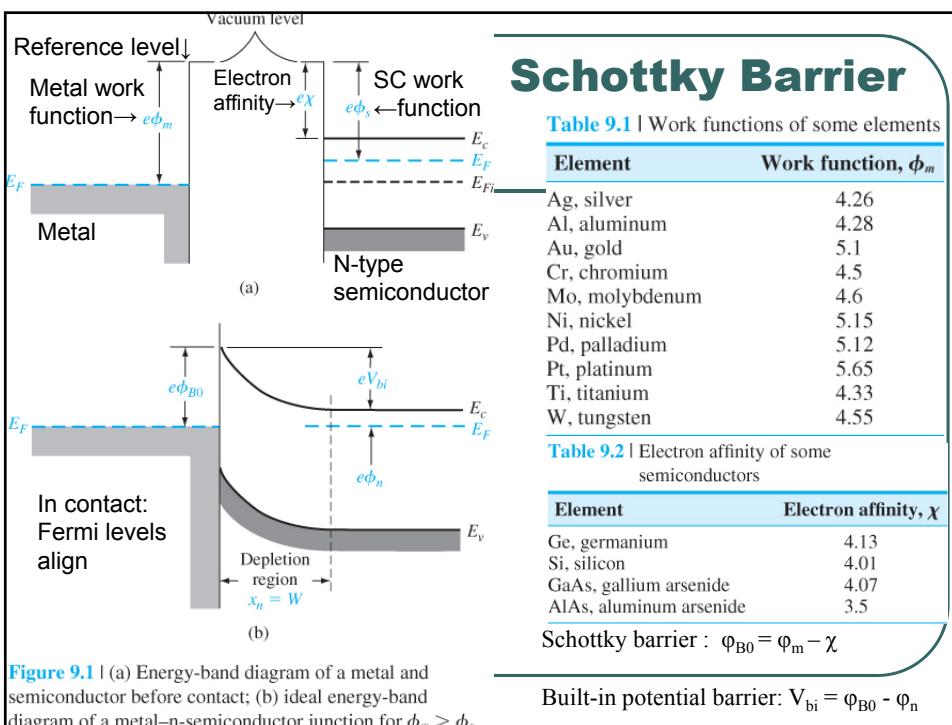


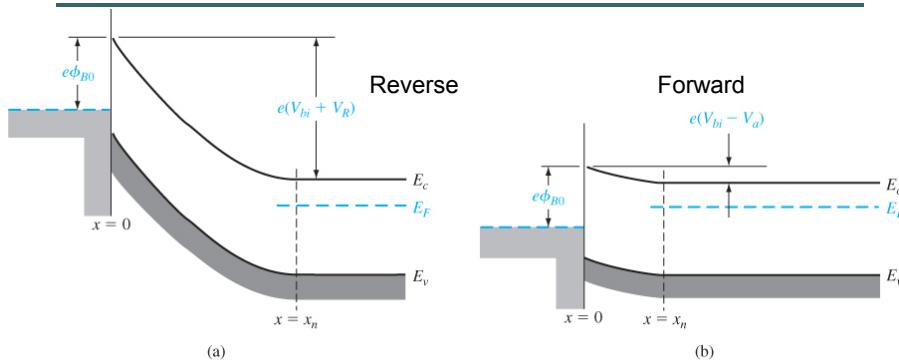
# **EE415/515 Fundamentals of Semiconductor Devices**

## **Fall 2012**

### **Lecture 9: MS & Hetero-Junctions (Chapter 9)**



## Schottky barrier bias



**Figure 9.2** | Ideal energy-band diagram of a metal–semiconductor junction (a) under reverse bias and (b) under forward bias.

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## Ideal Schottky junction

$$\text{In space charge region } \frac{dE}{dx} = \frac{\rho(x)}{\epsilon}$$

$$E = \int \frac{eN_d}{\epsilon_s} dx \text{ for uniform doping}$$

$$= \frac{eN_d}{\epsilon_s} x + C_1$$

$$= 0 \text{ at } x = x_n \text{ so } C_1 = -\frac{eN_d x_n}{\epsilon_s}$$

$$\text{and } E = \frac{eN_d}{\epsilon_s} (x - x_n) = -\frac{eN_d}{\epsilon_s} (x_n - x)$$

$$\text{Max } E(0) = -\frac{eN_d}{\epsilon_s} x_n$$

$E(0^-)$  is zero in metal, so (Gauss' Law)  $\rightarrow$  negative interface surface charge in metal

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## Ideal Schottky junction

As for one - sided p<sup>+</sup>n junction

$$W = x_n = \sqrt{\frac{2\epsilon_s(V_{bi} + V_R)}{eN_d}}$$

$$C' = eN_d \frac{dx_n}{dV_R} = \sqrt{\frac{e\epsilon_s N_d}{2(V_{bi} + V_R)}}$$

Plot  $\left(\frac{1}{C'}\right)^2 = \frac{2(V_{bi} + V_R)}{e\epsilon_s N_d}$  vs V<sub>R</sub> gives V<sub>bi</sub> (intercept) and N<sub>d</sub> (slope)

