

Binomial:  $P(X) = \binom{n}{X} (p^X) (q^{n-X})$ ;  $\mu = E(\bar{x}) = \sum xp(x) = np$ ;  $\sigma^2 = \sum (x - \mu)^2 p(x) = E(x^2) - E(p(x))$ ;  $V = E(x - \mu)^2 = E(x^2) - E^2(x)$  fixed number of independent trials with constant probability of well-defined success

Hypergeometric:  $P(X) = \frac{\binom{a}{x} \binom{b}{n-x}}{\binom{a+b}{n}}$ ;  $n := \text{trials}$ ;  $x := \text{successes}$ ;  $a := \text{total successes}$ ;  $b := \text{total failures}$ ;  
 $\mu = n \left( \frac{a}{a+b} \right)$ ;  $\sigma^2 = n \left( \frac{a}{a+b} \right) \left( 1 - \frac{a}{a+b} \right) \left( \frac{a+b-n}{a+b-1} \right)$  without replacement

Negative Binomial:  $P(x) = \binom{x+r-1}{r-1} (P)^r (1-P)^x$ ;

Continuous Distro:  $E(x) = \int xf(x)dx$ ;  $V = E(x - \mu)^2$ ;

Standard Normal:  $\mu = 0$ ;  $\sigma = 1$ ;  $z = \frac{X - \mu}{\sigma}$

Central Limit Theorem:  $z = \frac{\bar{X} - \mu}{\frac{\sigma}{\sqrt{n}}}$ : sample mean, not individual data

Confidence Interval:  $\mu = \bar{X} \pm z_{\alpha/2} \left( \frac{\sigma}{\sqrt{n}} \right)$ ; for 95%  $z_{\alpha/2} = 1.96$ ; Minimum sample size needed for interval estimate:  $n = \left( \frac{z_{\alpha/2} \sigma}{E} \right)^2$ ; If  $\sigma$  is unknown &  $n < 30$ :  $\bar{X} \pm t_{\alpha/2} \left( \frac{s}{\sqrt{n}} \right)$ ;

Is  $\sigma$  known? Yes:  $z = \frac{\bar{X} - \mu}{\frac{\sigma}{\sqrt{n}}}$ ; No: Is  $n \geq 30$ ? Yes:  $z = \frac{\bar{X} - \mu}{\frac{s}{\sqrt{n}}}$ ; No:  $t = \frac{\bar{X} - \mu}{\frac{s}{\sqrt{n}}}$

Z-proportion:  $z = \frac{\hat{p} - p}{\sqrt{pq/n}}$ ;  $\hat{p} = \frac{X}{n} = \text{sample proportion}$

Confidence Interval for a Variance:  $\frac{(n-1)s^2}{\chi^2_{right}} < \sigma^2 < \frac{(n-1)s^2}{\chi^2_{left}}$ ;  $\chi^2 = \frac{(n-1)s^2}{\sigma^2}$

Prediction Interval:  $\bar{x} \pm t_{\alpha/2}(s) \sqrt{1 + \frac{1}{n}}$

Type I ( $\alpha$ ): reject true  $H_0$ ; Type II ( $\beta$ ): accept false  $H_0$

Comparing two means:  $z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$

Comparing two proportions:  $z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$ ;  $\bar{p} = \frac{X_1 + X_2}{n_1 + n_2}$ ;  $\bar{q} = 1 - \bar{p}$

F-Test:  $F = \frac{s_1^2}{s_2^2}$

Hypothesis Testing:  $p > p_0 \mapsto z \geq z_{\alpha}$ ;  $p < p_0 \mapsto z \leq -z_{\alpha}$ ;  $p \neq p_0 \mapsto z \geq z_{\alpha/2} \text{ or } z \leq -z_{\alpha/2}$ ; When comparing two known variances:  $\mu_1 - \mu_2 = p = \Delta$ ;  $z = \frac{\bar{x} - \bar{y} - \Delta_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$ ;  $n_1, n_2 \geq 40$ ;

Signed Rank Test:  $Z = \frac{S_+ - n(n+1)/4}{\sqrt{n(n+1)(2n+1)/24}}$ ;

Rank Sum Test:  $Z = \frac{W - m(m+n+1)/2}{\sqrt{mn(m+n+1)/12}}$

Students are then told that this definition does not mean that an interval has a 95% chance of containing the true parameter value. The reason that this is true, is because a 95% confidence interval will either contain the true parameter value of interest or it will not (thus, the probability of containing the true value is either 1 or 0). However, you have a 95% chance of creating one that does. In other words, this is similar to saying, "you have a 50% of getting a heads in a coin toss, however, once you toss the coin, you either have a head or a tail". Thus, you have a 95% chance of creating a 95% CI for a parameter that contains the true value. However, once you've done it, your CI either covers the parameter or it doesn't