

# Assignment 4

Due: October 27th

**Problem 1** Give CFGs that generate the following languages:

- a)  $A = \{w \mid w \text{ starts and ends with the same symbol}\}$
- b)  $B = \{w \mid w \in \{0, 1\}^* \text{ is not a palindrome}\}$

**Problem 2** For the language:

$$B = \{w \in \{a, b\}^* \mid \text{The first, middle, and last character are the same}\}$$

- a) Using the pumping lemma, show that  $B$  is *not* regular.
- b) Give a CFG that generates the language  $B$ .

**Problem 3** Convert the context-free grammar for  $\{w \mid w \in \{0, 1\}^* \text{ is not a palindrome}\}$  into Chomsky normal form using the procedure from class.

**Problem 4** Prove or disprove: If  $G$  is a CFG in Chomsky normal form, then for any string  $w \in L(G)$  of length  $n \geq 1$  then exactly  $2n - 1$  steps are required for any derivation of  $w$ .