

I.

CHAPTER 1

Mass and Energy Transfer

-
- 1.1 INTRODUCTION
 - 1.2 UNITS OF MEASUREMENT
 - 1.3 MATERIALS BALANCE
 - 1.4 ENERGY FUNDAMENTALS
-
- PROBLEMS
-

When you can measure what you are speaking about, and express it in numbers, you know something about it; but when you cannot measure it, when you cannot express it in numbers, your knowledge is of a meagre and unsatisfactory kind; it may be the beginning of knowledge, but you have scarcely, in your thoughts, advanced to the stage of science.

—William Thomson,
Lord Kelvin (1891)

1.1 INTRODUCTION

While most of the chapters in this book focus on specific environmental problems, such as pollution in surface waters or degradation of air quality, there are a number of important concepts that find application throughout the study of environmental engineering and science.

This chapter begins with a section on units of measurement. Engineers need to be familiar with both the American units of feet, pounds, hours, and degrees Fahrenheit as well as the more recommended International System of units. Both are used in the practice of environmental engineering and both will be used throughout this book.

Next, two fundamental topics, which should be familiar from the study of elementary physics, are presented: the *law of conservation of mass* and the *law of conservation of energy*. These laws tell us that within any environmental system we theoretically should be able to account for the flow of energy and materials into, and out of, that system. The law of conservation of mass, besides giving us an important tool for quantitatively tracking pollutants as they disperse in the environment, reminds us that pollutants have to go somewhere, and that we should be wary of approaches that merely transport them from one medium to another.

In a similar way, the law of conservation of energy is also an essential accounting tool with special environmental implications. When coupled with other thermodynamic

principles, it will be useful in a number of applications, including the study of global climate change, thermal pollution, and the dispersion of air pollutants.

1.2 UNITS OF MEASUREMENT

In the United States, environmental quantities are measured and reported in both the *U.S. Customary System (USCS)* and the *International System of Units (SI)* and so it is important to be familiar with both. In this book, preference is given to SI units, though the American system will be used in some circumstances. Table 1.1 gives conversion factors between the SI and USCS systems for some of the most basic units that will be encountered. A more extensive table of conversions is given in the appendix at the end of the book.

In the study of environmental engineering, it is quite common to encounter both extremely large quantities and extremely small ones. The concentration of some toxic substance may be measured in parts per billion (ppb), for example, while a country's rate of energy use may be measured in thousands of billions of watts (terawatts). To describe quantities that may take on such extreme values, it is useful to have a system of prefixes that accompany the units. Some of the most important prefixes are presented in Table 1.2.

Quite often, it is the concentration of some substance in air or water that is of interest. In either medium, concentrations may be based on mass, volume, or a combination of the two, which can lead to some confusion.

Liquids

Concentrations of substances dissolved in water are usually expressed in terms of mass of substance per unit volume of mixture. Most often the units are milligrams (mg) or micrograms (μg) of substance per liter (L) of mixture. At times they may be expressed in grams per cubic meter (g/m^3).

Alternatively, concentrations in liquids are expressed as mass of substance per mass of mixture, with the most common units being parts per million (ppm), or parts

TABLE 1.1 Some Basic Units and Conversion Factors^a

Quantity	SI Units	SI Symbol	Conversion Factor = USCS Units	
Length	Meter	m	3.2808	ft
Mass	Kilogram	kg	2.2046	lb
Temperature	Celsius	$^{\circ}\text{C}$	$1.8 (^{\circ}\text{C}) + 32$	$^{\circ}\text{F}$
Area	Square meter	m^2	10.7639	ft^2
Volume	Cubic meter	m^3	35.3147	ft^3
Energy	Kilojoule	kJ	0.9478	Btu
Power	Watt	W	3.4121	Btu/hr
Velocity	Meter/sec	m/s	2.2369	mi/hr
Flow rate	Meter ³ /sec	m^3/s	35.3147	ft^3/s
Density	Kilogram/meter ³	kg/m^3	0.06243	lb/ft^3

^aSee the appendix for a more complete list.

TABLE 1.2 Common Prefixes

Quantity	Prefix	Symbol
10 ⁻¹⁵	femto	f
10 ⁻¹²	pico	p
10 ⁻⁹	nano	n
10 ⁻⁶	micro	μ
10 ⁻³	milli	m
10 ⁻²	centi	c
10 ⁻¹	deci	d
10	deka	da
10 ²	hecto	h
10 ³	kilo	k
10 ⁶	mega	M
10 ⁹	giga	G
10 ¹²	tera	T
10 ¹⁵	peta	P
10 ¹⁸	exa	E
10 ²¹	zetta	Z
10 ²⁴	yotta	Y

per billion (ppb). To help put these units in perspective, 1 ppm is about the same as 1 drop of vermouth added to 15 gallons of gin, while 1 ppb is about the same as one drop of pollutant in a fairly large (70 m³) backyard swimming pool. Since most concentrations of pollutants are very small, 1 L of mixture has a mass that is essentially 1000 g, so for all practical purposes we can write

$$1 \text{ mg/L} = 1 \text{ g/m}^3 = 1 \text{ ppm (by weight)} \quad (1.1)$$

$$1 \text{ } \mu\text{g/L} = 1 \text{ mg/m}^3 = 1 \text{ ppb (by weight)} \quad (1.2)$$

In unusual circumstances, the concentration of liquid wastes may be so high that the specific gravity of the mixture is affected, in which case a correction to (1.1) and (1.2) may be required:

$$\text{mg/L} = \text{ppm (by weight)} \times \text{specific gravity of mixture} \quad (1.3)$$

Gases

For most air pollution work, it is customary to express pollutant concentrations in volumetric terms. For example, the concentration of a gaseous pollutant in parts per million is the volume of pollutant per million volumes of the air mixture:

$$\frac{1 \text{ volume of gaseous pollutant}}{10^6 \text{ volumes of air}} = 1 \text{ ppm (by volume)} = 1 \text{ ppmv} \quad (1.4)$$

To help remind us that this fraction is based on volume, it is common to add a "v" to the ppm; giving ppmv, as suggested in (1.4).

