

If a question is wrong, or has no acceptable answer, do not mark any choice.

If a question has several correct answers, choose the most accurate/complete/informative one.

On a separate sheet, write a detailed justification of your choice.

You will be graded on the accuracy and precision of this justification only.

You will get 1 point for each correct answer and 0 points for missing or incorrect answers.

Your grade will be written on the back of this page.

1. How many iterations does Euclid *gcd* algorithm executes on input 15 and 4:

- [-A-] 1  
 [-B-] 2  
 [-C-] 3  
 [-D-] 4

2. Let  $f : \mathbb{N}_{24} \rightarrow \mathbb{N}_{24}$  be defined by  $f(n) = an + 5 \pmod{24}$  (mod 24 is intended).  
 For which value of  $a$  is  $f$  bijective.

- [-A-] 2  
 [-B-] 3  
 [-C-] 4  
 [-D-] 5

3. Let  $f : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{N}$  be defined by

$$f(0, y) = y$$

$$f(x + 1, y) = 1 + f(x, y)$$

the value of  $f(4, 4)$  is:

- [-A-] 0  
 [-B-] 4  
 [-C-] 8  
 [-D-] 12

4. Let  $f : \mathbb{N} \rightarrow \mathbb{N}$  be defined by

$$f(0) = 0$$

$$f(1) = 0$$

$$f(n + 2) = 1 + f(n)$$

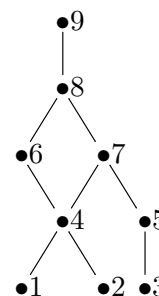
the value of  $f(7)$  is:

- [-A-] 1  
 [-B-] 3  
 [-C-] 4  
 [-D-] 7

5. Consider the Hasse diagram of the poset  $P$  to the right.

Which of the following is **not** a topological sort of  $P$ .

- [-A-] 1,2,3,4,5,6,7,8,9  
 [-B-] 1,2,4,6,7,8,9,3,5  
 [-C-] 3,2,1,5,4,7,6,8,9  
 [-D-] 3,5,1,2,4,6,7,8,9



6. Let  $f : \mathbb{N}_9 \rightarrow \mathbb{N}_9$  be defined by  $f(x) = (4x + 6) \bmod 9$ .

- [-A-]  $f$  has a fixpoint
- [-B-] 4 is a fixpoint of  $f$
- [-C-] 5 is a fixpoint of  $f$
- [-D-]  $f$  has no fixpoints

7.  $f(n) = O(g(n))$  iff there exist constants  $c$  and  $m$  such that:

- [-A-]  $|g(n)| \leq |f(n)|$ , for  $n \geq m$
- [-B-]  $|f(n)| \leq |g(n)|$ , for  $n \geq m$
- [-C-]  $|g(n)| \leq c|f(n)|$ , for  $n \geq m$
- [-D-]  $|f(n)| \leq c|g(n)|$ , for  $n \geq m$

8. if  $f(n) = O(g(n))$  then

- [-A-]  $f(n) \leq g(n)$ , for all  $n$
- [-B-]  $|f(n)| < |g(n)|$ , for all  $n$
- [-C-]  $|f(n)| \leq c|g(n)|$ , for some  $c$  and all  $n$
- [-D-] none of the above

9. Comparing rates of growth:

- [-A-]  $\log(n^2) = O(\log(n))$
- [-B-]  $\log(n^2) = O(n)$
- [-C-]  $\log(n^2) = O(n^2)$
- [-D-] All of the above

10. Let  $f : \mathbb{N}_{12} \rightarrow \mathbb{N}_{12}$  be defined by  $f(x) = (7x + 2) \bmod 12$ . The inverse, say  $g$ , of  $f$  is:

- [-A-]  $g(x) = (7x + 5) \bmod 12$
- [-B-]  $g(x) = (5x + 7) \bmod 12$
- [-C-]  $g(x) = (7x + 10) \bmod 12$
- [-D-]  $g(x) = (10x + 7) \bmod 12$

11. Which function of  $n$  is computed by *mystery*:

- [-A-]  $n^2$
- [-B-]  $2 * n + 1$
- [-C-]  $n(n - 1)/2$
- [-D-] none of the above

```
procedure mystery(n)
  r := 0
  for i := 1 to n
    r := r + 2*i - 1
  return r
end
```