Then  $\phi_{B0} = V_{bi} - \phi_n$  where  $\phi_n$  calculated as E<sub>C</sub> - E<sub>F</sub>

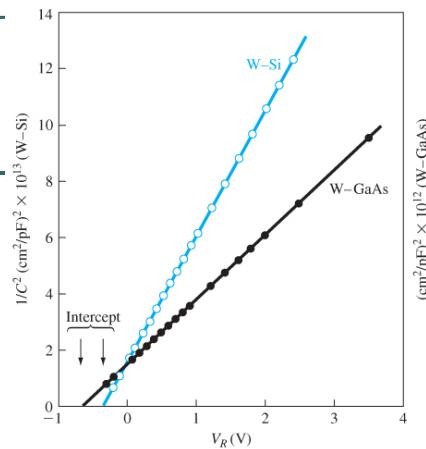


Figure 9.3 | 1/C<sup>2</sup> versus V<sub>R</sub> for W-Si and W-GaAs Schottky barrier diodes.  
(From Sze and Ng [15].)

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**Ex 9.1 Ideal W to n-type GaAs M-S junction; N<sub>d</sub>=5x10<sup>15</sup>/cm<sup>3</sup>.  
Find theoretical barrier height, built-in potential barrier, and maximum electric field for zero applied bias.**

$$\phi_{B0} = \phi_m - \chi = 4.55 - 4.07 = 0.48 \text{ V}$$

$$\begin{aligned} \phi_n &= V_t \ln\left(\frac{N_c}{N_d}\right) = (0.0259) \ln\left(\frac{4.7 \times 10^{17}}{5 \times 10^{15}}\right) \\ &= 0.1177 \text{ V} \end{aligned}$$

$$V_{bi} = \phi_{B0} - \phi_n = 0.48 - 0.1177 = 0.3623 \text{ V}$$

$$\begin{aligned} x_n &= \left\{ \frac{2\epsilon_s V_{bi}}{eN_d} \right\}^{1/2} \\ &= \left\{ \frac{2(13.1)(8.85 \times 10^{-14})(0.3623)}{(1.6 \times 10^{-19})(5 \times 10^{15})} \right\}^{1/2} \\ &= 3.24 \times 10^{-5} \text{ cm} \end{aligned}$$

$$\begin{aligned} |E_{max}| &= \frac{eN_d x_n}{\epsilon_s} \\ &= \frac{(1.6 \times 10^{-19})(5 \times 10^{15})(3.24 \times 10^{-5})}{(13.1)(8.85 \times 10^{-14})} \\ &= 2.24 \times 10^4 \text{ V/cm} \end{aligned}$$

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**Ex 9.2 Find the GaAs doping concentration and Schottky barrier height for the W-GaAs diode in Fig 9.3 (slide 5).**

From Figure 9.3,

$$V_{bi} \approx 0.64 \text{ V}$$

$$\frac{\Delta \left( \frac{1}{C'} \right)^2}{\Delta V_R} \approx \frac{8.5 \times 10^{12}}{3 + 0.64} = 2.335 \times 10^{12}$$

$$\text{Then } N_d = \frac{2}{e \epsilon_s} \cdot \frac{1}{\Delta \left( \frac{1}{C'} \right)^2} \\ \frac{2}{\Delta V_R}$$

$$= \frac{2}{(1.6 \times 10^{-19})(13.1)(8.85 \times 10^{-14})(2.335 \times 10^{12})}$$

$$\text{or } N_d = 4.62 \times 10^{18} \text{ cm}^{-3}$$

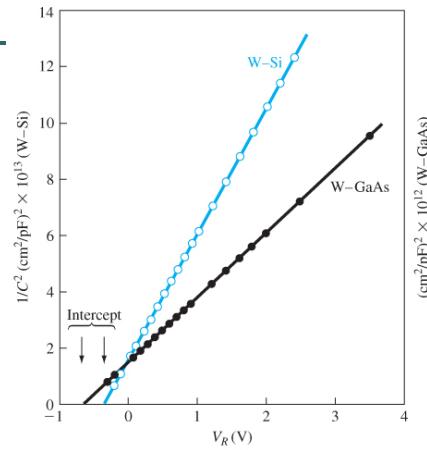


Figure 9.3 |  $1/C^2$  versus  $V_R$  for W-Si and W-GaAs Schottky barrier diodes.  
(From Sze and Ng [15].)

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## Schottky Effect (barrier lowering)

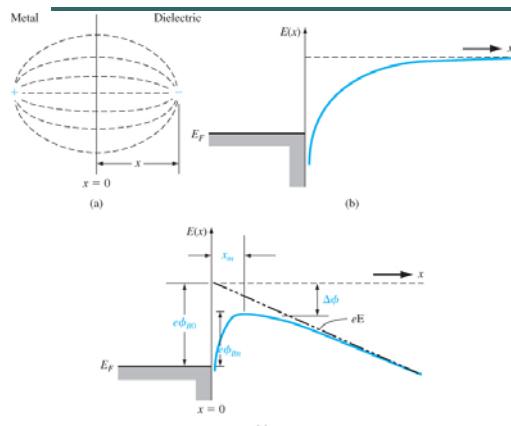


Figure 9.4 | (a) Image charge and electric field lines at a metal-dielectric interface.  
(b) Distortion of the potential barrier due to image forces with zero electric field and (c) with a constant electric field.

