trapping electrons in three dimensions**.
- Quantum dots are made by creating an **island of conductive material** surrounded by insulating material.
- Electrons that enter the quantum dot will be confined because of the **high potential required to escape**.

# Why are Quantum Dots important?

- Quantum dots will become the backbone of future microelectronic and photonic devices:
  - because of their unique properties due to **quantum confinement of electrons in 3-dimensions**
  - this results in interesting electronic and optical properties

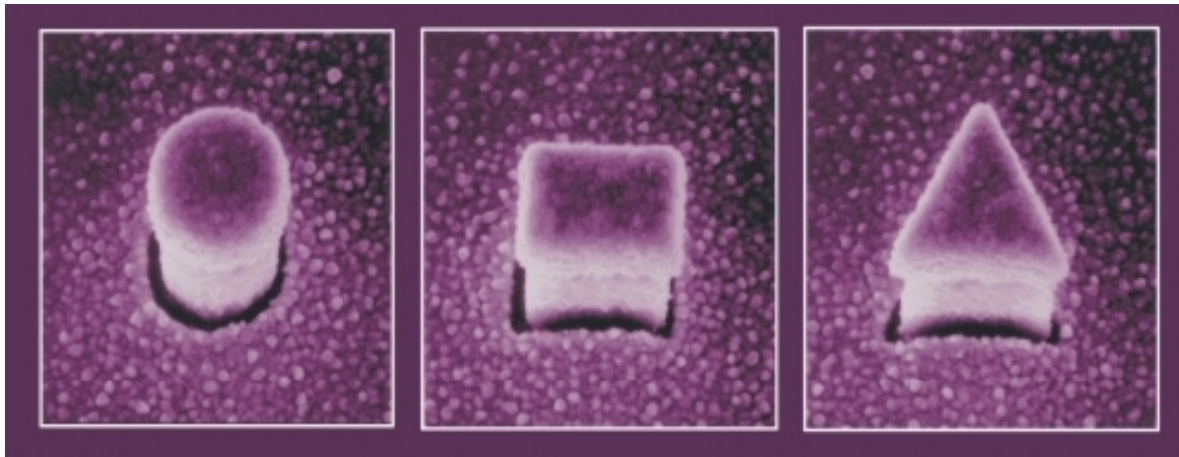


## What are their Applications?

- Neuro-quantum structures
- Single-electron devices, for instance transistors
- Tunable lasers
- Photodetectors
- Sensors
- **Quantum Computing:** Quantum Cellular Automata

# Mass production of Quantum Dots?

- Producing dots of small positional and size variability usually involves the use of **electron beam lithography**, which is similar to conventional lithography except that patterns are traced out using an electron beam rather than using a mask and light.
- Conventional lithography is not capable of creating devices at that scale since the wavelength of light used is greater than the required feature size.
- The image below shows three different quantum dot structures:



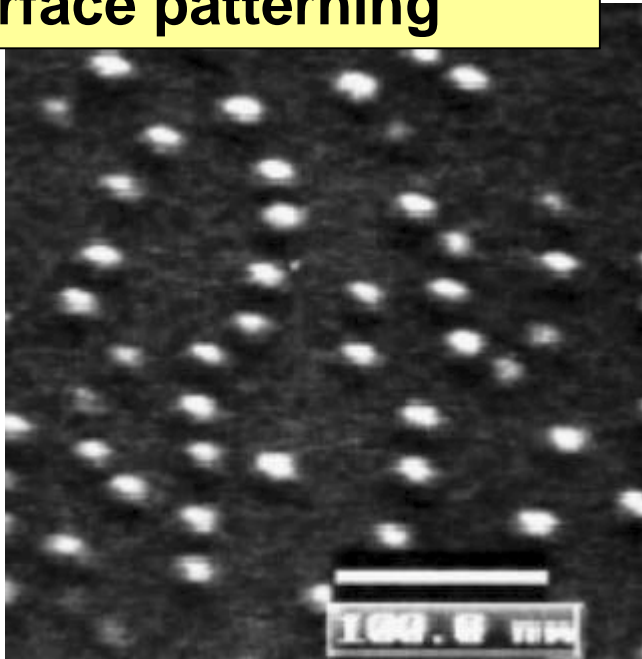
- As we can see the shape of a quantum dot is not necessarily round and varies depending on the process and application.

# mass production?

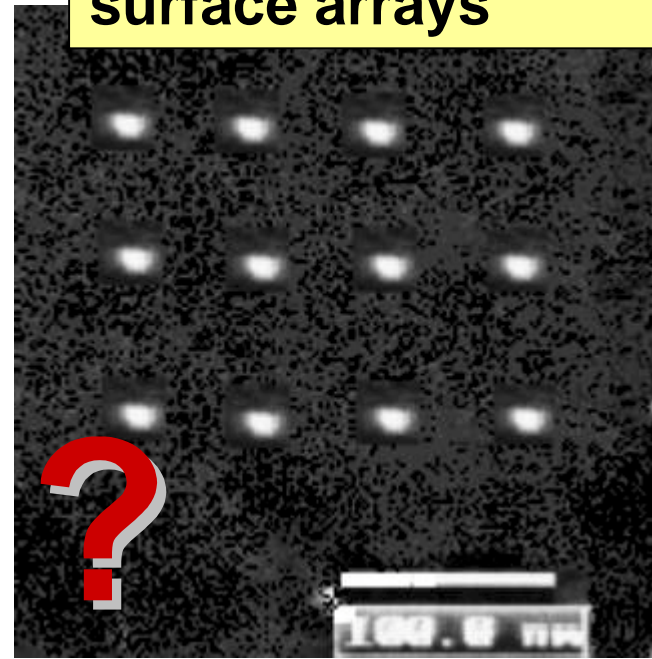
- The consistent and mass production of these devices at such scales is one of the main challenges.
- There are techniques available to produce quantum dots at extremely small scales, one of these is the self organization process.
- Self organization occurs when molecules of one crystal structure are deposited on top of another.
- The difference in lattice structure results in high stresses at the point of contact.
- As a result the deposited material tends to clump up in a manner that is analogous to depositing oil on water.
- Self organization processes can produce dots of incredibly small sizes.
- There is an important problem with trying to design with self organizing structures and that is the high variation in the final location of the resulting dots.
- Currently there is no self organizing process capable of creating quantum dots at precisely controlled locations.

