

### LAYOUTDRIVEN SYNTHESIS FOR SUBMICRON TECHNOLOGY MAPPING EXPANSIONS TO REGULAR LATTICES

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## □ A basic concept in VLSI layout

Applications to submicron design, quantum devices, and designing new fine-grain FPGAs
 In a regular arrangement of cells, every cell is connected to 4, 6, 8 neighbors and to vertical, horizontal and diagonal buses.





Expansions of functions

# Operators that transform a function to a few simpler functions

### □ Two types

- 1<sup>st</sup> category
  - canonical (such as Shannon)
  - noncanonical(such as Sum-of-Product)
- 2<sup>nd</sup> category
  - Maximum-type
  - Linearly-Independent type





Three components of lattice diagrams

- Expansion of a node function, which creates several successor nodes of this node.
- Joining operation joins several nodes of a bottom of the lattice.
- Regular geometry to which the nodes are mapped, this geometry guides which nodes of the level are to be joined.















- planar & based on a rectangular grid
  Each cell has two inputs and two outputs.
  For a 4-neighbor lattice geometry , any canonical form of Reed-Muller logic and its Linearly Independent generalizations can be realized.
- Any MV logic can be also realized in the 4neighbor lattice.















(d)



Layout Geometries–6 neighbors

- The rectangular grid is enhanced with one diagonal connection, thus every cell has three inputs and three outputs.
- This can realize the generalized ternary diagrams.















Layout Geometries-8 neighbors

The rectangular grid is enhanced with two diagonal connection, thus every cell has four inputs and four outputs.

This can realize the generalized quaternary diagrams.





Linearly Independent type

- Generalizations of Positive Davio and Negative Davio expansions.
- For arbitrary algebras they should have at least one linear group operation.
- Usually based on the algebraic structure of an arbitrary field.
- □ They include
  - S(Shannon expansion)
  - Positive and Negative Davio pD and nD respectively
  - general Linearly Independent(binary and MV)
  - EXOR Ternary expansions





Maximum-type

## □ Assumption : each binary function(f)

- f is represented by a pair [ON(f),OFF(f)]
- fa = [ON(f),OFF(f)]
- Shannon





- Prior figure explains the principle of creating a Shannon Lattice based on ordered Shannon expansions for f, g.
- A standard cofactor fx where x is a variable does not depend on this variable.
- This cofactor is vacuous cofactor(denoted by v-cofactor) though fx is still a function of all variables including x, but as a result of cofactoring the variable x becomes vacuous.





 $\Box$  For any two disjoint products  $a_1$  and  $a_2$ . the v-cofactors fa1 and ga2 are disjoint. Therefore functions fa1 and ga2 are in an incomplete tautology relation, and functions f and g are not changed when fa1 and ga2 are joined (OR-ed) to create a new function  $f_{a_1} + g_{a_2}$ , as in prior figure(where  $a_1 = a_2 = a_1$ ) This way the entire lattice is created levelby-level.





Design Methodology

- One level of function is expanded to an assumed type of a decision tree(Shannon, SOP, etc).
- □ The level of the tree is mapped to the assumed type of Lattice.
- This means joining together some nodes of the treelike lower part of the lattice.
- The procedure requires repeating some variables in the lattice.