As electron leaves metal surface,  
image charge exerts restoring force

$$F = -eE = \frac{-e^2}{4\pi\epsilon_s(2x)^2}$$

$$\text{Potential: } -\phi(x) = + \int_x^\infty \frac{e}{16\pi\epsilon_s(x')^2} dx' \\ = \frac{-e}{16\pi\epsilon_s x} \text{ for } \phi(\infty) = 0$$

With applied field E :

$$-\phi(x) = \frac{-e}{16\pi\epsilon_s x} - Ex$$

Maximum barrier when  $\frac{d(e\phi(x))}{dx} = 0$

$$\text{at } x_m = \sqrt{\frac{e}{16\pi\epsilon_s E}} \text{ where } \Delta\phi = \sqrt{\frac{eE}{4\pi\epsilon_s}}$$

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**Ex 9.3 Calculate the Schottky barrier lowering for a GaAs M-S contact for which the electric field in the GaAs is  $E=6.8 \times 10^4 \text{ V/cm}$ , for reverse biases of (a)  $V_R=1\text{V}$  & (b)  $V_R=5\text{V}$ .**

$$\begin{aligned}x_n &= \left\{ \frac{2 \epsilon_s (V_{bi} + V_R)}{e N_d} \right\}^{1/2} \\&= \left\{ \frac{2(11.7)(8.85 \times 10^{-14})(V_{bi} + V_R)}{(1.6 \times 10^{-19})(10^{16})} \right\}^{1/2} \\&= \left\{ (1.294 \times 10^{-9})(V_{bi} + V_R) \right\}^{1/2} \\(a) \quad V_R = 1\text{V}, \quad V_{bi} = 0.334\text{V} \\&\Rightarrow x_n = 4.155 \times 10^{-5} \text{ cm} \\|E_{max}| &= \frac{e N_d x_n}{\epsilon_s} \\&= \frac{(1.6 \times 10^{-19})(10^{16})(4.155 \times 10^{-5})}{(11.7)(8.85 \times 10^{-14})} \\&= 6.42 \times 10^4 \text{ V/cm}\end{aligned}$$

$$\begin{aligned}\text{Then } \Delta\phi &= \sqrt{\frac{eE}{4\pi \epsilon_s}} \\&= \sqrt{\frac{(1.6 \times 10^{-19})(6.42 \times 10^4)}{4\pi(11.7)(8.85 \times 10^{-14})}} \\&= 0.0281 \text{ V} \\(a) \quad V_R = 5\text{V}, \quad x_n &= 8.309 \times 10^{-5} \text{ cm} \\|E_{max}| &= \frac{(1.6 \times 10^{-19})(10^{16})(8.309 \times 10^{-5})}{(11.7)(8.85 \times 10^{-14})} \\&= 1.284 \times 10^5 \text{ V/cm} \\&\Delta\phi = \sqrt{\frac{(1.6 \times 10^{-19})(1.284 \times 10^5)}{4\pi(11.7)(8.85 \times 10^{-14})}} \\&\Delta\phi = 0.0397 \text{ V}\end{aligned}$$

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## Interface States

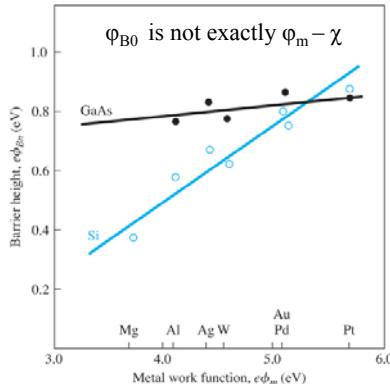


Figure 9.5 | Experimental barrier heights as a function of metal work functions for GaAs and Si.  
(From Crowley and Sze [2].)

$$(E_g - e\phi_0 - e\phi_{Bn}) = \frac{1}{eD_u} \sqrt{2e\epsilon_s N_d (\phi_{Bn} - \phi_n)} - \frac{\epsilon_i}{eD_u \delta} [\phi_m - (\chi + \phi_{Bn})]$$

If  $D_u \rightarrow \infty$   $\phi_{Bn} = (E_g - e\phi_0)/e$       If  $D_u \delta \rightarrow 0$   $\phi_{Bn} = \phi_m - \chi$

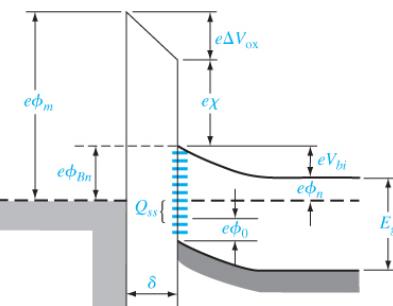


Figure 9.6 | Energy-band diagram of a metal-semiconductor junction with an interfacial layer and interface states.