# Patterning of Quantum Dots

**CURRENT:** random surface patterning

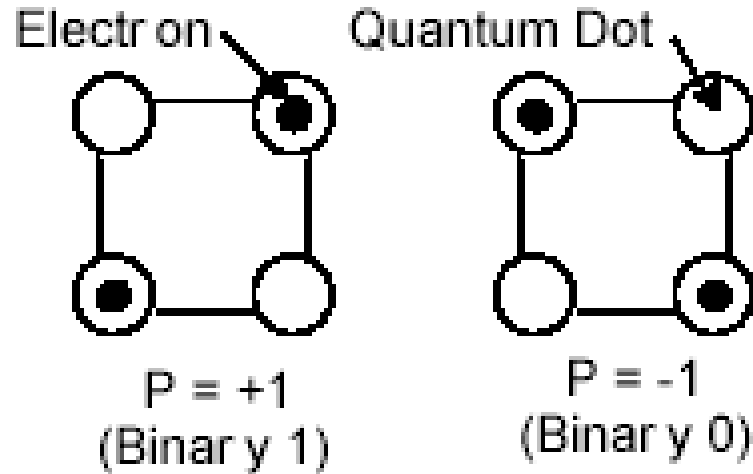


**FUTURE:** patterned surface arrays





# QCA – The Four Dot Device

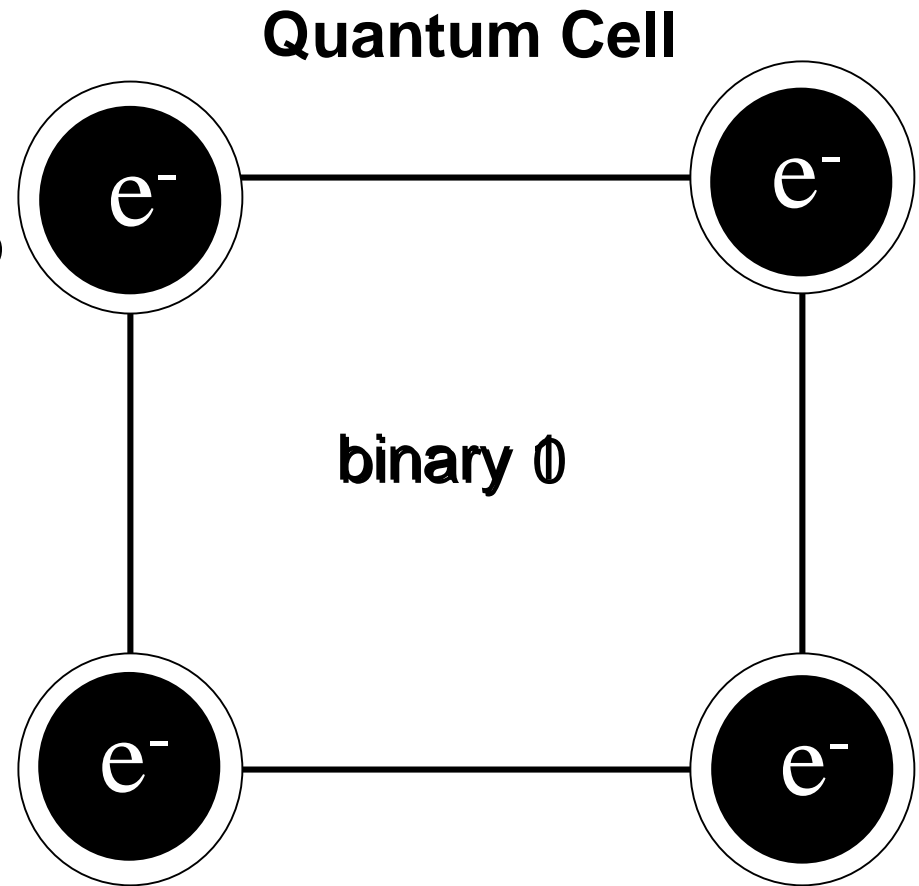


- Uses electrons in cells to **store** and **transmit** data
  - Electrons move between different positions via **electron tunneling**
- **Logic functions** performed by **Coulombic interactions**



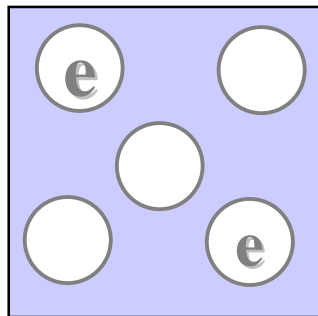
# Quantum Dots operate as Cellular Automata

- 2 **extra electrons** are introduced to the quantum cell
- Electrons have the ability to **tunnel from one quantum dot to the next**
- **Repelling force of electrons** moves the charge to **opposite corners** of the quantum cell, resulting in **two possible arrangements**, representing binary 0 and 1

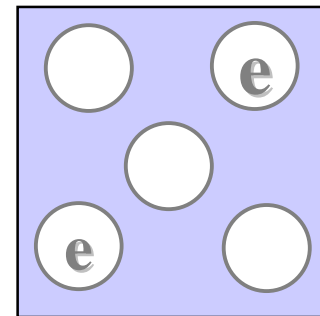


# Quantum Dot Wireless Logic: five dot model of Lent and Porod

- **Lent and Porod** of Notre Dame proposed a **wireless** two-state quantum dot device called a “cell”
  - Each cell consists of **5 quantum dots** and **two electrons**



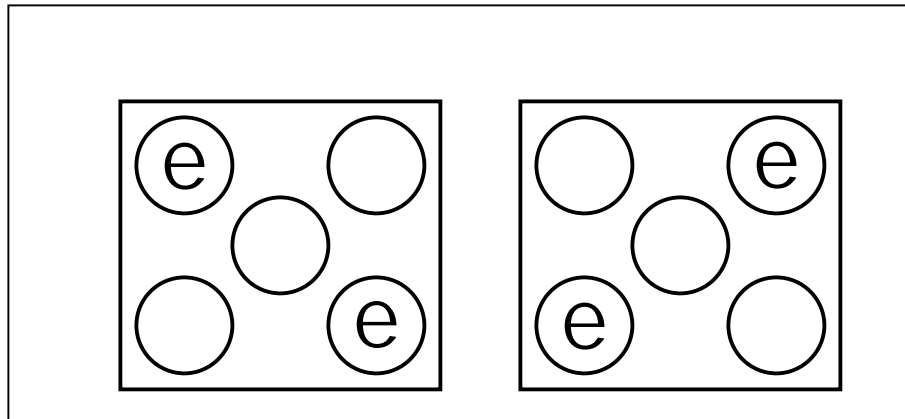
State “1”



State “0”

