











Gnox corresponds to the point where the interatomic forces would yield, is the material should break at about 5 mix = E/10 In practice: Gr (measured) ~ E/104 (But very small samples is. this films a whisker can reach Gp ~ E/15 or so.) POSTULATE: Small flaws or micro-cracks. (Statistically less likely to occur in a very small sample, hence size effect.) > This fiber stronger ofher thick rods.) Stress concentration ECE414/514 Electronics -----Packaging Spring 2012



Ob - elastic relationship for small crack L, Od — " "large "Lz When crack grows L, -> Lz, elastic curve shifts b-2 if crack propagation Li > L2 at constant displacements (or $b \rightarrow d$ if at constant load $P_b = P_d$) Work is done to open crack: For constant displacement | For constant load b > C b > d Initial stored energy at b Final stored energy at b Area Oce Area Oce Area Obc Supplied from internal t Stored energy. Reduced stored energy. Initial stored energy. Box of the stored energy energy. Box of the stored energy energy ene b->d Area Odf = Oce from storage + e cdf from wo Area (Obe + bdfe - Odf)=Obd Represents external = Obc from internal storage work Predistance + bdc from external Reduced stored energy - work. 5/21/2012 ECE414/514 Electronics 9 Packaging Spring 2012

Energy absorbed by growth
i.e. Work =
$$R(A_2 - A_1)$$
 where $R = \text{fracture toughness}$
= $R + (L_2 - L_1)$
 $R \implies \frac{\text{Area Obc}}{A_2 - A_1}$ $\frac{\text{Area Obd}}{A_2 - A_1}$
(greater, representing
external work done)
For incremental crack growth $L_2 = L_1 + \Delta L$
 k for large P , the difference (Area bdc) $\implies O$
 $bd + o$
 $bc - o$
In practice, crack growth P
 $M = \frac{M}{1 + M} = \frac{M}{1 + M}$
 $k = \frac{M}{1 + M} = \frac{M}{1 + M} = \frac{M}{1 + M}$
 $M = \frac{M}{1 + M} = \frac{M}{1 + M}$

ENERGY BALANCE for general case
$$P$$
, $\frac{\Delta S}{2}$
External work = $P\Delta S$
Grack pabsorbs energy = $R\Delta A$
Strain energy $\Delta charges$ by ΔA
Strain energy Δt j is area $Ojn = \frac{1}{2}PS$
 $\therefore \Delta A = \frac{1}{2}\Delta (PS)$
 $\therefore External work PAS = \Delta A$ + $R\Delta A$
 $Charge in introd strain energy Crack grant takes
 $PAS = \frac{1}{2}A(PS) + R\Delta A$
 $is P.\Delta S - S.\Delta P = 2R.\Delta A$
 $\frac{1}{P}\frac{\Delta S}{P^2} - \frac{S}{P^2}\frac{\Delta P}{AR} = \frac{2R}{P^2} + R\Delta A$
 $\frac{1}{QA}\left(\frac{S}{P}\right) = \frac{2R}{P^2} \rightarrow \frac{P^2}{crack} = \frac{2R}{dA}\left(\frac{S}{P}\right)$ 11$

Note on notation: Using R fracture doughness here. Commonly R written Gc "critical strain energy release note" 4.4 AP Path absor 00 Path W PS releases = constant Constant displacement Constant Load Final energy < puthol ... "released" by Final Encry > Initial ic about absorbed by crack propagation .. "rekeased og crack propagation by crack projogen-.: energy release not general 5/21/2012 ECE414/514 Electronics 12 Packaging Spring 2012





00 1 1 & Stress $\therefore \text{ Work done to fracture} = \int_{-\infty}^{\lambda/2} \mathcal{E}_{\text{max}} \sin\left(\frac{2\overline{u}x}{\lambda}\right) dx$ Atomic duplacement = $\left[-\cos\frac{2\pi}{\lambda}\right]^{\lambda/2} \leq m_{\chi} \frac{\lambda}{2\pi}$ (see back) A just wavelength of oppose. sine curve "Expect" 2~a. = XEmax/T = Increase in energy of TWO surfaces = 2 % = surface energy ic. I max = 21 ds relates of ys Another commonly the gnoted result from $\rightarrow G_{max} = \int \frac{E \delta_s}{a_0} \rightarrow \int \frac{E R}{T L}$ $G_{max} = \frac{2 \Pi \delta_s}{\lambda} \quad k \in G_{max} = \frac{\lambda E}{2 \Pi a_0} \quad \beta R = 2 \delta_s$ PR=285 & L=2α0/TT 15

4.231 Note: These variations all seen to be about dhe same as the first theoretical attempt ie. Gmox ~ E/10 which we already know is . OK for very small (no crack) specimens, but doo high for general use. (a) Consider brittle materials (eg gloss): By measurement R~ Vs So use the implied R= 27's above (b) Consider ductile materials: R>>> 8/5 (typ R = 10005) Extra work goes into plastic deformation of crack tip zone

















STRESS-CORROSION CRACK GROWTH & FAILURE PREDICTION for multiple mechanism gions I.L. Effective rate determined by 81 Writing da. dt an ā_{II} ar ar ġ + asteachy state cracking time + aI てき dt da where mK. a_r = С, е Com functions of T, P SH/RT. \mathcal{P}^{n} С, an _= e











Kirkendall VoidsInterface - dissimilar metalsMetal 1:
$$D_1$$
Metal 1: D_1 Metal 2:High diffusion 0coefficiente.g. Al $D_1 > D_2$ Net effect: 0 AlAlVoids developon Metal 1 side $5/21/2012$ ECE414/514 ElectronicsPackaging Spring 201231









FIG. 19. Schematic diagram depicting the effect of void formation and propagation on the current entering the solder bump. While the current is being displaced to the front of the void, there is little change in resistance. Only when the void has propagated across the entire contact interface, the resistance will jump abruptly (Ref. 59).







TABLE I.	Melting point	and diffusivities of Cu	1, Al, and eutectic SnPb.	Diffusivities at 350 °C	
	point (K)	373 K/T m	Diffusivities at 100 °C (cm ² /s)	(cm^2/s)	
Cu	1356	0.275	Lattice $D_l = 7 \times 10^{-28}$	$D_l = 5 \times 10^{-17}$	
			Grain boundary $D_{gb} = 3 \times 10^{-15}$ Surface $D_s = 10^{-12}$	$D_{gb} = 1.2 \times 10^{-9}$ $D_s = 10^{-8}$	
Al	933	0.4	Lattice $D_l = 1.5 \times 10^{-19}$	$D_l = 10^{-11}$	
			Grain boundary $D_{gb} = 6 \times 10^{-11}$	$D_{\rm gb} = 5 \times 10^{-7}$	
Eutectic SnPb	456	0.82	Lattice $D_l = 2 \times 10^{-9} - 2 \times 10^{-10}$	Molten state $D_l > 10^{-5}$	



MTTI	F =	Aj ⁻ⁿ e	$exp\left(\frac{Q}{kt}\right)$) n= (B	= 1.8, Q = (y Flip Chij	0.8 eV p Technol (hrs)	ogies)
	1.5 A (1.9x10 ⁴ A/cm ²)		1.8 A (2.25 x10 ⁴ A/cm ²)		$\frac{2.2 \text{ A}}{(2.75 \text{ x}10^4 \text{A/cm}^2)}$		
	Expected	Actual	Expected	Actual	Expected	Actual	
100 °C			380	97	265	63	
125 °C	108	573*	79.6	43	55.5	3	
140 °C	46	121	34	32	24	1	
* not fail	led,	These	MTTF are av	veraged val	lue of three sa	amples	































































