Goals of the course:
- Learn fundamental structure of programming languages.
- Understand key issues in language design and implementation.
- Be aware of the range of available languages and their uses.
- Learn how to learn a new language.
- Get a small taste of programming language theory.

Method of the course:
- Fairly conventional survey textbook, with broad coverage of languages.
- Homework exercises involve programming problems in real languages.
- Most homework problems will involve modifying implementations of “toy” languages that illustrate key features and issues.
- Exercises will use two modern languages: Java and Standard ML.
- Between them, these languages illustrate most of the important concepts in current language designs.

Non-goals
- Teaching how to program.
- Teaching how to write programs in any particular language(s).
- Surveying/cataloging the features of lots of different languages.
- Comprehensive coverage of programming paradigms (e.g., will skip logic and concurrent programming material).
- Will mostly be concerned with interpreting abstract syntax for the toy languages, and will spend very little time on parsing and code generation. (Not a compiler course!)

Some Languages
What languages do you know?
FORTRAN, COBOL, (Visual) BASIC, ALGOL-60, ALGOL-68, PL/I, C, C++, RPG, Pascal, Modula, Oberon, Lisp, Scheme, ML, Haskell, Ada, Prolog, Goedel, Curry, Snobol, ICON, . . .

Don’t forget things like:
scripting languages: perl, tcl, Python, . . .
SQL, other database query languages.
spreadsheet expression languages
text processing languages, tex, awk, etc.
application-specific languages.
“Higher-Level” Programming Languages

Consider a simple (dumb) algorithm for testing primality.

In Java:

```java
public static boolean isprime (int n) {
    // return true if n has no
    // divisor in interval [2,n-1]
    for (int d = 2; d < n; d++)
        if (n % d == 0)
            return false;
    return true;
}
```

In Standard ML (using a recursive function):

```ml
fun isprime (n:int) : bool =
    (* return true if n has no
     * divisor in interval [2,n-1] *)
    let
        fun no_divisor (d:int) : bool =
            (* return true if n has no
             * divisor in interval [d,n-1] *)
            (d >= n) orelse
            ((n mod d <> 0) andalso
             (no_divisor (d+1)))
        in
            no_divisor 2
        end
```

In Intel X86 assembler:

```assembly
.globl isprime
isprime:
    pushl %ebp ; set up procedure entry
    movl %esp,%ebp
    pushl %esi
    pushl %ebx
    movl 8(%ebp),%ebx ; fetch arg n from stack
    movl $2,%esi ; set divisor d := 2
    cmpl %ebx,%esi ; compare n,d
    jge true ; jump if d >= n
    loop: movl %ebx,%eax ; set n into ....
        cdtd ; ... dividend register
        idivl %esi ; divide by d
        testl %edx,%edx ; remainder 0?
        jne next ; jump if remainder non-0
        xorl %eax,%eax ; set ret value := false(0)
        jmp done
    next: incl %esi ; increment d
        cmpl %ebx,%esi ; compare n,d
        jl loop ; jump if d < n
    true: movl $1,%eax ; set ret value := true(1)
    done: leal -8(%ebp),%esp ; clean up and exit
    popl %ebx
    popl %esi
    leave
    ret
```
Example

Here’s the instruction set for a very simple stack machine:

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Stack Before</th>
<th>Stack After</th>
</tr>
</thead>
<tbody>
<tr>
<td>CONST i</td>
<td>s1 ... sn</td>
<td>i s1 ... sn</td>
</tr>
<tr>
<td>LOAD x</td>
<td>s1 ... sn</td>
<td>Vars[x] s1 ... sn</td>
</tr>
<tr>
<td>STORE x</td>
<td>s1 ... sn</td>
<td>s2 ... sn</td>
</tr>
<tr>
<td>PLUS</td>
<td>s1 s2 s3 ... sn</td>
<td>(s1+s2) s3 ... sn</td>
</tr>
<tr>
<td>MINUS</td>
<td>s1 s2 s3 ... sn</td>
<td>(s2-s1) s3 ... sn</td>
</tr>
</tbody>
</table>

Note that STORE x also sets Vars[x] = s1.