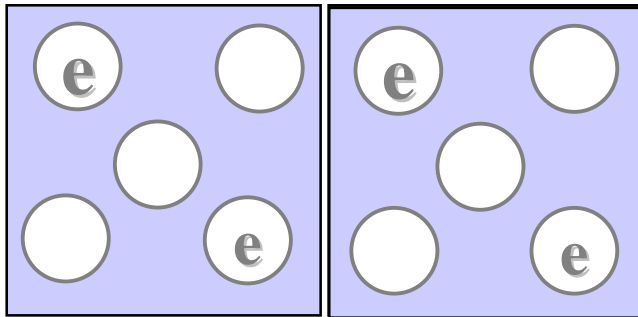
# Quantum Dots: Five dot Model

- Very similar to four-dot model
- The two electrons **repel each other**, causing them to move to opposite corners of the device
- This yields **two states** of equal energy in the cell



# Quantum Dot Wire

- By placing two “cells” adjacent to each other and *forcing the first cell into a certain state*, the second cell will assume the same state in order to lower its energy



The net effect is that a “1” has moved on to the next cell

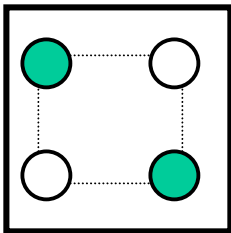
By stringing cells together in this way, a “pseudo-wire” can be made to transport a signal

In contrast to a real wire, however, no current flows

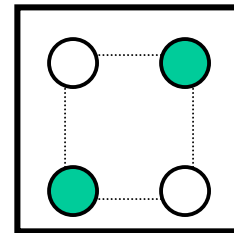
# Quantum Cellular Automata: A four-dot model

- **Basic cell:** four quantum dots connected by tunnel junctions
  - Can control voltage of tunnel junctions to freeze state of device
    - Allows clocking
- Add two excess electrons to cell to contain state
  - Repulsion between electrons will push them to opposite corners
  - One configuration indicates 0, the other 1
- Capacitively-coupled gates allow electrons to be forced into one configuration or the other
- Capacitively-coupled electrometers allow position of electrons, and thus bit state, to be **read**

0

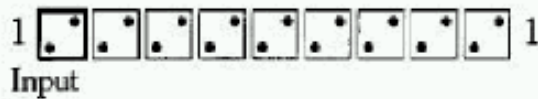


1

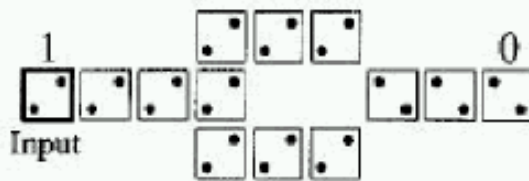


# Example of a complete geometrical-logical system for QD

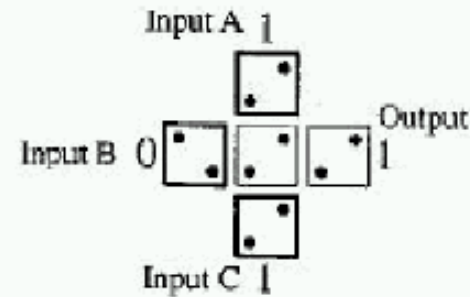
- Majority Gate can function as 2 input AND/OR



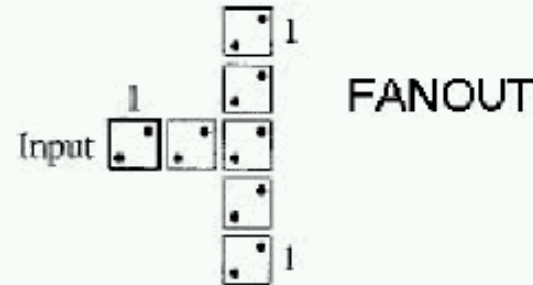
WIRE



INVERTER

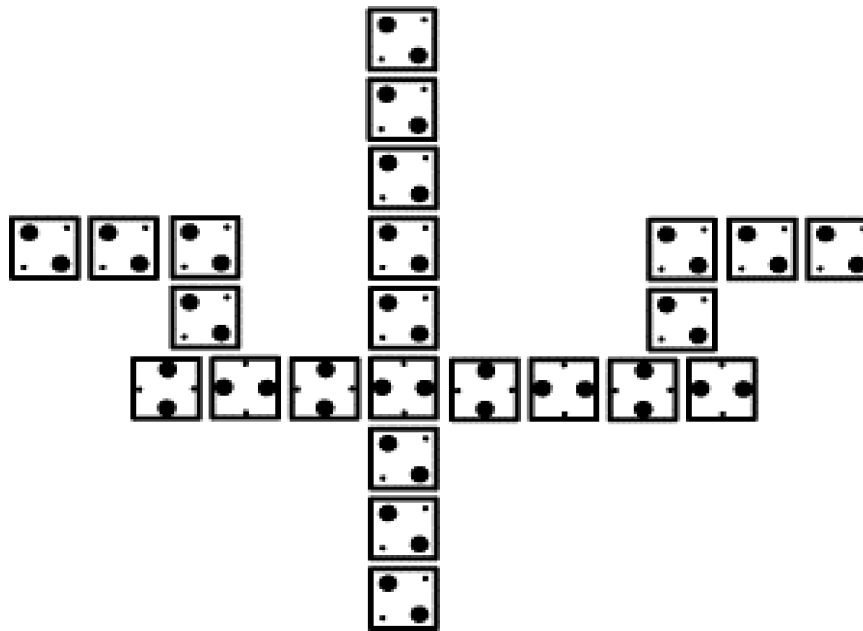


MAJORITY GATE



FANOUT

- Remember about the difficulty of equal time delays.
- Special CAD needed.

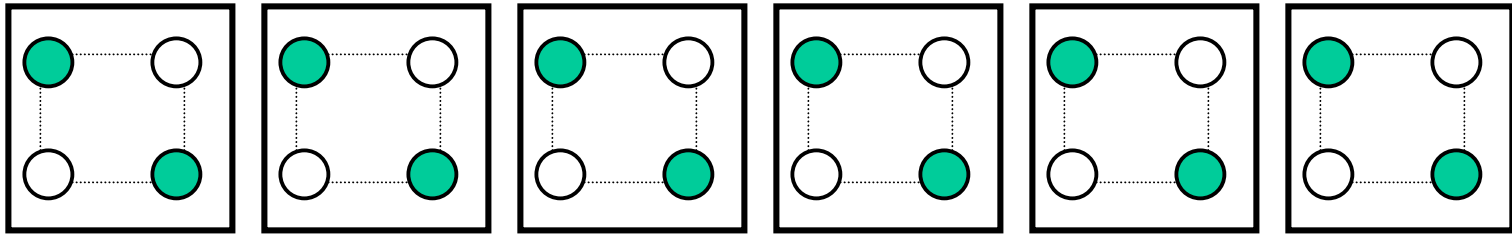


- This is a feature that is not available in conventional microelectronics.
- Actually the fact that there is no co-planer crossing in microelectronics is causing significant problems.
- Many layers of metal have to be created in order to connect the high density of devices on today's chips.
- These layers of metal interconnect cause large parasitic capacitances that slow the chip down.

