CSCE790 Topics in Information Technology

Computational Models (Lecture 5)

Department of Computer Science & Engineering University of South Carolina Spring, 2002

Review

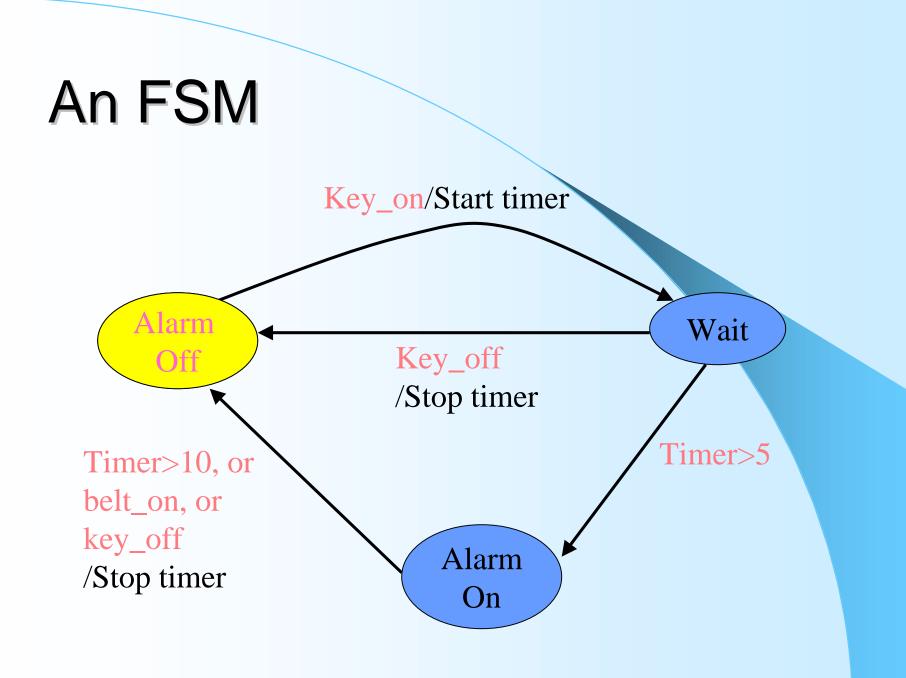
- Data Flow Graph
 - data dependency
- Control/Data Flow Graph
 - control dependency
- How about a reactive system?

Finite State Machine

• What ?

If the driver turns on the key, and does not fasten the seat belt within 5 seconds then

an alarm beeps for 5 seconds, or until the driver fastens the seat belt, or until the driver turns off the key



An FSM (Cont'd)

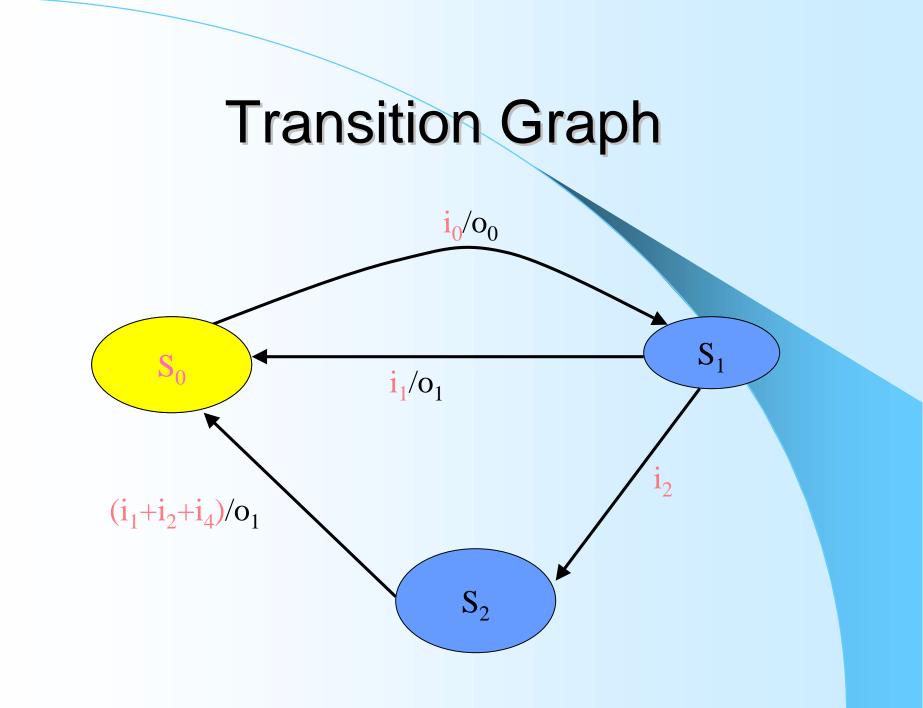
- States
 - Alarm off, Alarm on, Wait
- Initial State
 - Alarm off
- Inputs
 - Turn on/off the key, fasten the seat belt, timer reads
- Outputs
 - Start/stop the timer
- Start transitions
 - Alarm off + Turn on the key \rightarrow Wait
- Output
 - Alarm off + Turn on the key → start the timer