### More complete model:

- Thin oxide (electron transparent)
- $D_u/\text{cm}^2\cdot\text{eV}$  surface states in semiconductor
- Donor states below  $e\phi$
- Acceptor states above  $e\phi$

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## I-V characteristics

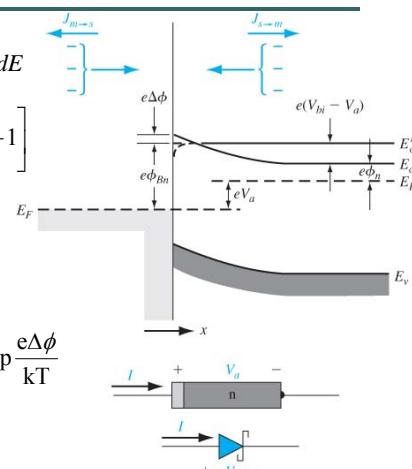
As before  $dn = \frac{4\pi(2m_n^*)^{\frac{3}{2}}}{h^3} \sqrt{E - E_c} \exp\left[-\frac{E - E_F}{kT}\right] dE$

$$J = J_{s \rightarrow m} - J_{m \rightarrow s} = \left[ A * T^2 \exp\left(-\frac{e\phi_{Bn}}{kT}\right) \right] \left[ \exp\left(\frac{eV_a}{kT}\right) - 1 \right]$$

$$= J_{st} \left[ \exp\left(\frac{eV_a}{kT}\right) - 1 \right]$$

where  $J_{st} = A * T^2 \exp\left(-\frac{e\phi_{Bn}}{kT}\right)$  and  $A^* = \frac{4\pi e m_n^* k^2}{h^3}$

and with barrier lowering  $J_{st} = A * T^2 \exp\left(-\frac{e\phi_{Bn}}{kT}\right) \exp\left(\frac{e\Delta\phi}{kT}\right)$



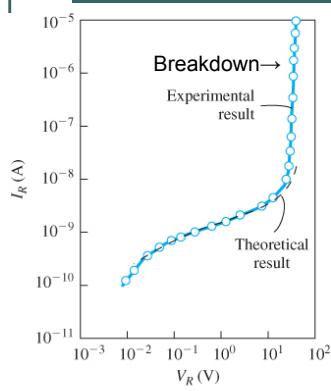
**Figure 9.7** | Energy-band diagram of a forward-biased metal–semiconductor junction including the image lowering effect.

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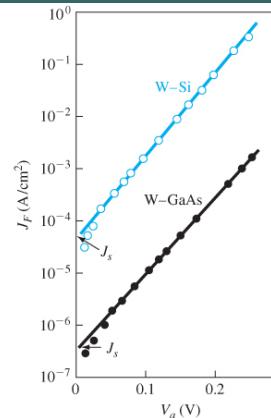
## Device characteristics

Reverse current increases with  $V_R$  due to barrier lowering

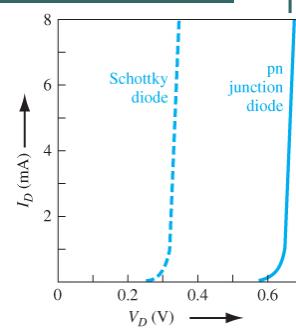
Plot gives  $J_{st}$  and hence (Si)  
 $A^* = 114 \text{ A/K}^2 \cdot \text{cm}^2$  for  $\phi_{Bn} = 0.67 \text{ V}$



**Figure 9.8** | Experimental and theoretical reverse-biased currents in a PtSi–Si diode. (From Sze and Ng [15].)



**Figure 9.9** | Forward-bias current density  $J_F$  versus  $V_a$  for Wi–Si and W–GaAs diodes. (From Sze and Ng [15].)



**Figure 9.10** | Comparison of forward-bias  $I$ - $V$  characteristics between a Schottky diode and a pn junction diode

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**Ex 9.4 Calculate the ideal Richardson constant for a free electron.**

$$A^* = \frac{4\pi e m_n^* k^2}{h^3}$$

Assume  $m_n^* = m_o$ , then

$$A^* = \frac{4\pi (1.6 \times 10^{-19}) (9.11 \times 10^{-31}) (1.38 \times 10^{-23})^2}{(6.625 \times 10^{-34})^3}$$

$$= 1.20 \times 10^6 \text{ A/K}^2 \cdot \text{m}^2$$

$$\Rightarrow A^* = 120 \text{ A/K}^2 \cdot \text{cm}^2$$

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**Ex 9.5 Use the results of Example 9.5 to determine the forward bias voltages required to produce a current of  $10\mu\text{A}$  in a W-Si diode of measured barrier height  $\varphi_{Bn}=0.67\text{eV}$  and a P-N junction of  $J_s=3.66 \times 10^{-11}\text{A/cm}^2$ . Assume junction areas of  $10^{-4}\text{cm}^2$ .**