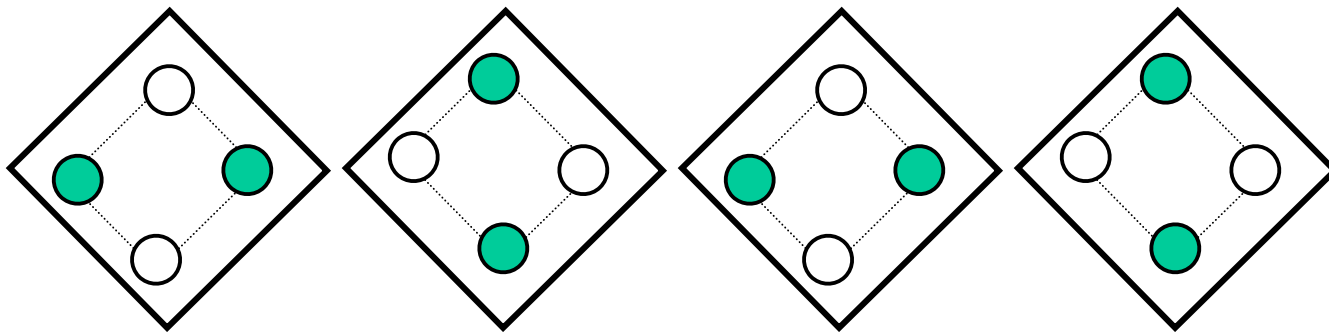


# Other QCA Structures-- Wires

- 90-degree wire



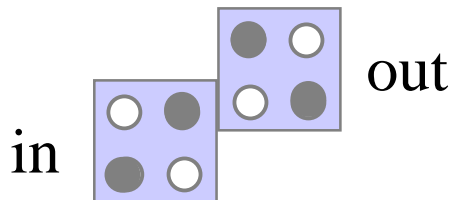
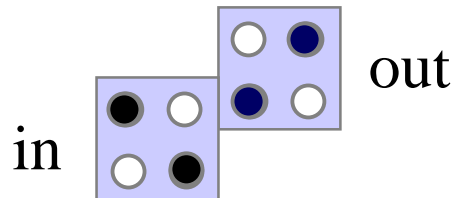
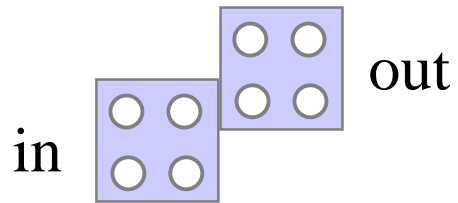
- 45-degree wire
  - Normal and inverted signal available on the same wire



Observe that in this logic  
an inverter costs nothing!

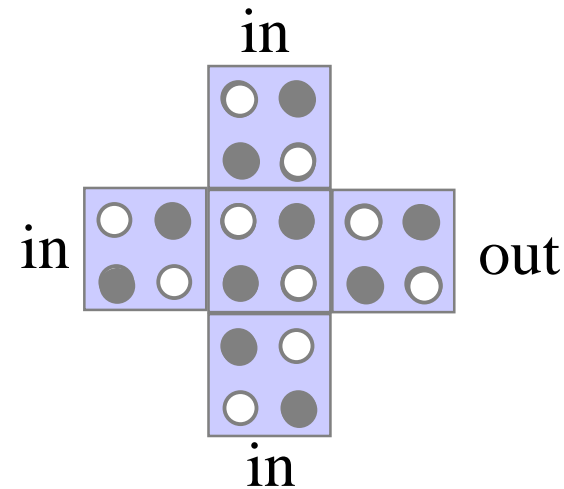
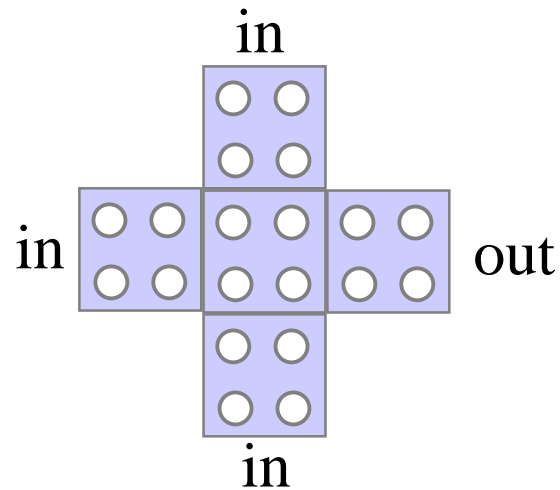
# Quantum Dot Inverter

- Two cells that are off center will invert a signal

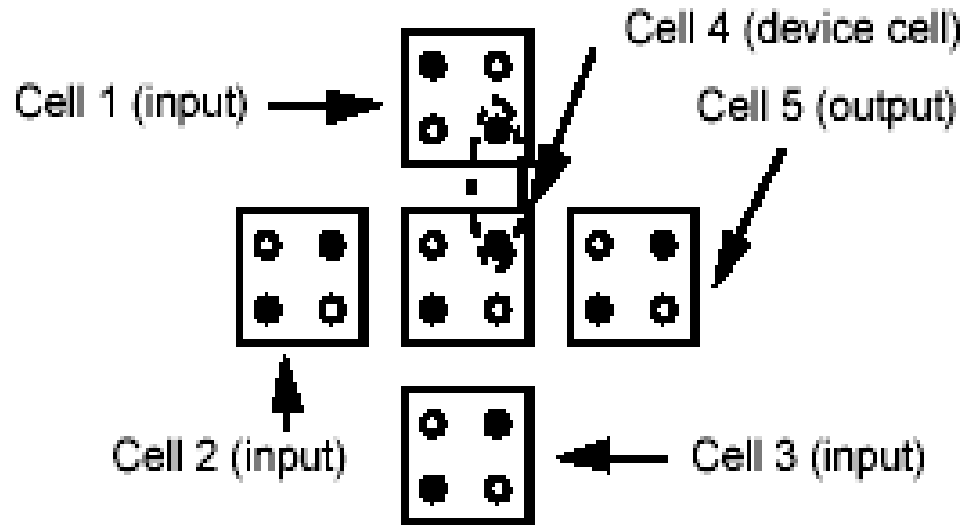


# Quantum Dot Majority Gate

- Logic gates can be constructed with quantum dot cells
  - The basic logic gate for a quantum dot cell is the majority gate

