Assignment 5

CS 311, Fall 2015 Due: December 2, 2014

Problem 1 Use a reduction to show that the language ALL_{TM} is undecidable

$$ALL_{TM} = \{\langle M \rangle \mid \text{ where } M \text{ is a TM and } L(M) = \Sigma * \}$$

[10 points]

Problem 2 A useless state in a Turing machine is one that is never entered on any input string. Consider the problem of determining whether a Turing Machine has any useless states. Formulate this problem as a language and show that it is undecidable. [10 points]

Problem 3 If $A \leq_m B$ and B is a regular language, does this imply that A is a regular language? Why or why not? [10 points]

Problem 4 Prove that the language

$$LOOP_{TM} = \{\langle M \rangle \mid M \text{ is a TM and } M \text{ loops on all inputs}\}$$

is not recognizable. [10 points]

Problem 5 Prove that the 3-SAT problem discussed in class is an element of NP by giving a verifier and a NTM decider that run in poly-time. (Only one of these is required for a proof, but I'd like both for this question.) [10 points]