

Application Considerations for the DHP Methodology

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SESSION on “Intelligent” Control

Generally, the human designer of the control system has lots of work to do before turning (remainder of) the design task over to our “intelligent” (aka: Neural Networks?) controller.

We here **ASSUME** that many design decisions have already been made:

e.g.

- need for reinforcement learning approach (due to absence of certain otherwise needed information)
- representation of plant (state?) variables/ measurables
- criterion function (re. “desired” qualities)
- basic architecture of controller neural network

Context (re. Reinforcement Learning):

Adaptive Critic Design (ACD)

A methodology for adaptively designing an (approximately) optimal controller for a given plant according to a stated criterion.

We use a NN as the controller [actionNN], and another NN [criticNN] to update (assist in the design of) the controller.

“Plant” is represented via state vector $R(t)$.

Context:

The ACD method entails the user defining a (primary) utility function $U(t)$ for the specific application, and then maximizing a new utility function (Bellman Eqn.):

$$J(t) = \sum_{k=0}^{\infty} \gamma^k U(t+k)$$

[We note: $J(t) = U(t) + \gamma J(t+1)$

Context: Family of Adaptive Critic Designs

The criticNN approximates either $J(t)$ or gradient of $J(t)$ wrt state vector $R(t)$ [$\nabla J(R)$]

❖ Heuristic Dynamic Programming (HDP)

CriticNN approximates $J(t)$

❖ Dual Heuristic Programming (DHP)

CriticNN approximates $\nabla J(R) \equiv \lambda$

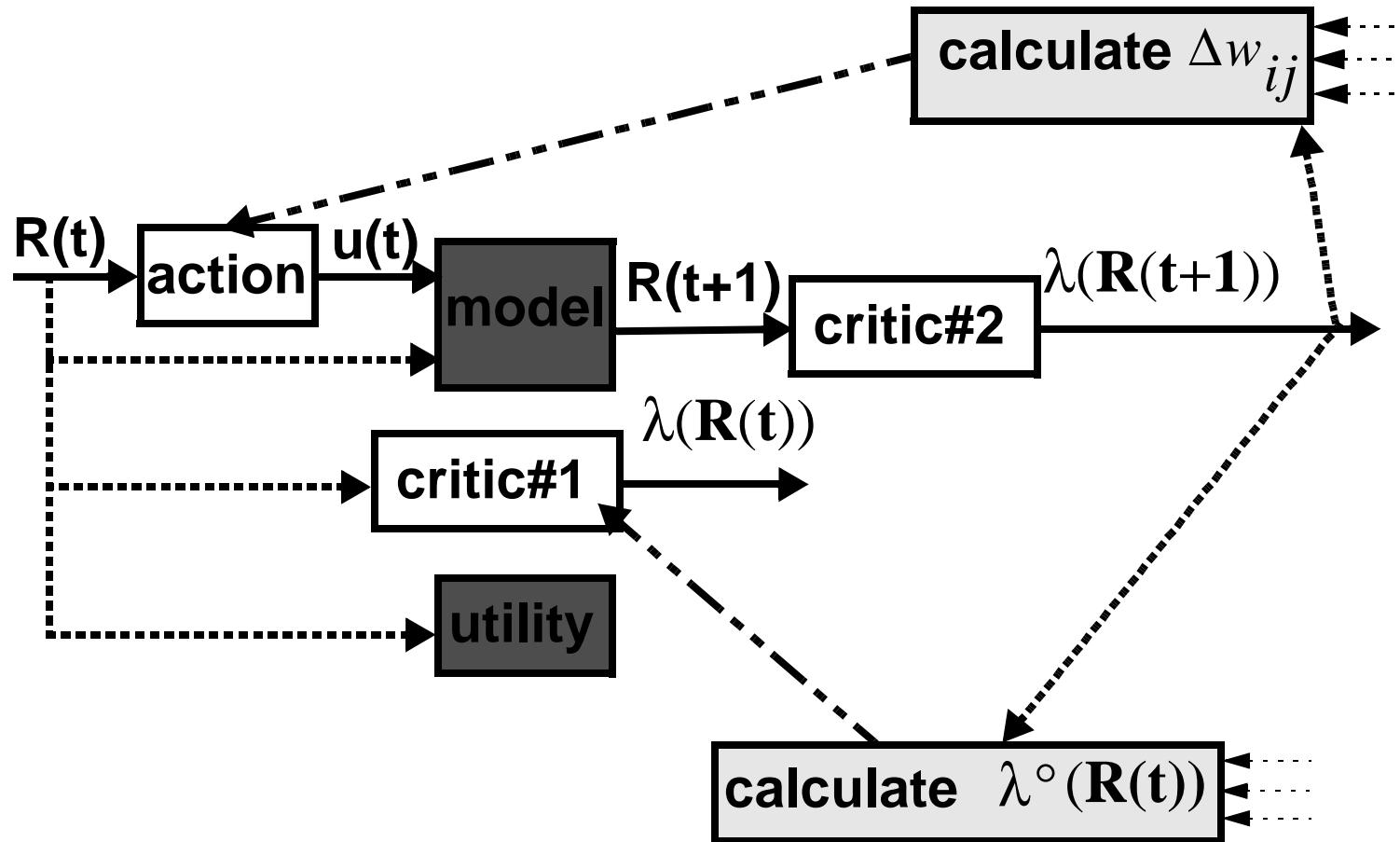
❖ Generalized Dual Heuristic Programming (GDHP)