And here’s a stack machine program corresponding to the simple statement $c = 3 - a + (b - 7)$:

```
CONST 3
LOAD a
MINUS
LOAD b
CONST 7
MINUS
PLUS
STORE c
```

Is this code sequence unique?

This illustrates the expressiveness of high-level expressions compared to machine code.

C

- Procedural imperative language.
- Widely used for systems programming, especially for Unix, Linux.
- First language to be implemented on almost any new machine.
- Influential expression-oriented syntax.
- Supports “bit-twiddling” low-level manipulation.
- Generates efficient, predictable machine code.
- Weak type system; run-time crashes common.
- Weak structuring mechanisms.
- C++ greatly extends C, but is almost completely backwards-compatible.

Java

- Object-oriented imperative language.
- Hyped for “web programming.”
- Designed as a “better C++.”
- Core language largely derived from C, C++.
- Strong static type checking.
- Classes serve as primary structuring mechanism.
- Automatic heap allocation and garbage collection.
- Extensive libraries.
- Portable interpretive environment (JVM) based on stack abstract machine.

Standard ML

- Mostly functional language.
- Designed for symbolic manipulation; inherits from Lisp, Scheme.
- Strong, static type inference.
- Simple, uniform, powerful recursive datatype mechanism.
- Recursion is primary control structure.
- Powerful parameterized module mechanism.
- Automatic heap allocation and garbage collection.
- Top-level “read-eval-print” loop for development.
Language Description and Documentation
For programmers, compiler-writers, and students . . .

Syntax (Easy)
- Grammars; BNF and Syntax Charts

Semantics (Hard)
- Informal
- Formal: Operational, Denotational, Axiomatic

Learning about a Language
- Reference Manuals
- User Guides
- Texts and tutorials

Grammars
- Used for description, parsing, analysis, etc.
- Based on recursive definition of program structure.
- Rich theory with connections to automatic parser generation, push-down automata, etc.
- Many possible representations, including BNF (Backus-Naur Form), EBNF (Extended BNF), syntax charts, etc.

Simple Example Grammar
Character set: \{ (, ) \}
Terminals: \{ (, ) \}
Nonterminals: \{ S \}
Productions:
\[
S ::= (S) \\
S ::= SS \\
S ::= \epsilon \quad \text{(the empty string)}
\]
Starting nonterminal: \( S \)
Sample derivation:
\[
S \rightarrow (S) \rightarrow (SS) \rightarrow (S)S \rightarrow (SS) \rightarrow ((SS)) \rightarrow (((SS)))
\]
This grammar generates the language of strings of properly matched parentheses.
It is often useful to think of a derivation as a tree (more shortly).

Grammars, Formally
A (context-free) Grammar over a given character set consists of
- A set of terminals, which are strings of zero or more characters.
- A set of nonterminals, which are variables representing a set of terminals.
- A set of productions, each of which has a left side consisting of a single nonterminal and a right side consisting of zero or more terminals or nonterminals.
- A distinguished starting nonterminal.
We can apply a production to a string by replacing some instance of the left side nonterminal by the right side.
The context-free language \( L(G) \) generated by a grammar \( G \) is the set of character strings that can be derived from the starting nonterminal by applying productions—in any order—until no nonterminals remain.
Note: Here we are using “language” in the technical sense meaning “a well-defined set of strings over the specified character set”.

Grammars
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- Based on recursive definition of program structure.
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- Many possible representations, including BNF (Backus-Naur Form), EBNF (Extended BNF), syntax charts, etc.
BNF

BNF was invented ca. 1960 and used in the formal description of Algol-60. It is just a particular notation for grammars, in which

- Nonterminals are represented by names inside angle brackets, e.g., `<program>`, `<expression>`, `<S>`.
- Terminals are represented by themselves, e.g., WHILE, (. 3. The empty string is written as `<empty>`.

**BNF Example**

```plaintext
<program> ::= BEGIN <statement-seq> END
<statement-seq> ::= <statement> <statement-seq>
<statement> ::= <while-statement> <for-statement> <empty>
<while-statement> ::= WHILE <expression> DO <statement-seq> END
<Expression> ::= Factor { (AND | OR) Factor }
Factor ::= '(' <expression> ')' | Variable
For-statement ::= ...
Variable ::= ...
```

EBNF

EBNF is (any) extension of BNF, usually with these features:

- A vertical bar, |, represents a choice,
- Parentheses, ( and ), represent grouping,
- Square brackets, [ and ], represent an optional construct,
- Curly braces, { and }, represent zero or more repetitions,
- Nonterminals begin with upper-case letters.
- Non-alphabetic terminal symbols are quoted, at least when necessary to avoid confusion with the meta-symbols above.

