Name:

If a question is wrong, or has no acceptable answer, do not mark any choice.

If a question has several correct answers, choose the most accurate/complete/informative one. On a separate sheet, write a detailed justification of your choice.

You will be graded on the accuracy and precision of this justification only.

You will get 1 point for each correct answer and 0 points for missing or incorrect answers. Your grade will be written on the back of this page.

- 1. Which of the following is a post-order traversal of the tree to the right:
 - $[-A-] \quad r \, b \, c \, d \, x \, y \, z \, w \, e \, u$
 - $[-B-] \quad r\,b\,x\,e\,c\,d\,y\,w\,u\,z$
 - $[-C-] \quad z \, c \, d \, y \, w \, u \, b \, x \, e \, r$
 - $[-D-] \quad c\,d\,b\,z\,y\,w\,x\,u\,e\,r$
- Consider again the previous tree.
 Which of the following is a pre-order traversal of the tree:
 - $[-A-] \quad r \, b \, c \, d \, x \, y \, z \, w \, e \, u$
 - $[-B-] \quad r \, b \, x \, e \, c \, d \, y \, w \, u \, z$
 - [-C-] z c d y w u b x e r
 - $[-D-] \quad c\,d\,b\,z\,y\,w\,x\,u\,e\,r$
- 3. Consider again the previous tree. The set of all the siblings of b is:
 - $\begin{array}{ll} [-\mathrm{A-}] & \{x\} \\ [-\mathrm{B-}] & \{x,e\} \\ [-\mathrm{C-}] & \{c,d\} \\ [-\mathrm{D-}] & \{\} \end{array}$
- 4. Consider again the previous tree. Its depth (also called height) is:
 - [-A-] 2 [-B-] 3 [-C-] 5 [-D-] 10
- 5. The Polish notation of the expression a + b * c + d is (where "+" is left associative):
 - $\begin{array}{ll} [-\mathrm{A-}] & + + a * b \, c \, d \\ [-\mathrm{B-}] & + a * b \, c + d \\ [-\mathrm{C-}] & + + * a \, b \, c \, d \\ [-\mathrm{D-}] & + * b \, c + a \, d \end{array}$



6. Language L consists of strings of a, b, and c with equal frequency. String s = aaaaabbbbbccccc (5 of each letter).

The length in bits of s with an optimal Huffman code is:

- [-A-] 15
- [-B-] 20
- [-C-] 25
- [-D-] 30
- 7. Consider the binary search tree to the right

If value 12 is inserted into the tree, the node holding this value will be:

- [-A-] a child of 11
- [-B-] the left child of 11
- [-C-] the right child of 11
- [-D-] not a child of 11



8. Consider again the previous tree.

If value 5 is deleted from the tree, the value of the node holding 5 is replaced by:

- [-A-] 1
- [-B-] 9
- [-C-] either 1 or 9
- [-D-] none of the above
- 9. Which traversal of a binary search tree produces a sorted sequence:
 - [-A-] Pre-order
 - [-B-] In-order
 - [-C-] Post-order
 - [-D-] Level-order

10. A binary tree is perfect is all its leaves are at the same depth. The number of leaves in a perfect binary tree of depth d is:

- $\begin{array}{ll} [-\mathrm{A-}] & d^2 \\ [-\mathrm{B-}] & 2^d \\ [-\mathrm{C-}] & 2^d 1 \\ [-\mathrm{D-}] & 2^{d+1} 1 \end{array}$
- 11. Let P be a problem with 20 outcomes.

The depth of a binary decision tree that solves P must be at least:

- [-A-] 2
- [-B-] 3
- [-C-] 4
- [-D-] 5