CriticNN approximates $J(t)$ and $\nabla J(R)$

❖ Action Dependent

CriticNN also inputs $u(t)$ and outputs $\nabla J(u)$

Computing Schema for discussing Strategies



Weights in actionNN are updated with objective of maximizing $J(t)$:

$$\Delta w_{ij}(t) = lcoef \bullet \frac{\partial}{\partial w_{ij}(t)} J(t)$$

where $\frac{\partial}{\partial w_{ij}(t)} J(t) = \sum_{k=1}^a \frac{\partial}{\partial u_k(t)} J(t) \bullet \frac{\partial}{\partial w_{ij}(t)} u_k(t)$

and $\frac{\partial}{\partial u_k(t)} J(t) = \frac{\partial}{\partial u_k(t)} U(t) + \frac{\partial}{\partial u_k(t)} J(t+1)$

and

$$\frac{\partial}{\partial u_k(t)} J(t+1) = \sum_{s=1}^n \frac{\partial}{\partial R_s(t+1)} J(t+1) \bullet \frac{\partial}{\partial u_k(t)} R_s(t+1)$$

call this term $\lambda(t+1)$ (to be output of critic)

CriticNN output is λ .

**For training criticNN, “desired output” is λ° .
(cf. Eqn. (6) in paper)**

Paraphrase of Eqn. (6) [cf. Eqn. (7) in paper]:

$$\begin{aligned}\lambda_s^\circ(t) &= [\sim\text{Utility}] + \sum_{j=1}^a ([\sim\text{Utility}] \bullet [\sim\text{Action}]) \\ &\quad + \sum_{k=1}^n ([\sim\text{Critic}(t+1)] \bullet [\sim\text{Plant}]) \\ &\quad + \sum_{k=1}^n \left\{ \sum_{j=1}^a ([\sim\text{Critic}(t+1)] \bullet [\sim\text{Plant}] \bullet [\sim\text{Action}]) \right\}\end{aligned}$$

Strategies to solve Eqn. (6) [and (7)]

Strategy 1. Straight application of the equation.

Strategy 2. Basic 2-stage process [“flip/flop”].