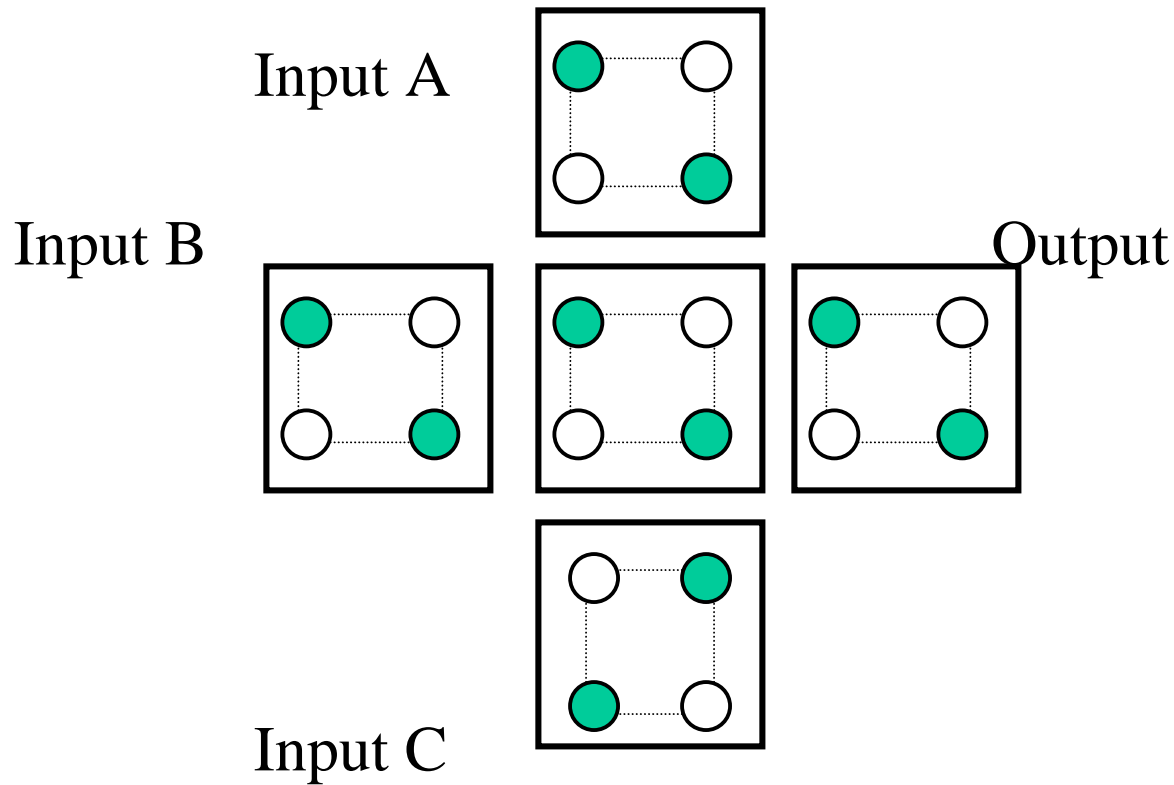


# QCA – The Circuit



- Fundamental circuit is shown above
  - This is a 90-degree wire
  - 45-degree wires can also be constructed
  - Binary value alternates between polarization +1 and -1 as it travels down the wire
  - Ripper cells can be placed to get the **actual binary value** or **complemented value** from the wire

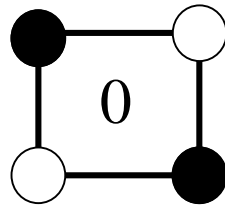
# Basic QCA Gate – Majority



- Can be used to implement AND, OR by setting one input to 0, 1

# Special cases of Majority

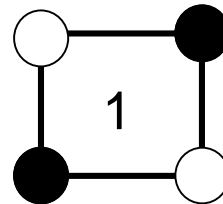
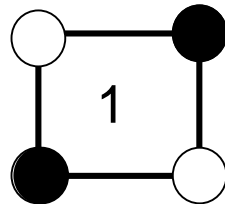
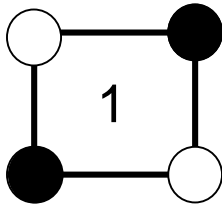
Program Line



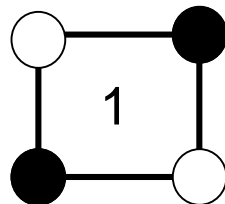
AND Gate (Program Line = 0)

