

CS 581: Theory of Computation
Fall 2009
Final exam
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This is a closed-notes, closed-book exam.

1. True or False

- (a) All terminating functions are primitive recursive.
- (b) All primitive recursive functions are terminating.
- (c) The Post Correspondence problem is undecidable.
- (d) The acceptance problem for DFAs is decidable.
- (e) The acceptance problem for PDAs is decidable.
- (f) The acceptance problem for Turing Machines is decidable.
- (g) The complement of a regular language is regular.
- (h) The complement of a context free language is context free.
- (i) The complement of a decidable language is decidable
- (j) The complement of a Turing-recognizable language is Turing-recognizable.

2. CFL construction

- (a) Construct a PDA (or CFG) accepting (or generating) the language:

$$A = \{a^i b^j c^k \mid i = j + k \vee i + j = k\}$$

- (b) Justify your construction
- (c) Illustrate your construction on the strings *aabccc* and *aaabbc*.

3. Rice's Theorem

- (a) State Rice's theorem. You may give either the version in the book (language properties) or the one presented in lecture (index sets).
- (b) Give the definition of a language property or an index set.
- (c) Prove Rice's theorem.
- (d) Give a trivial example that is decidable by Rice's theorem.
- (e) Give a non-trivial example that is undecidable by Rice's theorem.

4. Primitive Recursion

- (a) Sketch the definition of the primitive recursive functions
- (b) Argue systematically that all primitive recursive functions are Turing computable