[e.g., Santiago/Werbos, Prokhorov/Wunsch]

During stage 1, train criticNN, not actionNN;

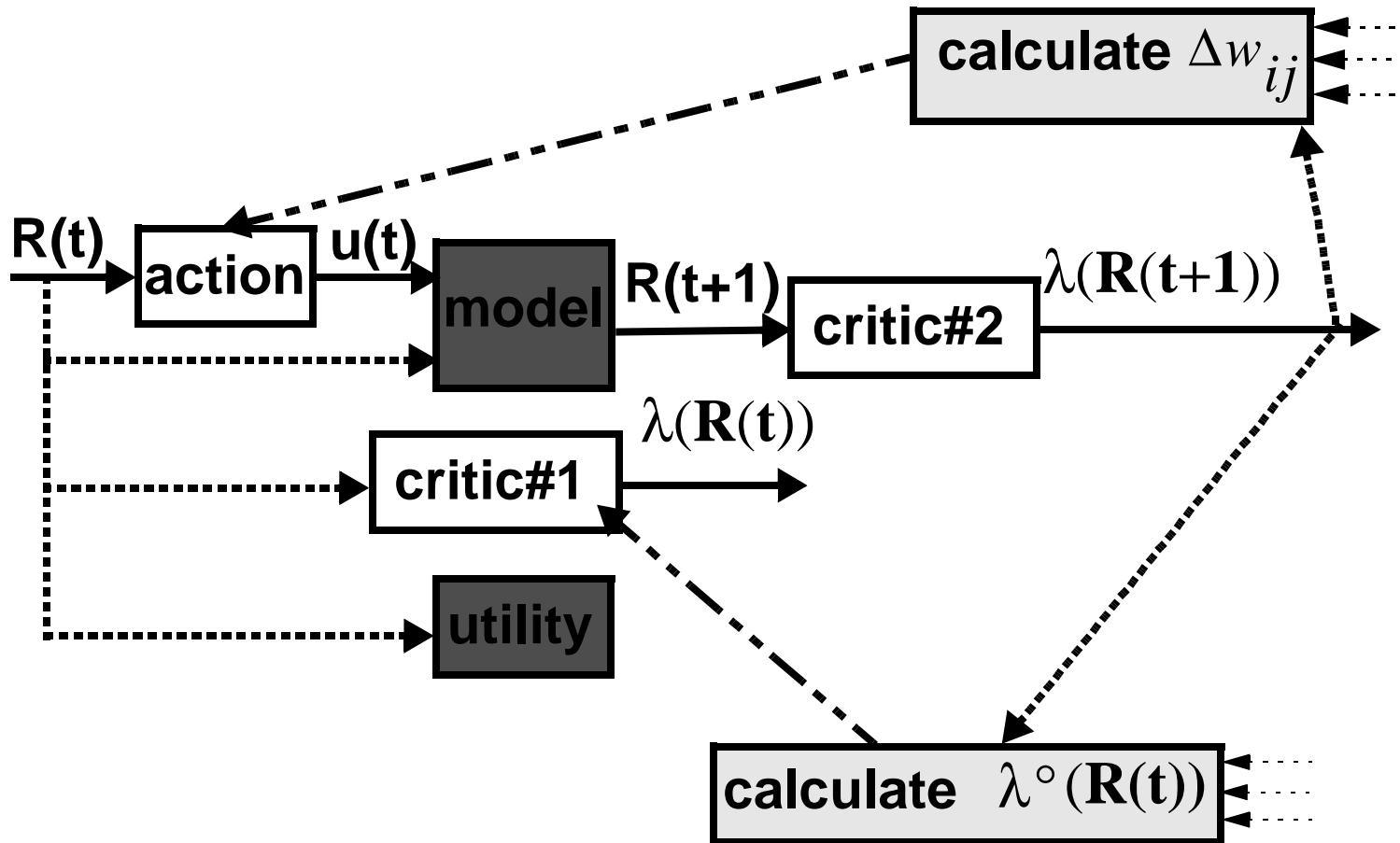
During stage 2, train actionNN, not criticNN.

Strategy 3. Modified 1st stage of 2-stage process.