A	B	OUT
1	1	1
1	0	0
0	1	0
0	0	0

Input A



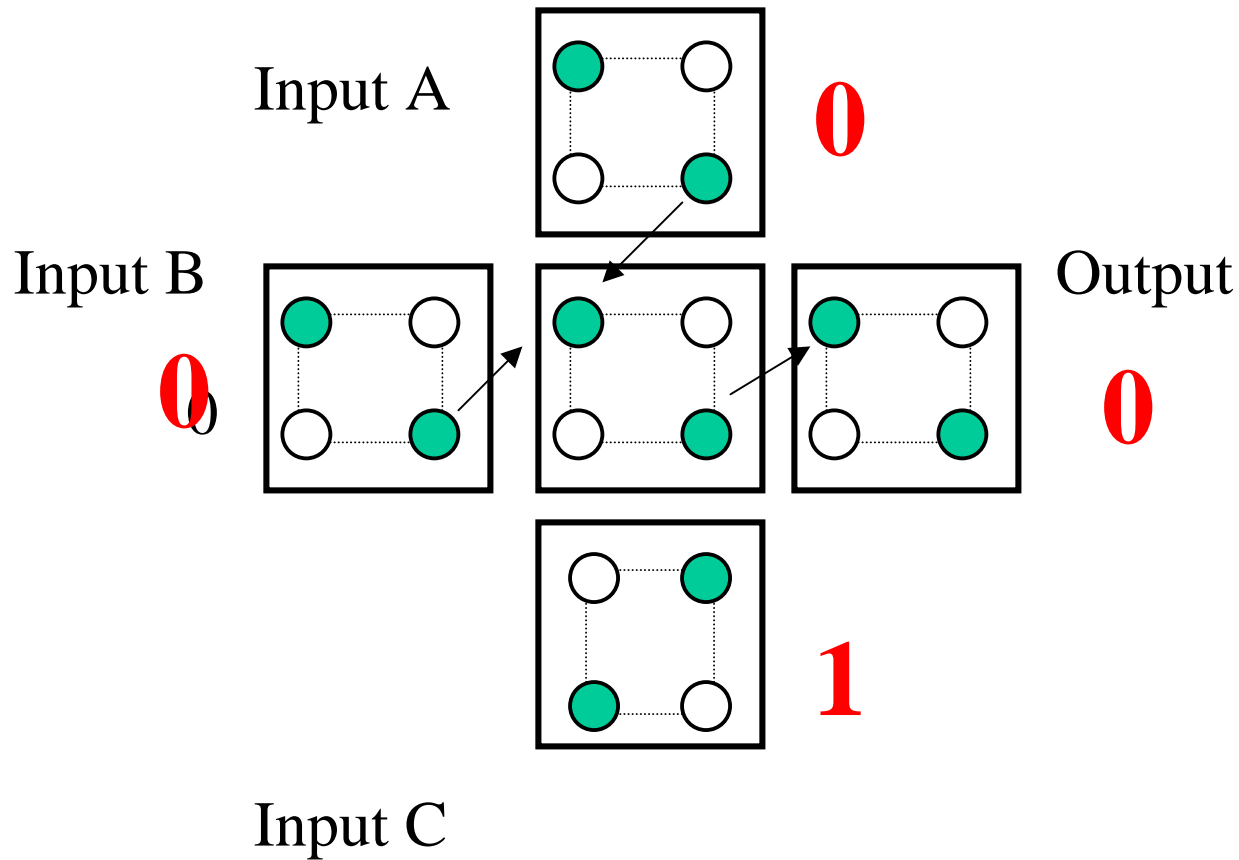
Output



Input B

\*by simply changing the program line to 1, the device is transformed to an OR gate