**EBNF Example**

```plaintext
Program ::= BEGIN Statement-seq END
Statement-seq ::= Statement
Statement ::= [ ';' | Statement-seq ]
While-statement ::= WHILE Expression DO Statement-seq END
Expression ::= Factor { (AND | OR) Factor }
Factor ::= '(' <expression> ')' | Variable
For-statement ::= ...
Variable ::= ...
```

Syntax Analysis (Parsing)

Parser recognizes syntactically legal programs (as defined by a grammar) and rejects illegal ones.

- Successful parse also captures hierarchical structure of programs (expressions, blocks, etc.).
- Convenient representation for further semantic checking (e.g., typechecking) and for code generation.
- Failed parse provides error feedback to the user indicating where and why the input was illegal.

Any context-free language can be parsed by a computer program, but only some can be parsed efficiently. Modern programming languages can usually be parsed efficiently.

Programming language grammars usually take simple tokens rather than characters as terminals. Converting raw program text into token stream is job of the lexical analyzer, which

- Detects and identifies keywords and identifiers.
- Converts multi-character symbols into single tokens.
- Handles numeric and string literals.
- Removes whitespace and comments.

Parse Trees

Graphical representation of a derivation.

Given this grammar:

```plaintext
expr → expr + expr | expr * expr | (expr) | -expr | id
```

Example tree for derivation of sentence \(- (x + y)\) :

```
expr
   / \  
-   expr
     /   
    (expr)
       /  
  expr + expr
    / |  
  id x | id y
```

Each application of a production corresponds to an internal node, labeled with a non-terminal.

Leaves are labeled with terminals, which can have attributes (in this case the specific identifier name).

The derived sentence is found by reading leaves (or “fringe”) left-to-right.
Ambiguity

A given sentence in \( L(G) \) can have more than one parse tree. Grammars \( G \) for which this is true are called ambiguous.

Example: given the grammar on the last slide, the sentence 
\[ a + b * c \]
has two parse trees:

We may think of the left tree as being the “correct” one, but nothing in the grammar says this.

To avoid the problems of ambiguity, we can:

- Rewrite grammar; or
- Use “disambiguating rules” when we implement parser for grammar.

Rewriting Arithmetic Grammars

One way to enforce precedence/associativity is to build them into the grammar using extra non-terminals, e.g.:

\[ \text{factor} \to \langle \text{expr} \rangle \mid \text{id} \]
\[ \text{term} \to \text{term} \ast \text{factor} \mid \text{term} / \text{factor} \mid \text{factor} \]
\[ \text{expr} \to \text{expr} + \text{term} \mid \text{expr} - \text{term} \mid \text{term} \]

Example: \( a \ast b - c + d \ast e \)

Limitations of Context-free Grammars

Context-free grammars are very useful for describing the structure of programming languages and identifying legal programs.

But there are many useful characteristics of legal programs that cannot be captured in a grammar (no matter how clever we are).

For example, in many programming languages, every variable in a legal program must be declared before it is used. But this property cannot be captured in a grammar.

To show this formally, we can abstract the notion of “declaration before use” into a formal language
\[ L = \{ wcw \mid w \in (a \mid b)^* \} \]

It can be easily shown that no context-free grammar generates \( L \).

So checking legality of programs typically requires more than syntax analysis. Most compilers use a secondary “semantic” analysis phase to check non-syntactic properties, such as type-correctness. Of course, sometimes illegal programs cannot be detected until runtime.
Parse Trees vs. Abstract Syntax Trees

Parse trees reflect details of the concrete syntax of a program, which is typically designed for easy parsing. For processing a language, we usually want a simpler, more abstract view of the program. (No firm rules about AST design: matter of taste, convenience.)