$$I \cong AJ_s \exp\left(\frac{V_a}{V_t}\right)$$

$$\text{so that } V_a = V_t \ln\left(\frac{I}{AJ_s}\right)$$

For the pn junction:

$$V_a = (0.0259) \ln\left(\frac{10 \times 10^{-6}}{(10^{-4})(3.66 \times 10^{-11})}\right)$$

$$= 0.5628 \text{ V}$$

For the Schottky junction:

$$V_a = (0.0259) \ln\left(\frac{10 \times 10^{-6}}{(10^{-4})(5.98 \times 10^{-5})}\right)$$

$$= 0.1922 \text{ V}$$

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**Ex 9.6 A PN diode and a Schottky diode have equal c/s areas and forward bias currents of 0.5mA. The Schottky reverse saturation current is  $5 \times 10^{-7}$ A. The difference between the forward bias voltages is 0.30V. Find the reverse saturation current of the PN diode.**

$$\frac{I_{ST} \exp\left(\frac{V_a - 0.3}{V_t}\right)}{I_S \exp\left(\frac{V_a}{V_t}\right)} = 1 = \frac{I_{ST}}{I_S} \exp\left(\frac{-0.3}{V_t}\right)$$

Then

$$I_S = (5 \times 10^{-7}) \exp\left(\frac{-0.3}{0.0259}\right)$$

$$\Rightarrow I_S = 4.66 \times 10^{-12} \text{ A}$$

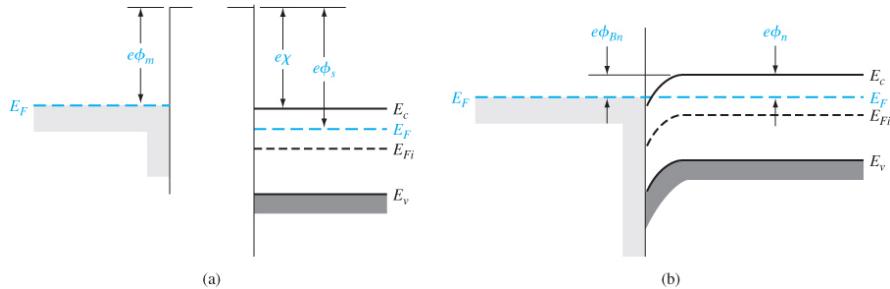
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## M-S Ohmic Contacts: Ideal non-rectifying barrier (N-type)

Previous case:  $\phi_m > \phi_s$ , (Schottky diode.) Consider now  $\phi_m < \phi_s$  (below). No barrier to electron flow semiconductor  $\rightarrow$  metal Effective barrier height for electron flow metal  $\rightarrow$  semiconductor is  $\phi_{Bn} = \phi_n$  (small) Hence ohmic contact.



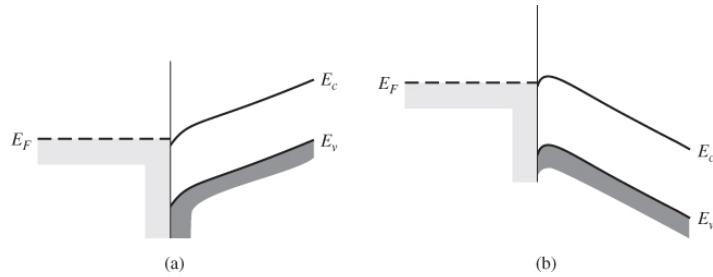
**Figure 9.11** | Ideal energy-band diagram (a) before contact and (b) after contact for a metal-n-type semiconductor junction for  $\phi_m < \phi_s$ .

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## Biased N-type Ohmic contacts



**Figure 9.12** | Ideal energy-band diagram of a metal-n-type semiconductor ohmic contact (a) with a positive voltage applied to the metal and (b) with a positive voltage applied to the semiconductor.

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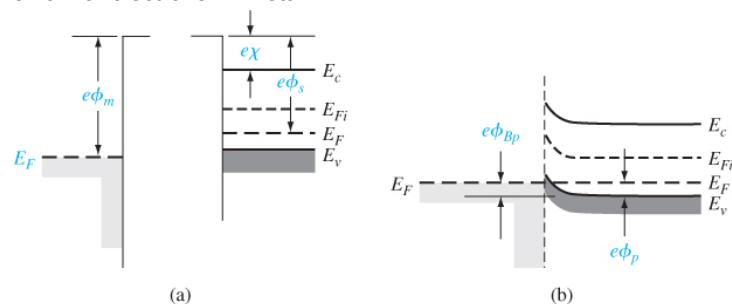
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## M-S Ohmic Contacts: Ideal non-rectifying barrier (P-type with $\phi_m > \phi_s$ )

Electrons flow metal  $\rightarrow$  sc valence band,  
(or no barrier to hole flow sc valence band  $\rightarrow$  metal)

Barrier small for electrons  $\rightarrow$  metal



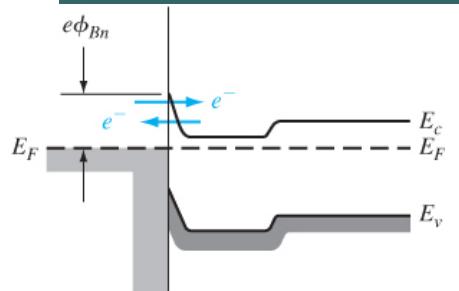
**Figure 9.13** | Ideal energy-band diagram (a) before contact and (b) after contact for a metal-p-type semiconductor junction for  $\phi_m < \phi_s$ .

