

Multi-Level Programmable Array

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□ Regular Structures

- Why? Easy to P&R(almost no need to P&R)
- Examples
 - PLA – like
 - Binary Tree base
 - Lattice Diagram
 - Better solution than UAA
 - UAA is treated as attempt to combine PLA-like and tree-like

- This Presentation is composed as following
 - Intro to Lattice Diagram
 - MOPS for multiple-out Lattice Diagram
 - Generalized architecture for MOPS

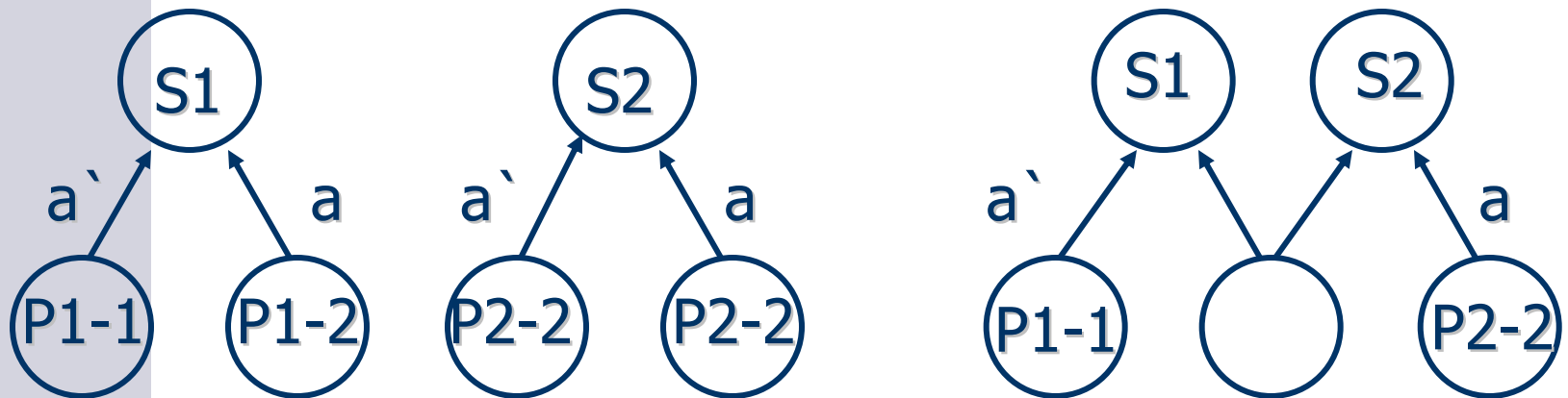
1. Intro to Lattice Diagram

□ Characteristics

- Like Tree and similar to BDD.
- BDD has combined predecessors if and only if predecessors in the same level is equal.
- But Lattice Diagram has always combine neighbor predecessors by some Rule. It occurs repetition of control variables.
- Although BDD grows horizontally, Lattice grows vertically by the repetition of variables...
- BDD and Lattice Diagram is made of MUX.

1. Intro to Lattice Diagram

- Combining Rule
 - Basic rule is the combining of two predecessors by XOR



$(a \text{ AND } P1-2) \text{ XOR } (a' \text{ AND } P2-1)$

- More rule and method are introduced in "LATTICE DIAGRAMS USING REED-MULLER LOGIC" by Perkowski

2. MOPS for multiple-out Lattice

- Some problems in Lattice Diagram
 - Repetition of control variable
 - It increases vertical depth.
 - This problem controlled by variable ordering.
 - In the case of multi-output func
 - Ordering is not easy to be performed
 - There is quite waste for one block
 - And Partitions generate big empty subareas
 - Not good method, it leads to horizontal growth.

2. MOPS for multiple-out Lattice

□ Functional Decomposition

- Basic conception is to divide function to sub-functions
- There are some decomposition methods
 - AND Decomposition, OR \sim , Decomposition with Mux
- Multi-output func can be decomposed by symmetric func
 - Multi-output func can be composed of Boolean operation(AND, OR, EXOR) of symmetric funcs.
 - Because of no repetition of variable in symmetric func, this method is very nice to reduce vertical depth.

2. MOPS for multiple-out Lattice

□ What is symmetric func?