Finite State Machine

- FSM = (S, I, O, s_0, δ, λ)
 - **S** = { $s_0, s_1, ..., s_k$ }
 - **I** = { $i_1, i_2, ..., i_m$ }
 - $\mathbf{O} = \{\mathbf{o}_1, \mathbf{o}_2, \dots, \mathbf{o}_n\}$
 - δ : S x I \rightarrow S (Transition function)
 - $-\lambda: S \times I \rightarrow O \text{ (Output function)}$
- Given an input sequence, an output sequence is produced which is depended on s_0, δ , and λ .

Representation

- Given
 - States
 - Alarm off (s₀), Alarm on (s₁), Wait (s₂)
 - Initial State
 - Alarm off (s₀)
 - Inputs
 - Turn on/off the key (i_0/i_1) , fasten the seat belt (i_2) , timer > 5 (i_3) , time > 10 (i_4)
 - Outputs
 - Start/stop the timer (0₀/0₁)

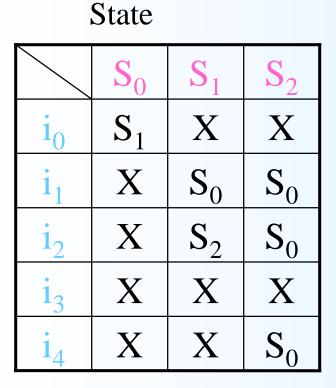


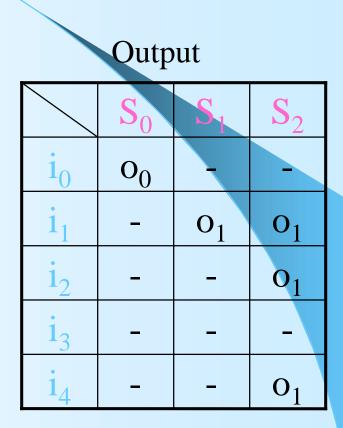
Transition Function

- Transition Function s1 = s0 * i0 s0=s1*i1 s2=s1 * i3 s0=s2*(i1+i2+i4)
- Output Function

