## CS 311: Computational Structures Exercise 3

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Let A be the langauge of binary numbers congruent to two modulo three. Let M be the three state DFA recognizing A. (This was assigned as homework in PS 1 and was used in the lecture notes to illustrate the GNFA construction.)

- 1. Give a string w accepted by the M that contains at least 4 symbols.
- 2. List the state sequence witnessing the acceptance of w.
- 3. Decompose w into x, y, and z such that:
  - (a) The states before and after the string y are the same, so all strings of the form  $xy^i z \in A$ .
  - (b) |y| > 0, and
  - (c)  $|xy| \le 3$
- 4. Verify that xz and xyyz are both accepted by M.