## CS 581: Theory of Computation <br> Spring 2010 Mid-term exam <br> James Hook

This is a closed-notes, closed-book exam.

1. Defining Regular languages
(a) Show that the set of binary numbers congruent to $3 \bmod 5$ is regular by constructing a DFA.
(b) State the definition of acceptance for a DFA.
(c) Illustrate the definition of acceptance by showing that the machine accepts the string encoding the number 13 .
2. Defining Context Free Languages
(a) Show the set of strings over $\{a, b\}$ that are not palindromes is context free. (You may use either a grammar or an automaton to do this.)
(b) Justify your construction.
(c) Illustrate on the string "abaa" (which is not a palindrome and should be accepted).
3. Not Regular

Show that the language of non-palindromes is not regular. (Recommend showing infinite index.)
4. Pumping Lemma

State and prove the pumping lemma for regular languages.