$$O_0 = s_0 * i_0$$
 $O_1 = s_1 * i_1$
 $O_1 = s_2 * (i_1 + i_2 + i_4)$

Transition Table

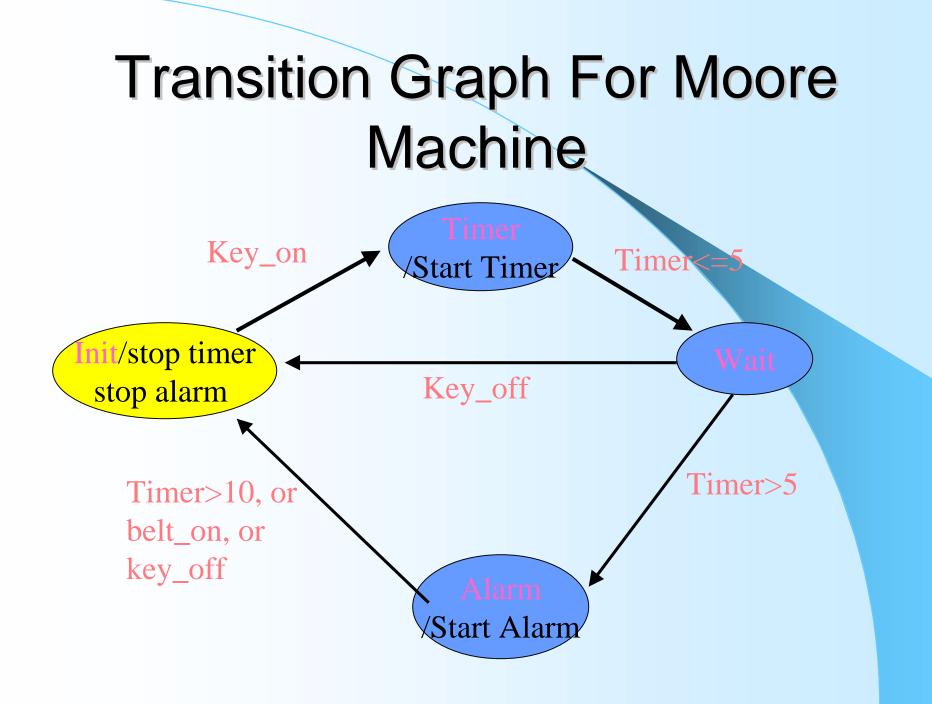




X: don't care

Mealy Machine and Moore Machine

- Mealy Machine
 - The output is a function of both the current state and the input
- Moore Machine
 - The output is only a function of the current state



Mealy/Moore Machine

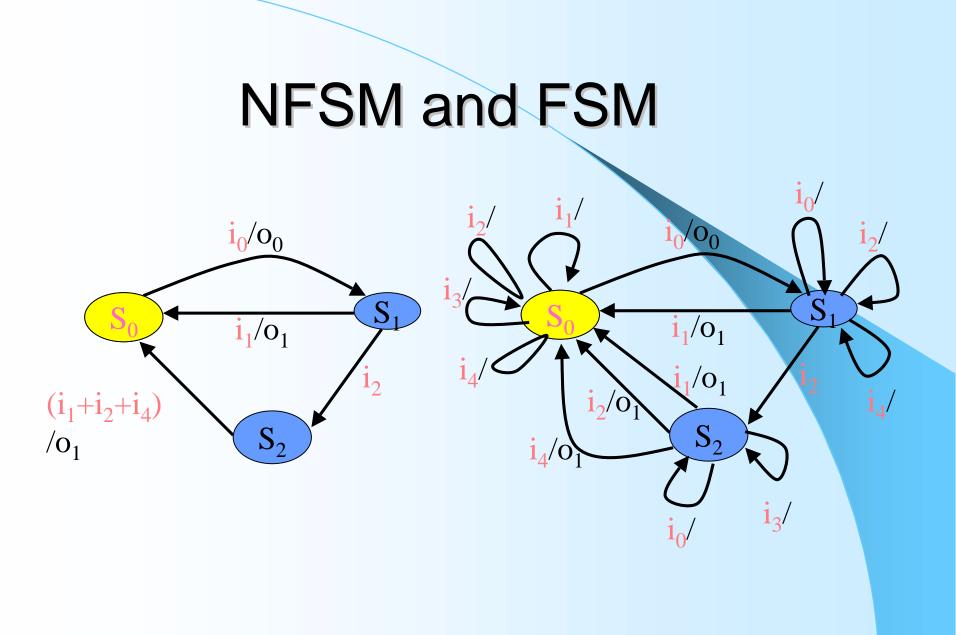
- An FSM can be realized either by Mealy or Moore machine
- Mealy machine may use less flip-flops and output signals are immediately after the transition
- Moore machine may use more flip-flops and output signals valid except during the transition

Nondeterministic FSM

- Deterministic FSM
 - Given a state and input, there is exactly one next state
- Nondeterministic FSM (NFSM)
 - Given a state and input, there maybe more than one next state, or a state can transform from one state to anther without any input, or for some given input there no next state at all
- For any NFSM, there is always one equivalent FSM

