Concepts addressed/touched in this unit:

Curry interpreter
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Defining Types
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Functional Patterns
Default Rules
List comprehensions

Curry interpreter

Functional logic programs are often executed by an interactive interpreter. Currently, a popular interpreter for Curry is Pakcs. The trace of an invocation of Pakcs follows:

```
 [antoy@localhost INTRO]$ pakcs
 some omitted lines
Type ":h" for help

Prelude>
```

The user can issue commands, such as :quit to terminate, or expressions to evaluate, such as 2+2.

```
Prelude> 2+2
Result: 4 ?
No more solutions.
Prelude> :quit
[antoy@localhost INTRO]$ 
```

The semicolon after the question mark asks for additional results. Functional computations always have one result only.

Several types and functions are available to the user in the interpreter. See the Prelude.curry file in the lib directory of the Pakcs distribution.

Predefined Types

Several types are predefined or built-in.

- **Int**: integers: \(-2,-1,0,1,2,\ldots\)
- **Bool**: booleans: `True,False`
- **Char**: characters: `'h','i','\n'
- **(α,β)**: tuples: `(1,True), ('J','Doe')`
- **List[α]**: lists: `[],1:2:[],['a','b','c']`
- **String**: strings: `"hello","word"
- **Success**: Success: no visible values
- **Unit**: Unit: `()`

Int is the only built-in numeric type in Pakcs, it has unlimited precision. See lib/CLPR for floats.

String is a synonym of List[Char].

Success is now deprecated, it may appear in old code as the type of constrains.

Unit is a type whose only value is `()`. Both α and β stand for an arbitrary type.

Tuples and lists are polymorphic.

Several common operations are available on these types. See the Prelude.curry file in the lib directory.

The programmer can define other types referred to as algebraic.

Defining Functions

The programmer can define functions in a file, say myfile.curry, and load them in the interpreter with the command :load myfile. E.g.:

```
square i = i * i
average (x,y) = (x+y) 'div' 2
swap (x,y) = (y,x)
mylen l = if l==[] then 0 else 1 + mylen (tail l)
nine = 9
```

The application of a function (symbol) to its argument(s) is denoted by juxtaposition. E.g., the function square takes one argument and returns its square.

No type declaration is necessary for the argument(s).

The argument of the function average is a pair.

The function div, integer division, is optionally used as an infix operation by enclosing it in backquotes.

The function swap is polymorphic, it swaps pairs of any types.

The if · then · else · construct has the usual meaning.

Functions can have zero arguments, see nine. They are constants.
Defining Types

User-defined types are introduced by a `data` type declaration.

```haskell
data Color = Red | Green | Blue

data MyBool = MyFalse | MyTrue

data Natural = Zero | Succ Natural

data MyList a = Nil | Cons a (MyList a)

data BinTree a
    = Leaf
    | Branch a (BinTree a) (BinTree a)
```

Functions on user-defined types (and predefined as well) are conveniently coded by `pattern matching`.

```haskell
myNot MyFalse = MyTrue
myNot MyTrue = MyFalse
leq Zero _ = True
leq (Succ n) Zero = False
leq (Succ n) (Succ m) = leq n m
lookup Leaf = False
lookup a (Branch b left right) =
    a == b || lookup a if a < b then left else right
```

The underscore symbol `_` denotes an `anonymous` variable. A variable that is not used in the result of a function.

Using Lists

`Lists` are ubiquitous for programming. Here are some simple examples of notations and techniques.

```haskell
[2..]  →  [2,3,4,...  infinite
[2..5]  →  [2,3,4,5]
[2,4..12]  →  [2,4,6,8,10,12]
[2,4..]  →  [2,4,6,...  infinite
```

The following example shows `nested` functions and `lazy evaluation`.

```haskell
fibseq = fsaux 0 1
    where fsaux x y = x : fsaux y (x+y)
fibo n = fibseq !! n
test = take 20 fibseq
```

It uses a nested function defined within a `where`. A nested function can be referenced only by the immediately nesting function and the functions in its block. The variables of the nesting functions can be referenced by the recursively nested functions.

