CS 581: Theory of Computation Spring 2010 Mid-term exam James Hook

This is a closed-notes, closed-book exam.

- 1. Defining Regular languages
 - (a) Show that the set of binary numbers congruent to 3 mod 5 is regular by constructing a DFA.
 - (b) State the definition of acceptance for a DFA.
 - (c) Illustrate the definition of acceptance by showing that the machine accepts the string encoding the number 13.
- 2. Defining Context Free Languages
 - (a) Show the set of strings over $\{a, b\}$ that are not palindromes is context free. (You may use either a grammar or an automaton to do this.)
 - (b) Justify your construction.
 - (c) Illustrate on the string "abaa" (which is not a palindrome and should be accepted).
- 3. Not Regular

Show that the language of non-palindromes is not regular. (Recommend showing infinite index.)

4. Pumping Lemma

State and prove the pumping lemma for regular languages.