

ABSTRACT

Arkesh, Vikram Bangalore. FPGA Implementation of a Low Power Doppler Invariant BFSK Receiver (Under the guidance of Dr Paul D. Franzon)

A non coherent frequency shift keying (FSK) receiver architecture is designed potentially for low power applications. The receiver incorporates a 16 point Fast Fourier Transform (FFT) for symbol detection and can withstand large Doppler shifts. Almost all the design units of the receiver are digital designs for better power efficiency and reliability. The receiver functions on one bit data processing and supports data rates of 10kbps, 1kbps and 100bps. Co-ordinate rotation (CORDIC) algorithm is used for complex multiplications while computing FFT, evading the use of power hungry multipliers.

The design and simulation of the receiver is carried out in MATLAB/SIMULINK. The MATLAB model is translated to a XILINX FPGA hardware model using system generation features of the XILINX development system. The hardware model is synthesized to a virtex-2 XILINX FPGA and various performance parameters are extracted. A control system for symbol and timing detection is designed and modeled in VHDL, synthesized to XILINX hardware and interfaced to the receiver.

**FPGA IMPLEMENTATION OF A LOW POWER
DOPPLER INVARIANT BFSK RECEIVER**

by
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of
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DEDICATION

To my parents, Arkesh and Sudha

BIOGRAPHY

Vikram Arkesh was born in Secunderabad, India in January 1978. He graduated from Bangalore University, Bangalore, India with a Bachelor's degree in Electronics and Communication in August 2000. He worked at Robert Bosch, Bangalore, India from September 2000 to August 2001 as software engineer in the area of communication applications. In the fall of 2001, he enrolled in North Carolina State University as a graduate student to pursue M.S in Electrical Engineering. He worked on his MS thesis under the guidance of Dr Paul Franzon from May 2002 to August 2003.

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Last but not the least, I would like to thank my parents, Arkesh and Sudha and my sister, Chitra for being a constant source of inspiration and motivation for the entire tenure of my Masters course.

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Chapter 1

Introduction

Wireless communication is one of the fastest growing fields owing to its length and breadth of applications. Deep space communication is one such field where the use of wireless systems is indispensable. The most important issue in space communication is power and happens to be one of the major driving forces in the quest for low power wireless systems. We focus on the design of a low power FSK receiver intended specifically for deep space communications that involves an orbiter and a lander.

A typical set up in space explorations will involve an orbiter, orbiting a planet or a satellite and a lander which is on the planet or satellite and which is in communication with the orbiter. In such a scenario, there exists a relative displacement between the orbiter and lander. This results in Doppler shifts in the transmitted/received signal and could potentially introduce detection errors in the receiver. Hence, the receiver designed for such applications should be invariant to Doppler changes in frequency.

A receiver architecture based on frequency shift keying is proposed by Grayver [1] which uses an FFT detection scheme. The receiver can take care of Doppler shifts and has almost all digital architecture intended for low power applications. We explore this architecture for the FSK receiver design. The FFT computation in the receiver involves non trivial complex multiplications suggesting the need to use power consuming multipliers. The FFT algorithm proposed by Bertazonni [2] uses co-ordinate rotation algorithm (CORDIC) in place of complex multiplications. CORDIC algorithm works on the principle of rotating the complex phasors instead of multiplying them and uses adders/shifters. We explore a CORDIC approach for FFT computation to improve power efficiency.

The receiver is designed and modeled in MATLAB and SIMULINK. We simulate the receiver and test it for data rates of 10kbps, 1kbps and 100bps. We design an FSK transmitter and introduce additive white Gaussian noise and Doppler shifts in the transmitted signal and test the receiver for such conditions.

We port the SIMULINK model to a XILINX hardware model using the system generation features and block sets of SIMULINK. The block set contains various building blocks for digital signal processing, communication and math operations. We simulate the XILINX model in SIMULINK and synthesize the model to a VIRTEX-2 FPGA using XILINX's optimized logiCOREs. Then we perform static timing analysis and power analysis of the synthesized design. A control system is designed and developed in VHDL to take care of symbol and timing detection of the receiver. The system is tested, synthesized to XILINX hardware and interfaced to the receiver.

1.1 Organization of the thesis

Chapter 2 gives an introduction to FSK systems and the design entities used in the receiver. Chapter 3 describes the FSK receiver design and control system design in detail. Chapter 4 describes the MATLAB model, the simulation results, waveforms and analysis. Chapter 5 describes the XILINX hardware model and synthesis results. Chapter 6 gives a summary of the thesis and suggests future work that can be done in the direction of this thesis.