At times, concentrations are expressed as mass per unit volume, such as μg/m³ or mg/m³. The relationship between ppmv and mg/m³ depends on the pressure,

temperature, and molecular weight of the pollutant. The ideal gas law helps us establish that relationship:

$$PV = nRt \quad (1.5)$$

where

P = absolute pressure (atm)

V = volume (m^3)

n = mass (mol)

R = ideal gas constant = $0.082056 \text{ L} \cdot \text{atm} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$

T = absolute temperature (K)

The mass in (1.5) is expressed as moles of gas. Recall from chemistry that one mole of any gas has Avogadro's number of molecules in it (6.02×10^{23} molecules/mol) and has a mass equal to its molecular weight. Also note the temperature is expressed in kelvins (K), where

$$K = ^\circ\text{C} + 273.15 \quad (1.6)$$

There are a number of ways to express pressure; in (1.5) we have used atmospheres. One atmosphere of pressure equals 101.325 kPa (Pa is the abbreviation for Pascals). One atmosphere is also equal to 14.7 pounds per square inch (psi), so 1 psi = 6.89 kPa. Finally, 100 kPa is called a bar and 100 Pa is a millibar, which is the unit of pressure often used in meteorology.

EXAMPLE 1.1 Volume of an Ideal Gas

Find the volume that 1 mol of an ideal gas would occupy at standard temperature and pressure (STP) conditions of 1 atm of pressure and 0°C temperature. Repeat the calculation for 1 atm and 25°C .

Solution Using (1.5) at a temperature of 0°C (273.15 K) gives

$$V = \frac{1 \text{ mol} \times 0.082056 \text{ L} \cdot \text{atm} \cdot \text{K}^{-1} \cdot \text{mol}^{-1} \times 273.15 \text{ K}}{1 \text{ atm}} = 22.414 \text{ L}$$

and at 25°C (298.15 K)

$$V = \frac{1 \text{ mol} \times 0.082056 \text{ L} \cdot \text{atm} \cdot \text{K}^{-1} \cdot \text{mol}^{-1} \times 298.15 \text{ K}}{1 \text{ atm}} = 24.465 \text{ L} \quad \blacksquare$$

From Example 1.1, 1 mol of an ideal gas at 0°C and 1 atm occupies a volume of 22.414 L ($22.414 \times 10^{-3} \text{ m}^3$). Thus we can write

$$\text{mg}/\text{m}^3 = \text{ppm} \times \frac{1 \text{ m}^3 \text{ pollutant}/10^6 \text{ m}^3 \text{ air}}{\text{ppm}} \times \frac{\text{mol wt (g/mol)}}{22.414 \times 10^{-3} \text{ m}^3/\text{mol}} \times 10^3 \text{ mg/g}$$

or, more simply,

$$\text{mg}/\text{m}^3 = \frac{\text{ppm} \times \text{mol wt}}{22.414} \quad (\text{at } 0^\circ\text{C and 1 atm}) \quad (1.7)$$

Similarly, at 25 °C and 1 atm, which are the conditions that are assumed when air quality standards are specified in the United States,

$$\text{mg/m}^3 = \frac{\text{ppm} \times \text{mol wt}}{24.465} \quad (\text{at } 25^\circ\text{C and } 1 \text{ atm}) \quad (1.8)$$

In general, the conversion from ppm to mg/m^3 is given by

$$\text{mg/m}^3 = \frac{\text{ppm} \times \text{mol wt}}{22.414} \times \frac{273.15 \text{ K}}{T(\text{K})} \times \frac{P(\text{atm})}{1 \text{ atm}} \quad (1.9)$$

EXAMPLE 1.2 Converting ppm to $\mu\text{g/m}^3$

The federal Air Quality Standard for carbon monoxide (based on an 8-hour measurement) is 9.0 ppm. Express this standard as a percent by volume as well as in mg/m^3 at 1 atm and 25 °C.

Solution Within a million volumes of this air there are 9.0 volumes of CO, no matter what the temperature or pressure (this is the advantage of the ppm units). Hence, the percentage by volume is simply

$$\text{percent CO} = \frac{9.0}{1 \times 10^6} \times 100 = 0.0009 \text{ percent}$$

To find the concentration in mg/m^3 , we need the molecular weight of CO, which is 28 (the atomic weights of C and O are 12 and 16, respectively). Using (1.8) gives

$$\text{CO} = \frac{9.0 \times 28}{24.465} = 10.3 \text{ mg/m}^3$$

Actually, it is usually rounded and listed as 10 mg/m^3 . ■

The fact that 1 mol of every ideal gas occupies the same volume (under the same temperature and pressure condition) provides several other interpretations of volumetric concentrations expressed as ppmv. For example, 1 ppmv is one volume of pollutant per million volumes of air, which is equivalent to saying 1 mol of pollutant per million moles of air. Similarly, since each mole contains the same number of molecules, 1 ppmv also corresponds to 1 molecule of pollutant per million molecules of air.

$$1 \text{ ppmv} = \frac{1 \text{ mol of pollutant}}{10^6 \text{ mol of air}} = \frac{1 \text{ molecule of pollutant}}{10^6 \text{ molecules of air}} \quad (1.10)$$