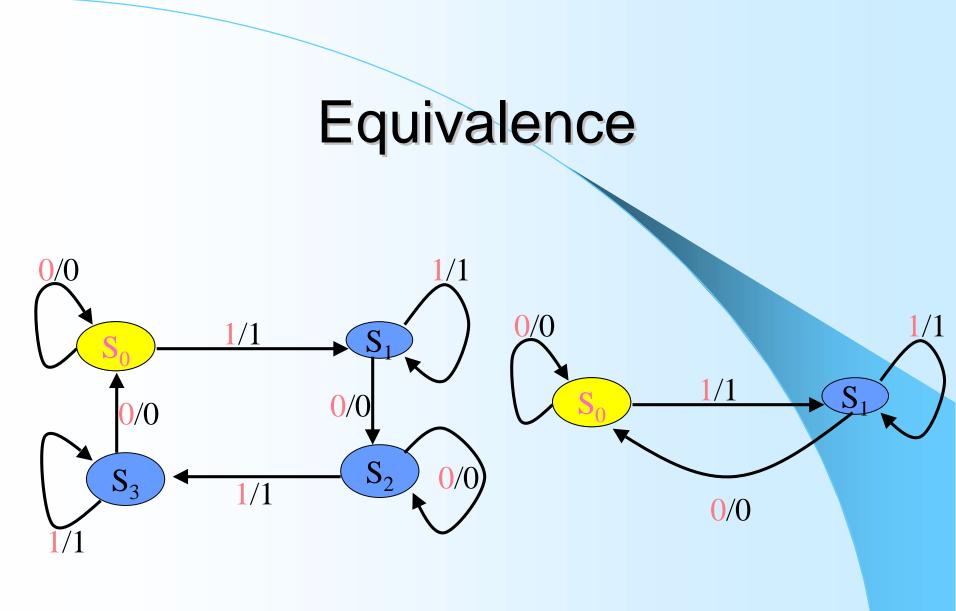
Nondeterministic FSM

- For unknown/unspecified behavior
- Less states, more compact
- Useful for
 - Optimization
 - Verification
- Can be refined
- For any NFSM, there is always one equivalent DFSM



Equivalence

• Two FSMs are equivalent iff for any given input sequence, identical output sequences are produced



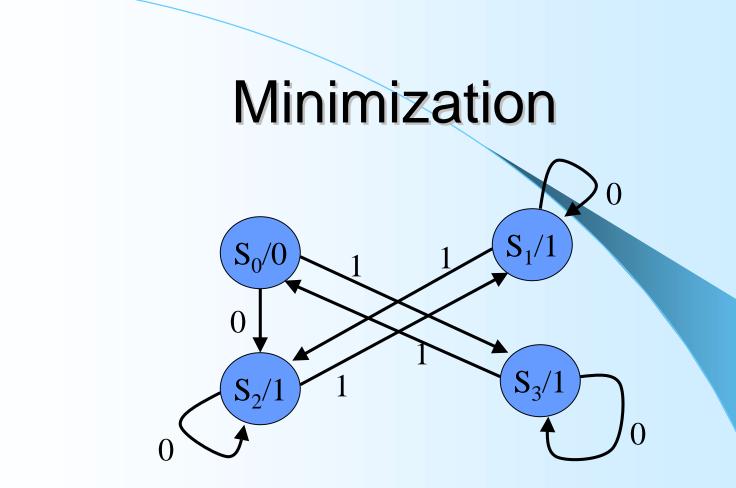
Minimization

- What
 - Given an FSM, find the equivalent FSM with a minimum number of states
 - Two states s1 and s2 in an FSM are equivalent iff each input sequence beginning from s1 yields an output sequence identical to that obtained by starting from s2

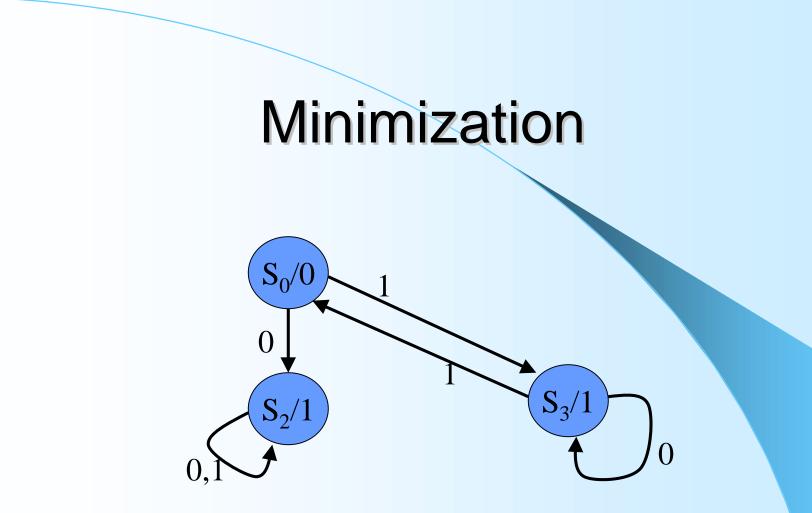


Minimization(Moore Machine)

For each pair of the states (si,sj) If si and sj have different output Mark si and si as not equivalent End for Do for each unmarked pair for each input, si and sj are transferred to states which are not equivalent Mark si and sj as not equivalent end for end for until no mark is possible Unmarked pairs are equivalent



(s0, s1)(s0, s2)(s0, s3) (s1, s2)(s1, s3) (s2, s3)



(s0, s1)(s0, s2)(s0, s3) (s1, s2)(s1, s3) (s2, s3)