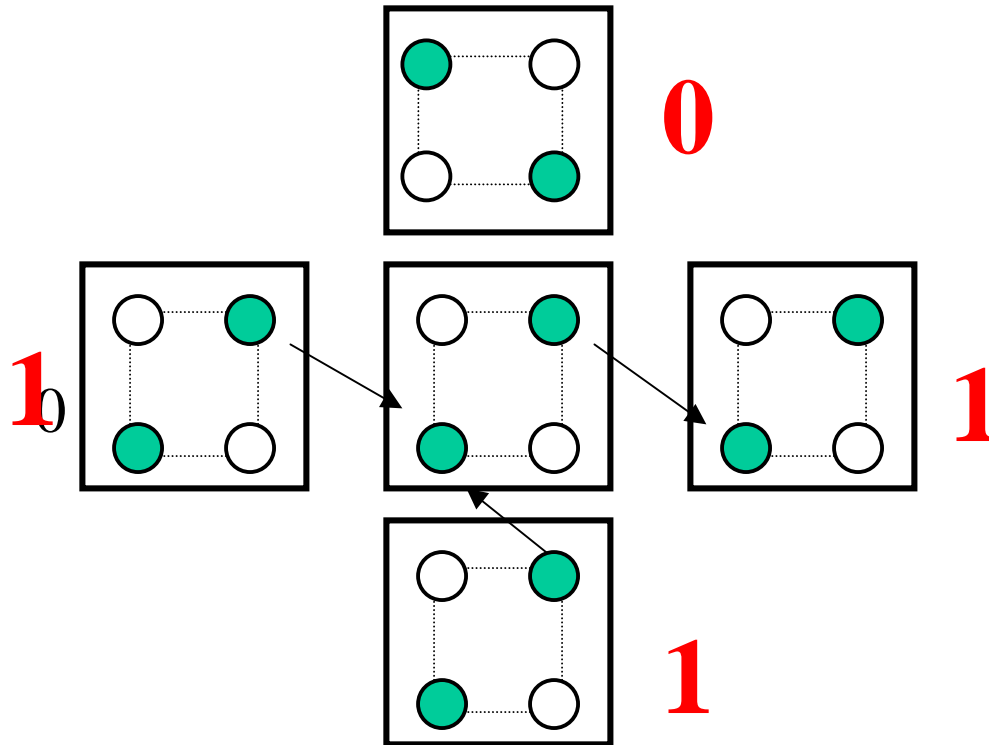
# Majority 0,0,1 $\rightarrow$ 0



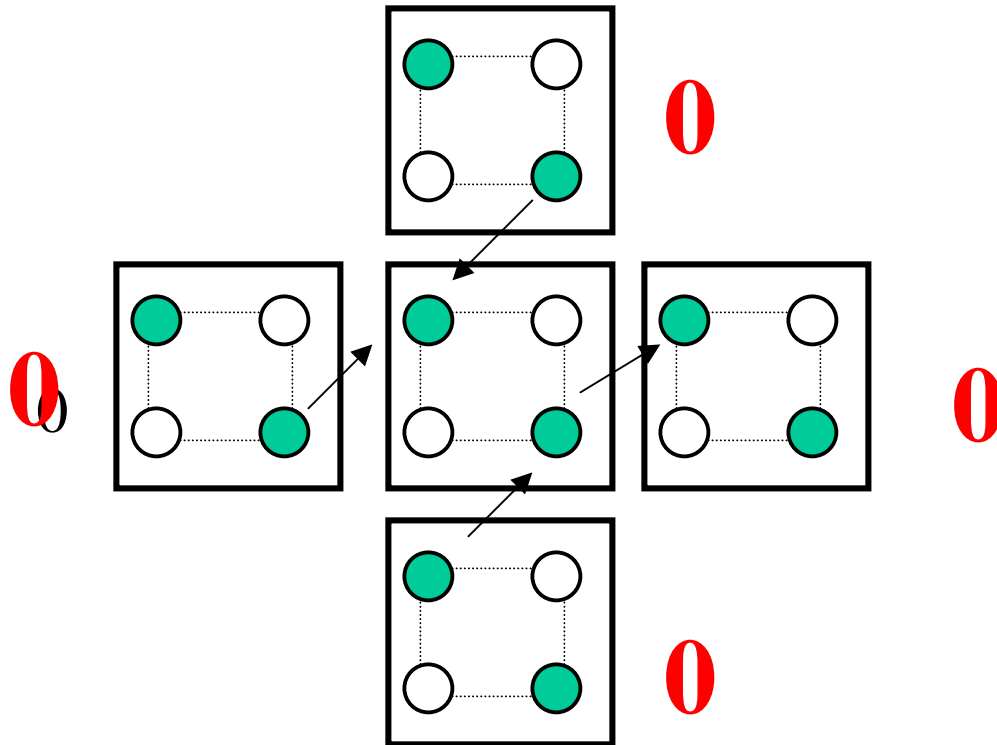
**Stronger wins!**



# Majority 0,1,1 $\rightarrow$ 1

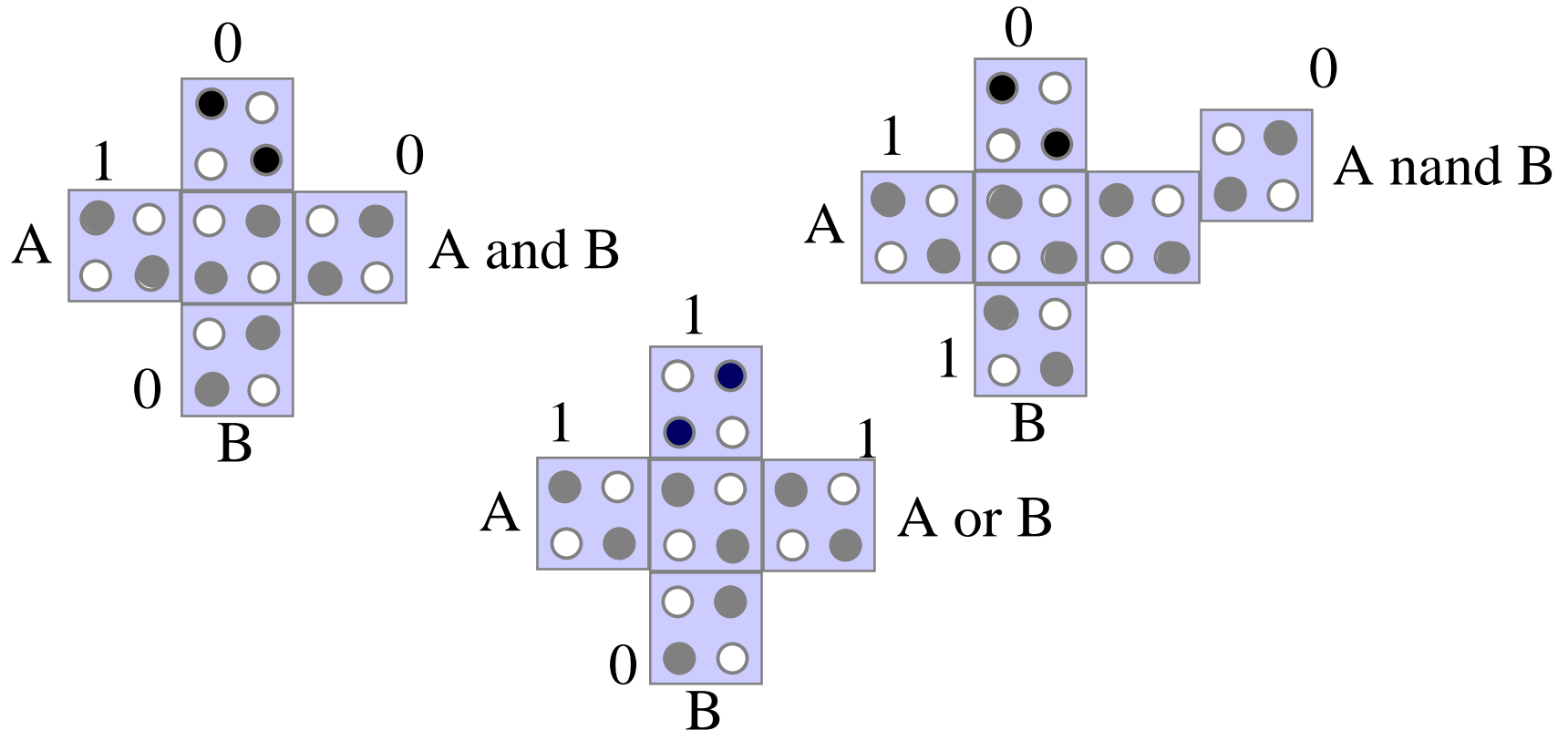


# Majority 0,0,0 $\rightarrow$ 0



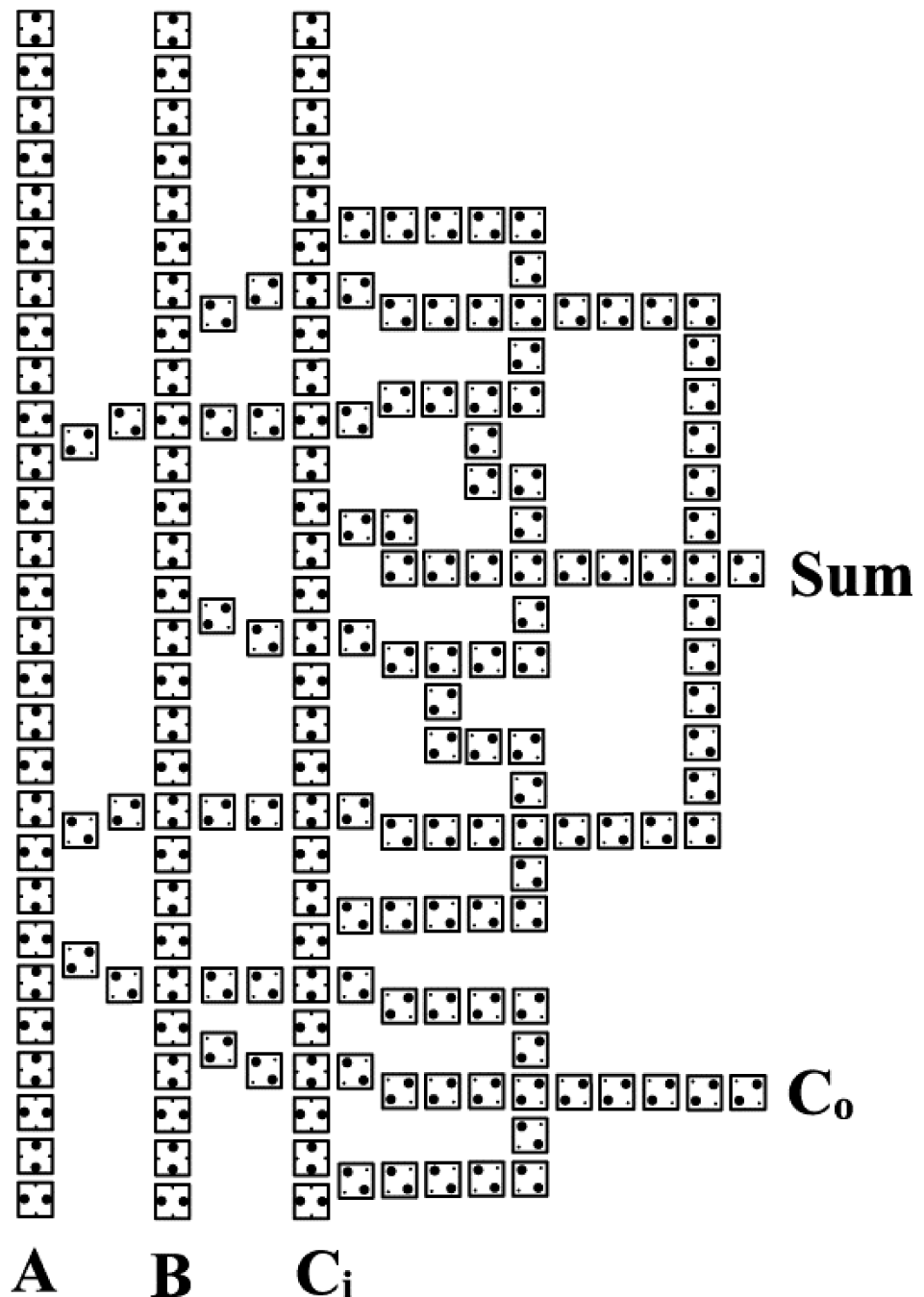
# Quantum Dot Logic Gates that use NOT

- AND, OR, NAND, etc can be formed from the NOT and the MAJ gates



# QCADesigner

- Using QCADesigner we will easily create and simulate such designs. If you have any questions please contact:  
Konrad Walus  
[walus@atips.ca](mailto:walus@atips.ca)

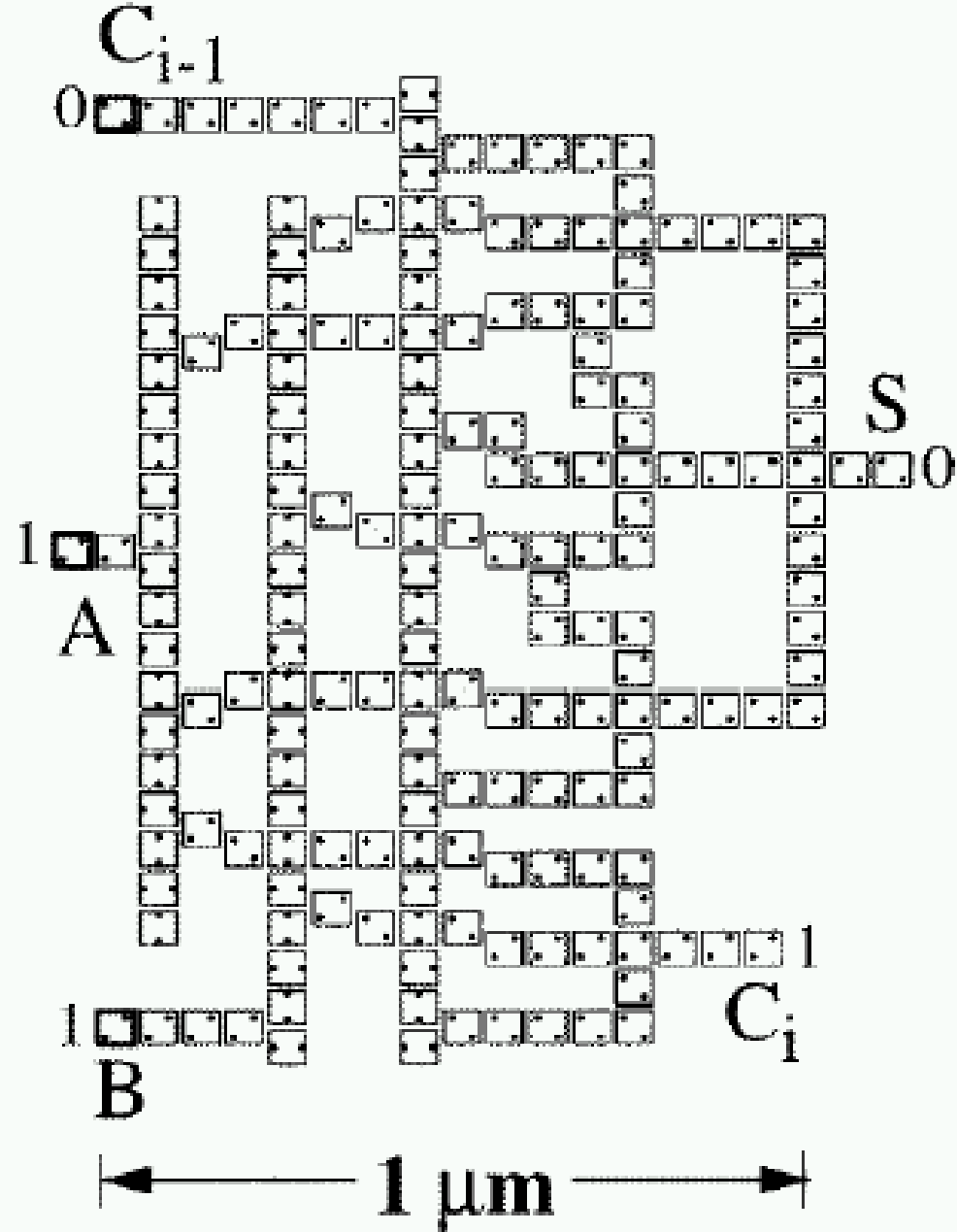


# QCA Circuits

- 1 -Bit Full Adder (Lent, et al, 1994) Bit Full Adder (Lent, et al, 1994)
- For a dot size of 10 nm, area For a dot size of 10 nm, area required is less than  $1.5 \mu\text{m}^2$  and replaces about 30 transistors
- Very Low Power
- No power is directly supplied to the interior of the array the interior of the array
- Theoretical Switching Frequency in THz range!!!

## • Possible Research Projects:

- adaptation of DDs
- adaptation of Lattices
- adaptation of PLAs
- adaptation of FPGA structures
- adaptation of Net Structures
- reversibility
- Reversible CA
- Universal CA, life, reproduction, Billiard Ball model
- pipelined, systolic, etc.
- Three - dimensional?



**A QCA 1-Bit Full Adder**