- All minterms that have same number of ones in their binary number have same value(zero, or one).
- Eg

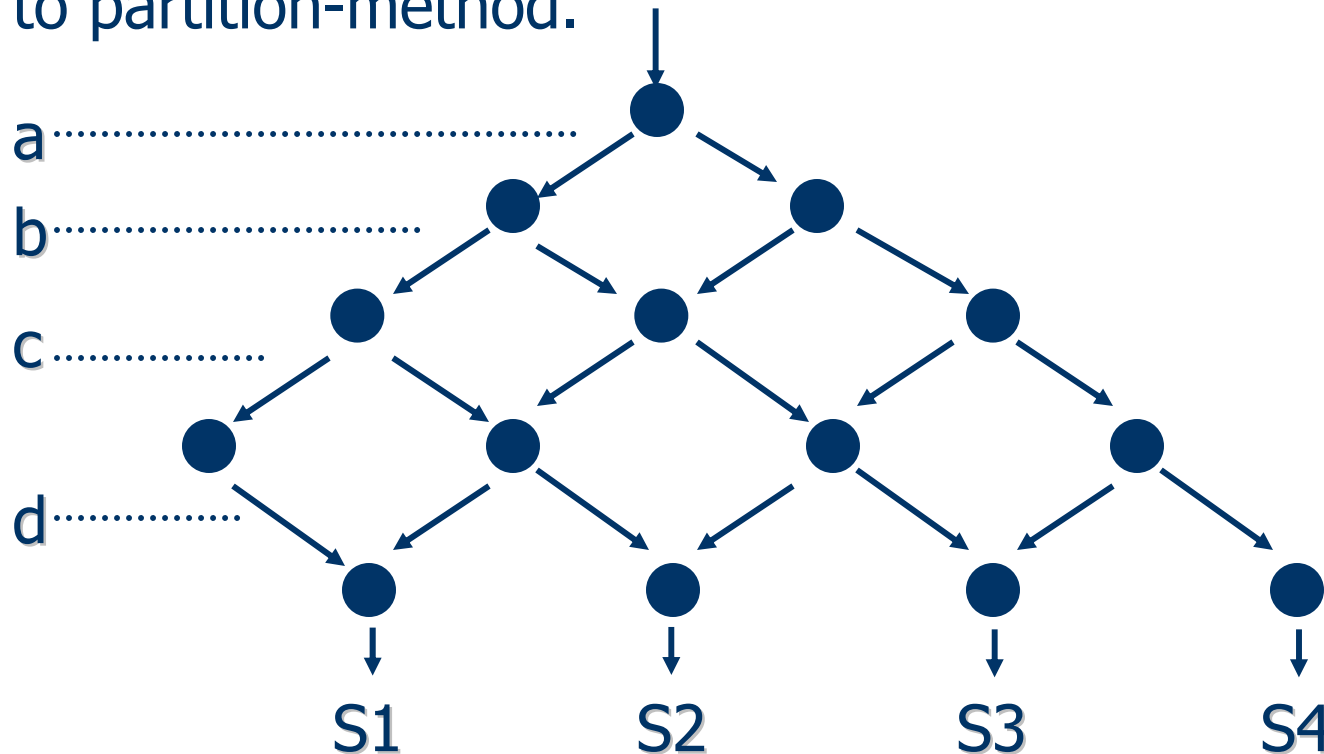
$F(a,b,c,d)$
 : It polarity 1111
 = $S_{3,4}$

		c,d			
		00	01	11	10
a,b	00	0	0	0	0
	01	0	0	1	0
	11	0	1	1	1
	10	0	0	1	0

2. MOPS for multiple-out Lattice

□ MOPS for 4-variables

- MOPS is one diagram but it can express all symmetric func which has same polarity
 - So that reason, it reduces horizontal width compare to partition-method.

