

CS581 Worksheet #5

Due by midnight, Thursday, May 2, Submit via D2L

This worksheet is meant to explore the ideas behind the CFL-pumping lemma. We will not use the lemma to prove anything in this worksheet. First consider the conditions that the lemma sets out: If L is CF, then every string w in L can be written as $xu^iyv^iz \in L$

1. $uv \neq \varepsilon$ ($|uv| > 0$, which means that at least one of u or v is not empty)
2. And for every $i \geq 0$ $xu^iyv^iz \in L$

For each grammar below (where S is the start symbol) do all 6 of the following:

1. Find a string w in L . Write it down.
2. Write the string as $xuyvz$. Identify each of the substrings x, u, y, v, z of w
3. Draw a parse tree for w .
4. Draw a parse tree for xu^0yv^0z
5. Draw a parse tree for xu^2yv^2z
6. Find the smallest constant, N (i.e. 4, 7, 24, you decide) such that for every string longer than N , the grammar has a pump.

Grammar 1, over the alphabet $\{a,b,c\}$

$S \rightarrow a T X T c$
 $T \rightarrow a$
 $T \rightarrow b$
 $X \rightarrow b c$

Grammar 2, over the alphabet $\{0,1\}$

$S \rightarrow X S$
 $S \rightarrow 0$
 $X \rightarrow 1$

Grammar 3, over the alphabet $\{M,N,P,Q\}$

$S \rightarrow S M$
 $S \rightarrow X$
 $X \rightarrow N P$
 $X \rightarrow Q$