

Specific Unilateral Laplace Transform Pairs		
Signal	$x(t) = \mathcal{L}^{-1}[X(s)]$	$X(s) = \int_0^{\infty} x(t)e^{-st}dt$
Unit impulse	$\delta(t)$	$\Longleftrightarrow 1$
Unit step	$u(t) = \begin{cases} 1, & t > 0 \\ 0, & t < 0 \end{cases}$	$\Longleftrightarrow \frac{1}{s}$
Exponential	$e^{-\alpha t} u(t)$	$\Longleftrightarrow \frac{1}{s + \alpha}$
Power of t	$t^n u(t)$	$\Longleftrightarrow \frac{n!}{s^{n+1}}$
Damped power of t	$t^n e^{-\alpha t} u(t)$	$\Longleftrightarrow \frac{n!}{(s + \alpha)^{n+1}}$
Sine	$\sin(\beta t) u(t)$	$\Longleftrightarrow \frac{\beta}{s^2 + \beta^2}$
Cosine	$\cos(\beta t) u(t)$	$\Longleftrightarrow \frac{s}{s^2 + \beta^2}$
Damped sine	$e^{-\alpha t} \sin(\beta t) u(t)$	$\Longleftrightarrow \frac{\beta}{(s + \alpha)^2 + \beta^2}$
Damped cosine	$e^{-\alpha t} \cos(\beta t) u(t)$	$\Longleftrightarrow \frac{s + \alpha}{(s + \alpha)^2 + \beta^2}$
t times damped sine	$t e^{-\alpha t} \sin(\beta t) u(t)$	$\Longleftrightarrow \frac{2\beta(s + \alpha)}{((s + \alpha)^2 + \beta^2)^2}$
t times damped cosine	$t e^{-\alpha t} \cos(\beta t) u(t)$	$\Longleftrightarrow \frac{(s + \alpha)^2 - \beta^2}{((s + \alpha)^2 + \beta^2)^2}$

$$2^{\text{nd}} \text{ order step} \quad 1 - \frac{e^{-\zeta \omega_n t}}{\sqrt{1 - \zeta^2}} \sin(\omega_n \sqrt{1 - \zeta^2} t + \phi) \quad \Longleftrightarrow \quad \frac{\omega_n^2}{s(s^2 + 2\zeta \omega_n s + \omega_n^2)}$$

$$\phi = \cos^{-1} \zeta$$

Unilateral Laplace Transform Properties		
Property	$x(t) = \mathcal{L}^{-1}[X(s)]$	$X(s) = \int_0^{\infty} x(t)e^{-st}dt$
Linearity	$Ax_1(t) + Bx_2(t)$	$\Longleftrightarrow AX_1(s) + BX_2(s)$
Scale change	$x(at)$	$\Longleftrightarrow \frac{1}{a} X\left(\frac{s}{a}\right), a > 0$
Time shift	$x(t - T) u(t - T)$	$\Longleftrightarrow e^{-sT} X(s), T > 0$
frequency shift	$e^{-\alpha t} x(t)$	$\Longleftrightarrow X(s + \alpha)$
Differentiation*	$\frac{dx(t)}{dt}$	$\Longleftrightarrow sX(s) - x(0^-)$
Times t	$t x(t)$	$\Longleftrightarrow \frac{-dX(s)}{ds}$
Integration	$\int_0^t x(\tau) d\tau$	$\Longleftrightarrow \frac{X(s)}{s}$
Convolution	$\int_0^t x_1(\tau) x_2(t - \tau) d\tau$	$\Longleftrightarrow X_1(s) X_2(s)$
Conjugation	$x^*(t)$	$\Longleftrightarrow X^*(s^*)$
Initial value (if it exists)	$x(0^+)$	$\Longleftrightarrow \lim_{s \rightarrow \infty} sX(s)$
Final value (if it exists)	$x(\infty)$	$\Longleftrightarrow \lim_{s \rightarrow 0} sX(s)$

$$^* \quad x''(t) = \frac{d^2 x(t)}{dt^2} = s^2 X(s) - sx(0) - x'(0)$$