More on Functions (1)

Functions can take other `functions` as arguments. This is a powerful feature to parameterize a computation with another computation.

```haskell
map _ [] = []
map f (x:xs) = f x : map f xs
foldr _ z [] = z
foldr f z (x:xs) = f x (foldr f z xs)
```

The following equations explain what the above functions compute. In both cases, `f` is the function parameter.

```haskell
map f [x1,x2,...,xn] = [f x1, f x2, ... f xn]
foldr f z [x1,x2,...,xn] = (x1 'f' (x2 'f' ... (xn 'f' z)...) )
```

A function can be defined by an expression, like the expression `2+3` defines a number. A function defined by an expression, referred to as `lambda abstraction`, is called `anonymous`. For example:

```haskell
sumList l = foldr (+) 0 l
maxList (x:xs) =
    foldr (\u v -> if u>v then u else v) x xs
atoi str = num
    where
digits = map (\x -> ord x - ord '0') str
num = foldl (\x y -> 10*x+y) 0 digits
```

More on Functions (2)

Functions can have optional `conditions`:

```haskell
max x y | x < y = y
         | otherwise = x
lookup _ Leaf = False
lookup a (Branch b left right) =
    a == b || lookup a if a < b then left else right
```

Case expressions are allowed in the returned value. This is somewhat equivalent the the earlier example.

```haskell
mylen l =
    case l of
        [] -> 0
        (xs) -> 1 + mylen (tail l)
```

Both conditions and cases are tested sequentially, from top to bottom. The arm of the first that succeeds is evaluated. Otherwise the evaluation fails.
More on Types

The user can optionally declare the type of a symbol and/or ask the interpreter to show the type of a symbol.

Functions take “one argument only at the time.” The type of a function that takes an argument of type \( \alpha \) and returns an argument of type \( \beta \) is \( \alpha \rightarrow \beta \).

Referring to previous examples:

```haskell
myNot :: MyBool -> MyBool
leq :: Natural -> Natural -> Bool
lookup :: Int -> BinTree Int -> Bool
```

The operator \( \rightarrow \) is right-associative which means that function `lookup` takes an `Int` and returns a function of type `BinTree Int -> Bool`. Thus, this function takes a `BinTree Int` and returns a `Bool`.

This style of function definition is called **curried**. By contrast:

```haskell
average :: (Int,Int) -> Int
```

i.e., the function `average` takes a pair of `Int` and returns an `Int`.

To get the interpreter tell you the type of a symbol, say \( s \), load the file defining \( s \) and input the command `:type s`.

Non-Determinism (1)

Function (and constants) may return more than one value. E.g., in file `sample4.curry`:

```haskell
coin = 0
coin = 1
```

The constant `coin` has two values, 0 and 1. If it appears in a computation, one of its values is chosen (don’t count on it as a random bit generator).

```haskell
sample4> coin+6
Result: 6 ? ;
Result: 7 ? ;
No more solutions.
```

```haskell
sample4> coin==coin
Result: True ? ;
Result: False ?
```

**Non-deterministic** computations are convenient when the programmer does not have a better algorithm for making a choice, e.g., which move to make in a puzzle. Or when the programmer does not want to put the effort and time to learn, code, and test an algorithm for making a choice.

It is intended that a non-deterministic choice is later **constrained** to filter out “bad” choices.

Non-Determinism (2)

Compute a permutation of a list. Every permutation should be produced. Use the testing properties tool to verify the code.

```haskell
import Test.Prop
perm [] = []
perm (xs++x:ys) = x : perm (xs++ys)
sample = [1,2,3,4]
-- the reverse of the input is produced
prop_1 = perm sample -> reverse sample
-- some random permutation is produced
prop_2 = perm sample -> [2,4,1,3]
-- the number of perms is the factorial
prop_3 = perm sample # 4*3*2*1
```

To understand the code, draw a diagram of input and output.

Execute with `curry check filename`.

List comprehensions

A special notation is available to transform lists. Here are some examples:

```haskell
triangNumbers = [x * (x+1) \ 'div' \ 2 | x <- [0..]]
primeNumbers = [x | x <- [2..], isPrime x]
isPrime x = and [x \ 'mod' \ y/=0 | y<-[2..x \ 'div' \ 2]]
lexPairs = [(x,y) | x <- [0..3], y <- [x..3]]
```

The part of the form `var <- list` is called a **generator**. A condition following generators is called a **guard** and it acts as a filter.

Multiple generators are allowed and lexically scoped.

```haskell
qsort :: [Int] -> [Int]
qsort [] = []
qsort (x:1) = qsort [y | y<-1, y<x] ++
x:qsort [z | z<-1, z>x]
```
Exercises (optional/proposals)

Exercise I1. Define the absolute value function.

Exercise I2. Define a function that counts how many integers in a list are even, and run it on a few test samples. Hint: the remainder function is mod (similar to div).

Exercise I3. Define a function that counts how many integers in a list are positive, and run it on a few test samples. Observe the similarities with the previous function.

Exercise I4. Define a function, say gencount, that counts how many elements in a list have a certain property. Redefine the previous functions using gencount.

Exercise I5. Define a type to represent a tree. A tree has a root and zero or more children which are trees. Most often, the root has a decoration.

Exercise I6. Build a trie from a list of words and use it to find whether a word is in a dictionary. Use the previous exercise.