While train criticNN during stage 1, keep parameters constant in module that calculates critic’s desired output $\lambda^\circ(R)$.
Then adjust weights all at once at end of stage 1.

Strategy 4. Single-stage process, using modifications introduced in Strategy 3.

Computing Schema for discussing Strategies



Recap re. criticNN:

Performs mapping: $\lambda(\mathbf{R})$

Desired output for training purposes: $\lambda^\circ(\mathbf{R})$

Solution (not known) of Bellman equation: $\lambda^\wedge(\mathbf{R})$

Learn process: $\lambda(\mathbf{R})$ is to converge to $\lambda^\circ(\mathbf{R})$;

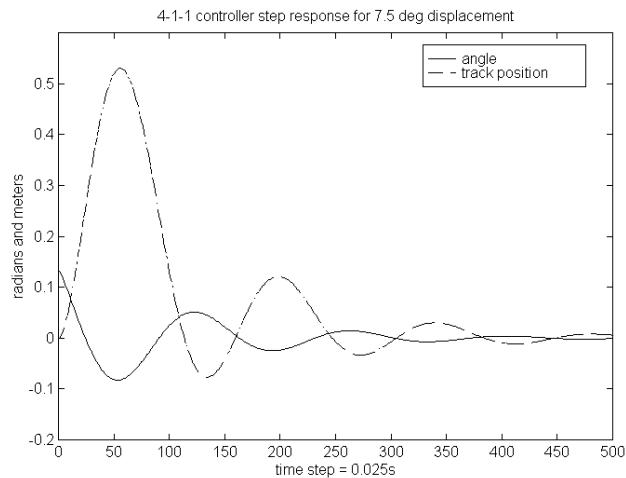
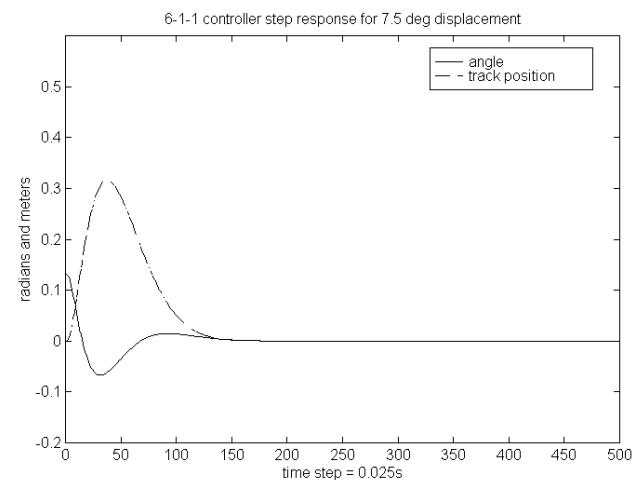
$\lambda^\circ(\mathbf{R})$ is to converge to $\lambda^\wedge(\mathbf{R})$.

i.e., $\lambda(\mathbf{R})$ $\lambda^\circ(\mathbf{R})$ $\lambda^\wedge(\mathbf{R})$

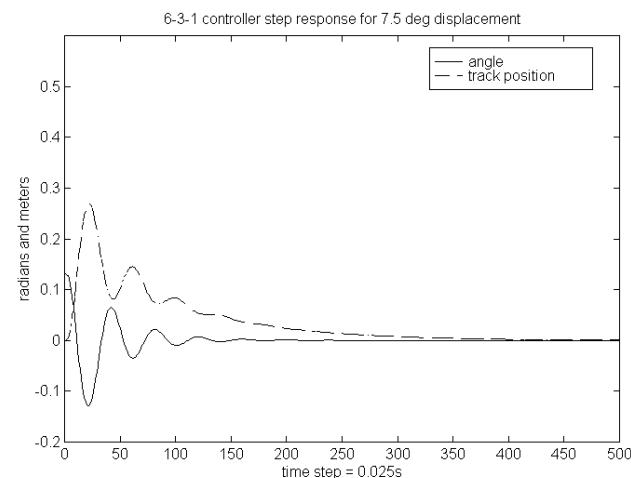
**[The better the criticNN “solves” the Bellman eqn.,
the better the actionNN will approximate an
optimal controller.]**