Simple concrete grammar:

\[
S \rightarrow \text{ 'while' '(' } E \text{ ')' 'do' } S \mid \text{ 'ID' '=' } E \text{ } \\
E \rightarrow E \text{ '+' } T \mid E \text{ '-' } T \mid T \text{ } \\
T \rightarrow \text{ 'ID' } \mid \text{ 'NUM' } \mid \text{ ' (' } E \text{ ')' }
\]

Example concrete parse tree for

\[
\text{while (n) do n = n - (b + 1)}
\]

Abstract Syntax Captures the Essence

Concrete syntax is important for usability, but fundamentally superficial. The same abstract syntax can be used to represent many different concrete syntaxes.

Examples:

- C-like:
  
  \[
  \text{while (n) do n = n - (b + 1)}
  \]

- Fortran-like:
  
  \[
  \text{do while(n .NE. 0)} \text{ } \\
  \text{n = n - (b + 1)} \text{ } \\
  \text{end do}
  \]

- COBOL-like:
  
  \[
  \text{PERFORM 100-LOOP-BODY} \text{ } \\
  \text{WITH TEST BEFORE} \text{ } \\
  \text{WHILE N IS NOT EQUAL TO 0} \text{ } \\
  \text{100_LOOP-BODY.} \text{ } \\
  \text{ADD B TO 1 GIVING T} \text{ } \\
  \text{SUBTRACT T FROM N GIVING N}
  \]

  - Use Chinese keywords in place of while and do.
  - Use a graphical notation.

Internal Representation of ASTs in C

AST’s have recursive structure and irregular shape and size, so it makes sense to store them as heap data structures using one record for each tree node.

In C, Pascal, Ada, etc., we might use unions or variant records for the different node labels of each node kind. E.g., in C:

```
struct stmt {
    enum { While, Assgn, ... } label;
    union {
        struct {
            struct exp *test;
            struct stmt *body;
        } while_s;
        struct {
            char *lhs; struct exp *rhs;
        } assgn_s;
        ...
    } u;
}

struct exp {
    enum { Add, ..., Num } label;
    union {
        struct {
            struct exp *left; struct exp *right;
        } add_e;
        ...
    } u;
}
```
AST’s in Java or ML

In Java, heap records are objects. We define classes corresponding to the various kinds and a subclass for each label, e.g.

```java
abstract class Stmt {
}
class While extends Stmt {
    Exp test;
    Stmt body;
}
class Assign extends Stmt {
    String lhs; Exp rhs;
}
...
abstract class Exp {
}
class Add extends Exp {
    Exp left; Exp right;
}
...
class Num extends Exp {
    int value;
}
```

In ML, we can use datatypes to define a suitable set of variants.

```ml
datatype stmt = While of exp * stmt
| Assign of string * exp
| ...
and exp = Add of exp * exp
| ...
| Num of int
```

Heap Structure

All these approaches generate roughly the same heap structures, e.g. for

```plaintext
while (n) do n = n - (b + 1)
```

```
  stmt
  ------------
  | Stmt
  | ----- stmt
  | |
  | Exp
  | |
  | ID
  | n
  |
  Exp
  |
  ID
  n
  |
  Stmt
  |
  Assign
  |
  |
  Exp
  |
  ID
  n
  |
  Sub
  |
  |
  Exp
  |
  ID
  n
  |
  Add
  |
  |
  Exp
  |
  ID
  b
  |
  Num
  |
  1
  |
  Exp
```

External Representation of ASTs

Although ASTs are designed as an internal program representation, it can be useful to give them an external form too that can be read or written by other programs or by humans.

Any external representation of ASTs must accurately reflect the internal tree structure as well as the “fringe” of the tree. Can’t use tree grammar to parse, since it is typically ambiguous!

One approach (deriving from the programming language LISP) is to use parenthesized prefix notation to represent trees.

Each node in the tree is represented by the expression

```
( label attr_1 ... attr_m child_1 child_n )
```

where label is the node label, the attr_i are the label’s attributes (if any), and the child_i are the labels sub-trees (if any), each of which is itself a node expression. To make things more readable, we might use abbreviations for common labels, e.g., + for Add.

So the representation of our AST example could be

```
(While (Id n)
    (Assign n (- (Id n)
        (+ (Id b)
            (Num 1)))))
```

where the indentation is optional, but makes the representation easier for humans to read.

Parsing this representation is easy!