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## Tunneling barrier



**Figure 9.14** | Energy-band diagram of a heavily doped n-semiconductor-to-metal junction.

When a Schottky barrier would otherwise result, (n - type with  $\phi_m > \phi_s$  or p - type with  $\phi_m < \phi_s$ ) dope the semiconductor very heavily.

Space charge  $\propto N_d^{-\frac{1}{2}}$  so barrier very thin, and electrons can tunnel through.

$$J_t \propto \exp - \frac{2e\phi_{Bn}}{e\hbar} \sqrt{\frac{\epsilon_s m_n^*}{N_d}}$$

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**Ex 9.7 Calculate the space charge width of a rectifying metal-GaAs junction. Assume  $N_d=7\times10^{18}/\text{cm}^3$  in the GaAs and that the built-in potential barrier is  $V_{bi}=0.80\text{V}$ .**

We have

$$\begin{aligned} x_n &= \left\{ \frac{2 \epsilon_s V_{bi}}{e N_d} \right\}^{1/2} \\ &= \left\{ \frac{2(13.1)(8.85 \times 10^{-14})(0.80)}{(1.6 \times 10^{-19})(7 \times 10^{18})} \right\}^{1/2} \\ &= 1.287 \times 10^{-6} \text{ cm} \end{aligned}$$

or  $x_n = 128.7 \text{ } \overset{\circ}{\text{A}}$

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## Contact resistance

$$R_c = \left( \frac{\partial J}{\partial V} \right)^{-1} \Big|_{V=0} \quad \text{in } \Omega \cdot \text{cm}^2$$

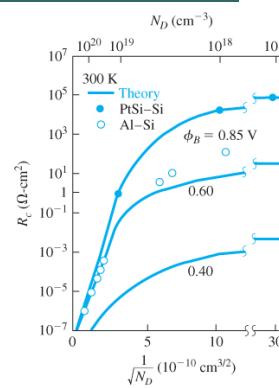
For rectifying contact, thermionic current dominates :

$$J_n = A * T^2 \exp\left(\frac{-e\phi_{Bn}}{kT}\right) \left[ \exp\frac{eV}{kT} - 1 \right]$$

$$\text{so } R_c = \frac{1}{A * T^2} \cdot \frac{kT}{e} \cdot \exp\frac{e\phi_{Bn}}{kT}$$

For tunneling contact (large  $N_d$ )

$$R_c \propto \exp\left(\frac{2\sqrt{\epsilon_s m_m^*}}{\hbar} \cdot \frac{\phi_{Bn}}{\sqrt{N_d}}\right)$$



**Figure 9.15** | Theoretical and experimental specific contact resistance as a function of doping.  
(From Sze and Ng [15].)

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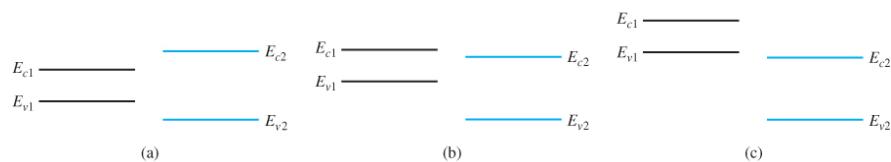
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## Heterojunctions

Homojunctions → same semiconductor (e.g. GaAs) on both sides  
Heterojunctions → different materials

e.g. GaAlAs system .... Vary composition to vary band-gap



**Figure 9.16** | Relation between narrow-bandgap and wide-bandgap energies: (a) straddling, (b) staggered, and (c) broken gap.

“Straddling” most common, and considered below

“Anisotype” → different doping

→ Np or Pn (where “N” or “P” indicates the larger bandgap material)

“Isotype” → Nn or Pp

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## e.g. nP (Ge/GaAs)

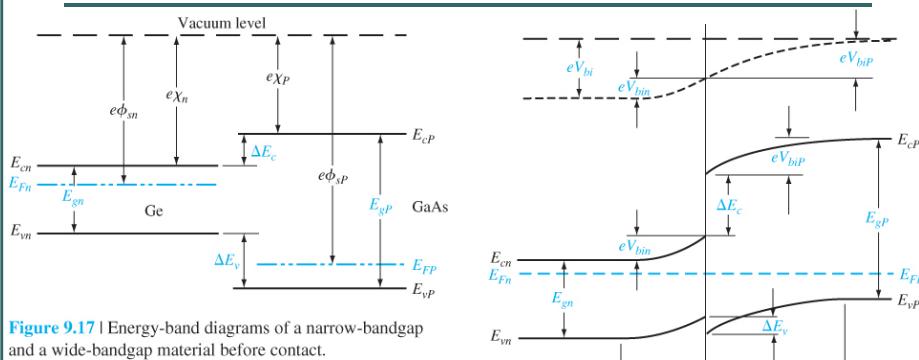


Figure 9.17 | Energy-band diagrams of a narrow-bandgap and a wide-bandgap material before contact.

