

# Assignment 1

CS 581

Due October 4, 2018

**Problem 1 [10 points]** For languages  $A$  and  $B$ , let the **perfect shuffle** of  $A$  and  $B$  be the language:

$$\{w \mid w = a_1b_1a_2b_2\dots a_kb_k, \text{ where } a_1\dots a_k \in A \text{ and } b_1\dots b_k \in B, \text{ each } a_i, b_i \in \Sigma\}$$

Show that the class of Regular languages is closed under **perfect shuffle**.

**Problem 2 [10 points]** For languages  $A$  and  $B$ , let the **shuffle** of  $A$  and  $B$  be the language:

$$\{w \mid w = a_1b_1a_2b_2\dots a_kb_k, \text{ where } a_1\dots a_k \in A \text{ and } b_1\dots b_k \in B, \text{ each } a_i, b_i \in \Sigma^*\}$$

Show that the class of Regular languages is closed under **shuffle**.

**Problem 3 [10 points]** For any string  $w$ , define

$$SCRAMBLE(w) = \{t \mid t \text{ contains the same symbols as } w \text{ in any order}\}$$

For any language  $L$ , define

$$SCRAMBLE(L) = \{t \mid t \in SCRAMBLE(w) \text{ for some } w \in L\}$$

Prove or disprove that if  $L$  is a Regular language and  $\Sigma = \{0, 1\}$  then  $SCRAMBLE(L)$  is Regular.