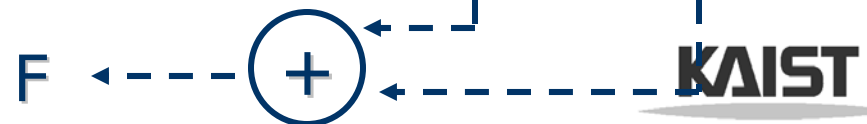
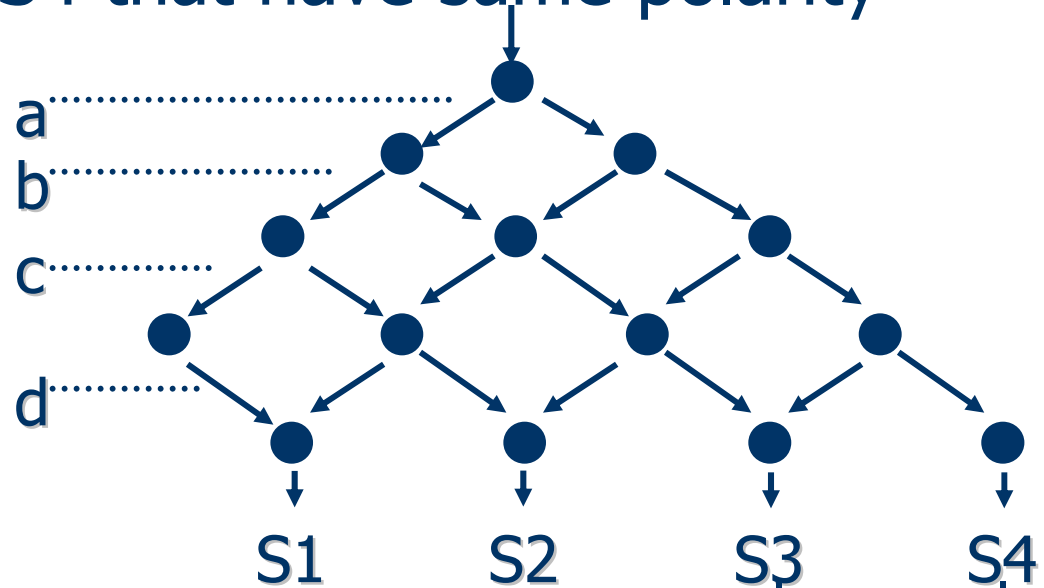


2. MOPS for Multiple-out Lattice

□ Examples of using MOPS

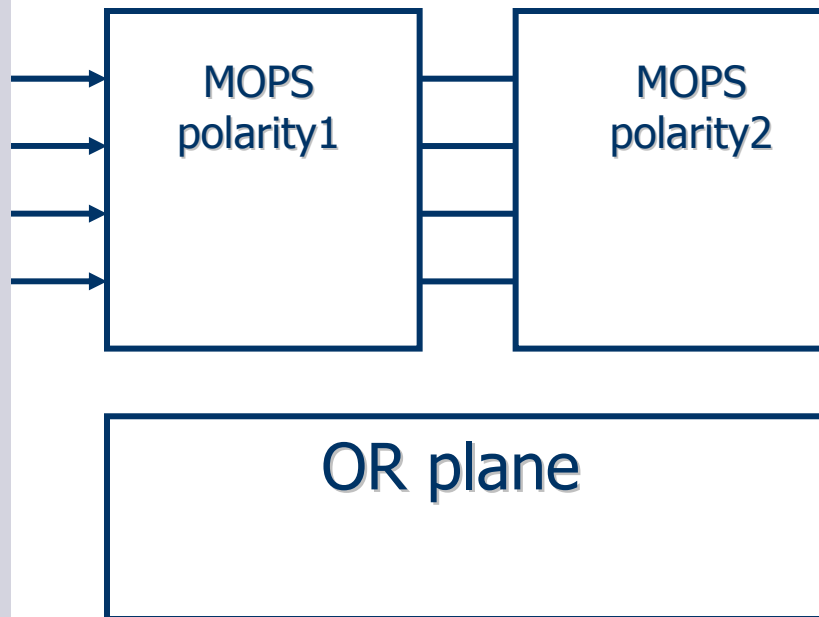
- $F = (\sim b \text{ XOR } \sim d) \text{ OR } (a \text{ XOR } c) \text{ OR } (abcd)$
 → It is decomposed to two symmetric functions S3, S4 that have same polarity

		c,d			
		00	01	11	10
a,b	00	0	0	0	0
	01	0	0	1	0
	11	0	1	1	1
	10	0	0	1	0



3. Generalized architecture for MOPS

- Every multi-output Boolean func can be decomposed to vector-OR of symmetric func of variable polarity
 - Each MOPS has same control variable but different polarity
 - Outputs of two MOPSes are combined in OR plane



3. Generalized architecture for MOPS

- Every multi-output func with subset SV_i , $i= 1\sim k$ of mutual symmetric variables can be decompsed to serial composition of K MOPS arrays followed by AND/OR plane.
 - $F(SV) = f_1(SV_1) \text{ OR } f_2(SV_2) \dots \text{ OR } f_k(SV_k)$
 - Each $f_i(SV_i)$ is symmetric , it can be expressed by one MOPS