$$\Delta E_c = e(\chi_n - \chi_p)$$

$$\Delta E_c + \Delta E_v = E_{gP} - E_{gn} = \Delta E$$

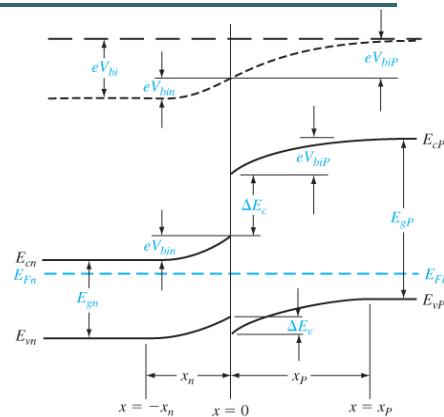


Figure 9.18 | Ideal energy-band diagram of an nP heterojunction in thermal equilibrium.

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## Np heterojunction

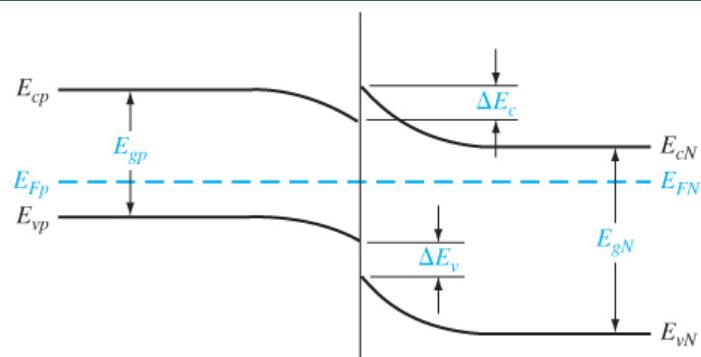


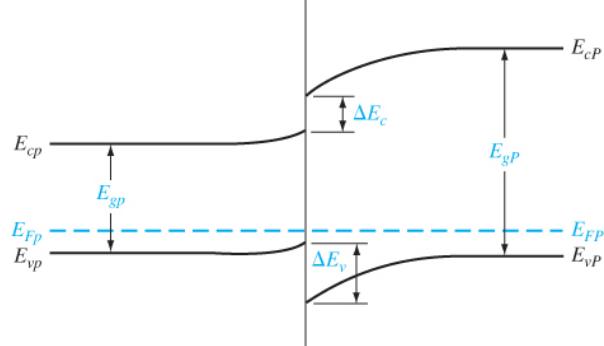
Figure 9.23 | Ideal energy-band diagram of an Np heterojunction in thermal equilibrium.

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## pP heterojunction



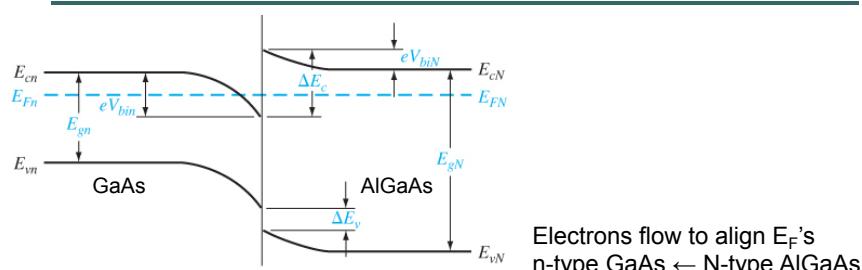
**Figure 9.24** | Ideal energy-band diagram of a pP heterojunction in thermal equilibrium.

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## nN GaAs-AlGaAs heterojunction



