

1. A watershed receives 1000 mm/yr precipitation and has an evapotranspiration rate of 600 mm/yr. If the watershed covers 10 ha, what is the total net input of water to the watershed in m³/y?

ANS: Net Input = P - ET = (1000 - 600) mm/y = 400 mm/y

Total Volumetric Input = (400 mm/y) $\left(\frac{1 \text{ m}}{1000 \text{ mm}}\right)$ (10 ha) $\left(\frac{10^4 \text{ m}^2}{1 \text{ ha}}\right)$
Net Input Rate Area
 = $4 \times 10^4 \text{ m}^3/\text{y}$ ANS

2. In the watershed above what is the heat loss associated with evaporation in units of W/m²?

ANS. ET = 600 mm/y

In class we noted: 1 mm/y = $\frac{1 \text{ kg-H}_2\text{O}}{\text{m}^2 \cdot \text{yr}}$

(Because $\frac{1 \text{ mm/y}}{1 \text{ m}^2 \text{ AREA}} = 10^{-3} \text{ m}^3/\text{m}^2 \cdot \text{y} \rightarrow \left(\frac{1 \text{ L}}{\text{m}^2 \cdot \text{yr}}\right) \left(\frac{1 \text{ kg}}{\text{L}}\right) = 1 \text{ kg/m}^2 \cdot \text{y}$)

∴ ET Heat loss

[Evap Mass Flux, kg/m²·y] [Latent Heat Vaporization J/kg]

H_L = 2400 J/g near 20°C → H_L = 2.4 × 10⁶ J/kg

$\Phi_{\text{evap}} = (600 \text{ mm/y}) \left(\frac{1 \text{ kg/m}^2 \cdot \text{y}}{1 \text{ mm/y}}\right) (2.4 \times 10^6 \frac{\text{J}}{\text{kg}}) \left(\frac{1 \text{ day}}{86,400 \text{ s}}\right) \left(\frac{1 \text{ yr}}{365 \text{ d}}\right)$

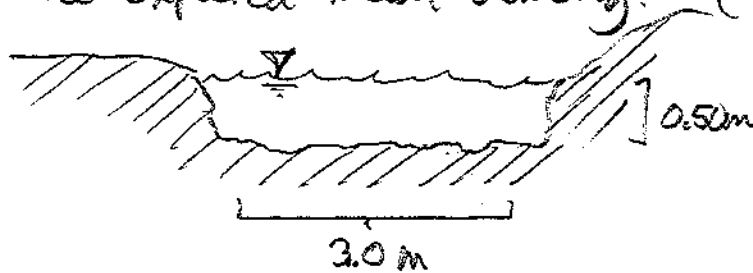
$\Phi_{\text{evap}} = 46 \text{ W/m}^2$

FROM NOTES →

3. A stream has a slope of 0.010 and a moderately rough bottom such that a Manning Coeff. of 0.040 is appropriate.

The stream is 3.0 m wide and has an average depth of 0.50 m. Assume the stream is approximately rectangular in cross section.

What is the expected mean velocity? (m/s)



ANS Use Manning's Eqn

$$v = \frac{R^{2/3} S^{1/2}}{n}$$

As noted in class
 ⇒ OMIT 1.49 factor
 if working in
 meters & $v = \text{m/s}$

$$R = \frac{A_{\text{xs}}}{P_{\text{wet}}} = \frac{(0.5 \text{ m})(3.0 \text{ m})}{2(0.5) + (3.0 \text{ m})} = 0.375 \text{ m}$$

$$v = \frac{(0.375)^{2/3} (0.01)^{1/2}}{0.040} = \boxed{1.3 \text{ m/s}}$$

4. A small pond has the following thermal properties

$$\phi_s^{\text{in}} = -300 \text{ W/m}^2$$

$$\phi_e^{\text{out}} = +360 \text{ W/m}^2$$

$$\phi_e^{\text{in}} = -200 \text{ W/m}^2$$

The temperature of the
 lake is steady
 (steady state).

Evaporation = 2.0 mm/day

What is the heat flux to/from the lake (ϕ_c) in W/m^2

Be sure to specify if ϕ_c is "in" (-) or "out" (+).

4 cont'd

At steady state

3/

ANS

$$\phi_s + \phi_e^{in} + \phi_e^{out} + \phi_{evap} + \phi_c = 0$$

$$\therefore \phi_c = \phi_s - \phi_e^{in} - \phi_e^{out} - \phi_{evap}$$

$$\text{Find } \phi_c = [\text{Evap Rate}] H_L$$

$$= \left[2.0 \frac{\text{kg}}{\text{m}^2 \cdot \text{d}} \right] \left(2400 \text{ kJ/kg} \left(\frac{10^3 \text{ J}}{\text{kg}} \right) \left(\frac{1 \text{ d}}{86,400 \text{ s}} \right) \right) = 56 \frac{\text{W}}{\text{m}^2}$$

$$\phi_c = (-300) + (-200) + (+360) + (+56) \text{ [W/m}^2\text{]}$$

$$\phi_c = \boxed{84 \text{ W/m}^2}$$

5. In problem 4 ϕ_e^{out} is $+360 \text{ W/m}^2$

What is the temperature of the lake? ($^{\circ}\text{C}$)

$$\text{ANS: } \phi_e^{out} = \sigma T^4 \quad (\epsilon \approx 1.0 \text{ for H}_2\text{O})$$

$$T = \left(\frac{360 \text{ W/m}^2}{5.7 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4}} \right)^{0.25} = 282 \text{ K}$$

$$\boxed{T = 9^{\circ}\text{C}}$$

Sounds reasonable ($\sim 48^{\circ}\text{F}$)

6. At Fred Meyer, potting soil bags are sold by volume (not weight). A large bag is 2.0 cu. feet. You are curious about the weight you bought & find the bag weighs 65 kg. What is the bulk density (ρ_B) of the potting soil? (Loose soil _{in bag})

$$V = (2.0 \text{ cu. ft}) (0.0283 \text{ m}^3/\text{ft}^3) = 0.057 \text{ m}^3$$

$$= 57 \text{ L}$$

$$\rho_B = \frac{M_s}{V_T} = \frac{65 \text{ kg}}{57 \text{ L}} = \boxed{1.14 \frac{\text{kg}}{\text{L}}} \quad \left(\text{Low for real soil} \right. \\ \left. \text{but this is bagged} \right)$$