Step Responses to 7.5° pole displacement

6-1-1 Controller



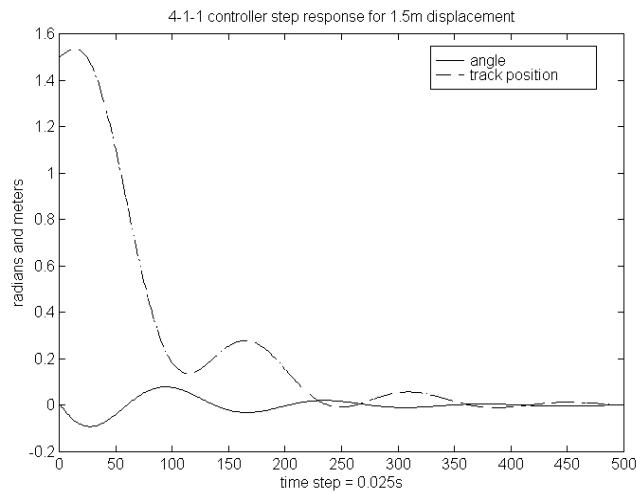
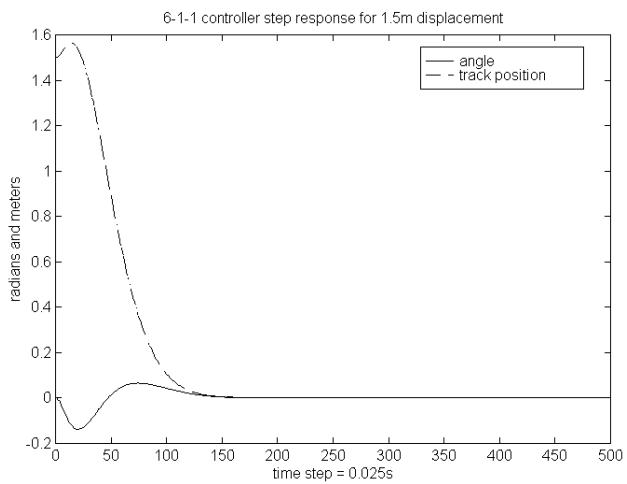
4-1-1 Controller



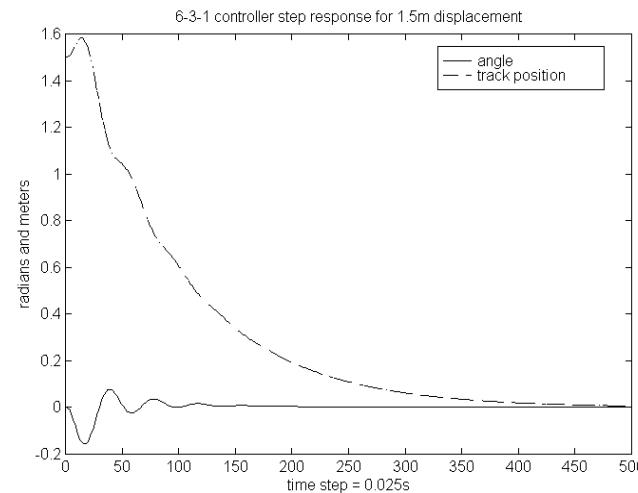
6-3-1 Controller

Step Responses to 1.5m cart displacement

6-1-1 Controller



4-1-1 Controller



6-3-1 Controller

Step Responses of 6-1-1 Controller, 1m pole

[Trained w/ max $\pm 10^\circ$]
[No explicit X training]

Trained: 7.5°displ.

Tested: 38°displ.

Tested: -6.6m displ.