**Figure 9.19** | Ideal energy-band diagram of an nN heterojunction in thermal equilibrium.

Electrons flow to align  $E_F$ 's  
n-type GaAs  $\leftarrow$  N-type AlGaAs

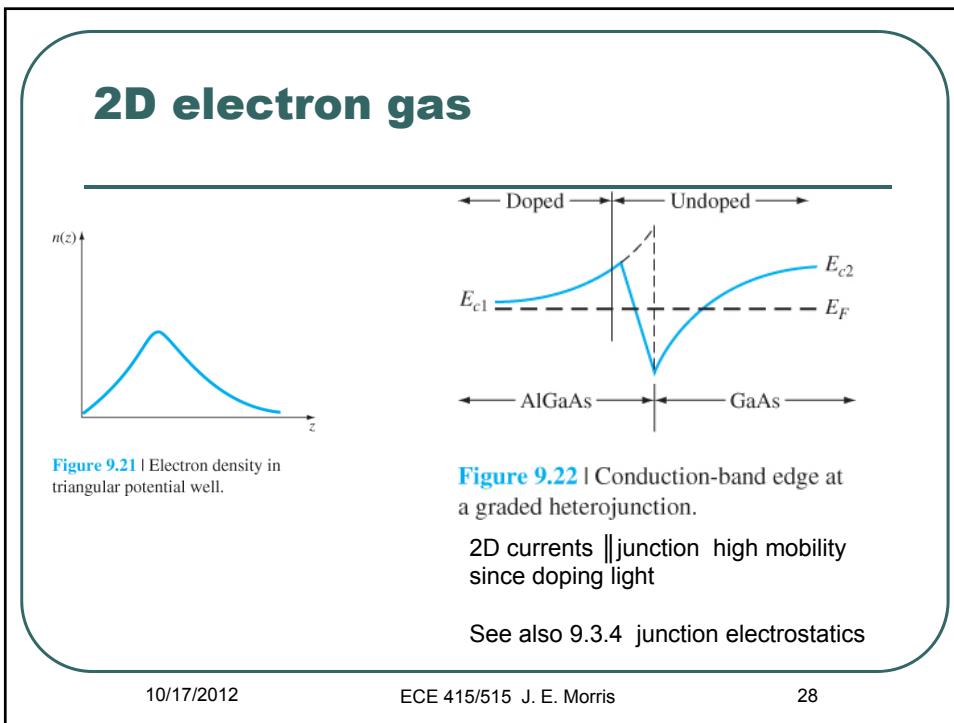
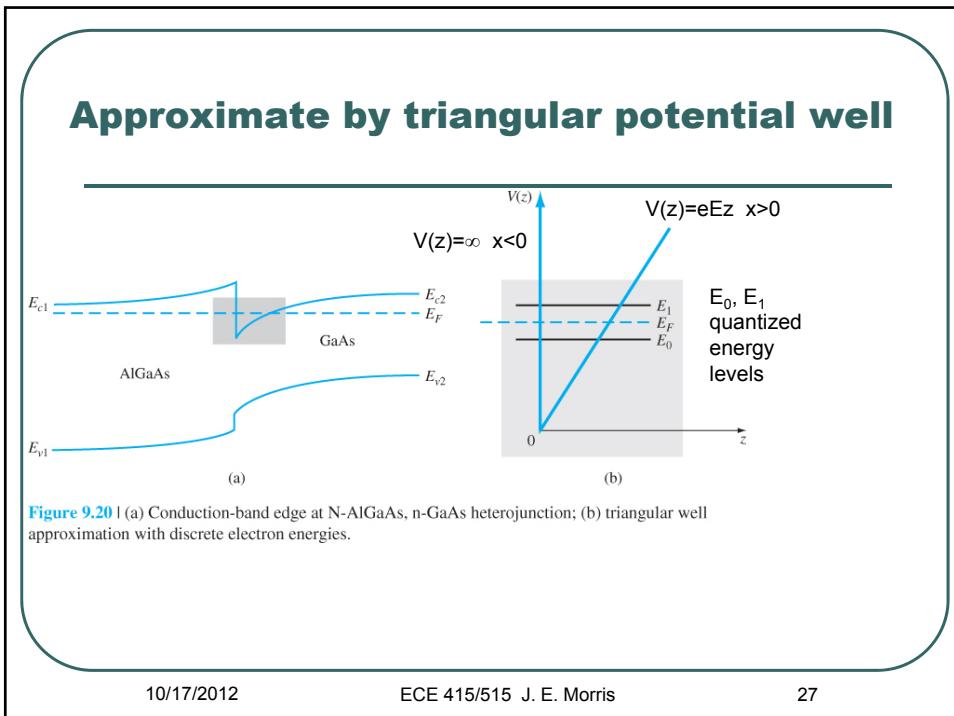
Electrons in interface potential well

“2-D electron gas”  
Quantized energy levels  $\perp$  j'n  
Free to move in 2D  $\parallel$  junction

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**Ex 9.8 Find  $\Delta E_c$ ,  $\Delta E_v$ ,  $V_{bi}$  for n-Ge P-GaAs heterojunction at 300K using the electron affinity rule. ( $n_i=2.4 \times 10^{13}/\text{cm}^3$  for Ge.)  
N-Ge:  $N_d=10^{15}/\text{cm}^3$       P-GaAs:  $N_a=10^{15}/\text{cm}^3$ .**

From Example 9.8,  $\Delta E_v = 0.70 \text{ eV}$ .

We find

$$p_{no} = \frac{n_i^2}{N_d} = \frac{(2.4 \times 10^{13})^2}{10^{15}} = 5.76 \times 10^{11} \text{ cm}^{-3}$$

Now

$$\begin{aligned} eV_{bi} &= \Delta E_v + kT \ln \left( \frac{p_{po}}{p_{no}} \cdot \frac{N_{vn}}{N_{vp}} \right) \\ &= 0.70 + (0.0259) \ln \left[ \frac{(10^{15})(6 \times 10^{18})}{(5.76 \times 10^{11})(7 \times 10^{18})} \right] \end{aligned}$$

or  $V_{bi} = 0.889 \text{ V}$

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