Chapter 2

FSK Systems, an Overview

Digital modulation is the process by which digital symbols are transformed into waveforms that are compatible with the characteristics of the channel. In the case of baseband modulation these waveforms are pulses, but in the case of band pass modulation, the desired information signal is modulated to a sinusoid called a carrier wave. FSK modulation is a class of band pass modulation in which the frequency of the carrier varies in accordance with the information signal.

2.1 Frequency shift keying (FSK):

Frequency Shift Keying (FSK) system is a class of wireless systems that is very popular today and has widespread applications. An FSK system carries its information in the instantaneous frequency of the received signal. For e.g. a binary FSK system which transmits the symbols 0 and 1 have one frequency corresponding to the symbol 0 and another frequency to the symbol 1.

FSK systems are broadly classified into Coherent and Non-coherent systems. A coherent system requires carrier or phase synchronization at the receiver end in order to detect the signals whereas non coherent detection does not require any sort of synchronization. Consequently the design of non coherent systems is much simpler when compared to coherent systems making them more popular when power is an important concern. But non coherent systems have a BER performance of 3db less than the traditional coherent receiver at a BER of $10E-5$.

The general analytic expression for FSK modulation is

$$s_i(t) = \sqrt{\frac{2E}{T}} \cos(\omega_i t + \phi) \quad \begin{array}{l} 0 \leq t \leq T \\ i = 1, \dots, M \end{array}$$

where $s_i(t)$ is the modulated carrier, E is the energy content of $s_i(t)$ over each information symbol of duration T , ω_i is the frequency term with M discrete values, and the phase term, ϕ is an arbitrary constant. $(\omega_{i+1} - \omega_i)$ is typically assumed to be an integral multiple of π/T since FSK is implemented as orthogonal signaling where each tone in the signal set cannot interfere with any other tones. In case of binary FSK, the value of M is two, representing binary information symbols and a carrier with two possible frequencies.

2.2 BINARY FSK SYSTEM:

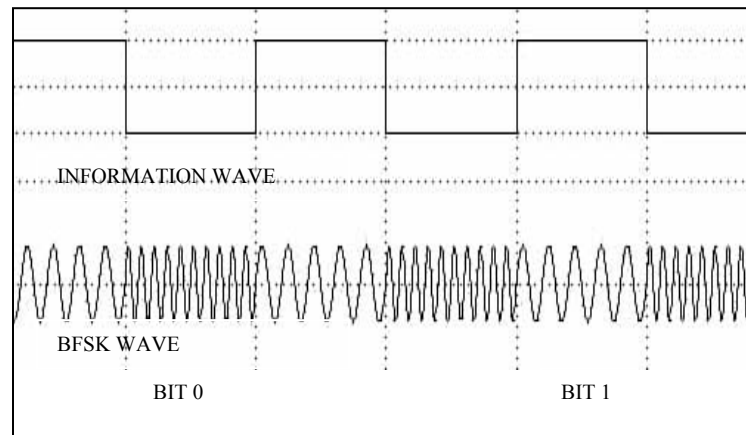


Fig 2.1: Binary FSK waveform

The binary FSK waveform displayed in Fig 2.1 illustrates the typical abrupt frequency changes at the symbol transitions. The top waveform represents the information symbols and the bottom waveform represents the modulated carrier signal. It can be seen that symbol '1'

is represented with a particular frequency and symbol '0' is represented with a different frequency. These frequencies would lie in the pass band of the channel in use.

A binary FSK system is characterized by having a signal space that is two dimensional with two message points. The message points are defined by the signal vectors:

$$s_1 = \begin{bmatrix} \sqrt{E_b} \\ 0 \end{bmatrix} \quad \text{and} \quad s_2 = \begin{bmatrix} 0 \\ \sqrt{E_b} \end{bmatrix}$$

where E_b represents the energy of the signal over one symbol duration.

The distance between the two message points is $\sqrt{2E_b}$.

The observation vector \mathbf{x} has two elements x_1 and x_2 defined by,

$$x_1 = \int_0^{T_b} x(t)\phi_1(t)dt$$

$$x_2 = \int_0^{T_b} x(t)\phi_2(t)dt$$

where $\phi_1(t)$ and $\phi_2(t)$ are orthonormal basis functions.

Figure 2.2 shows the signal space diagram for a binary FSK system.

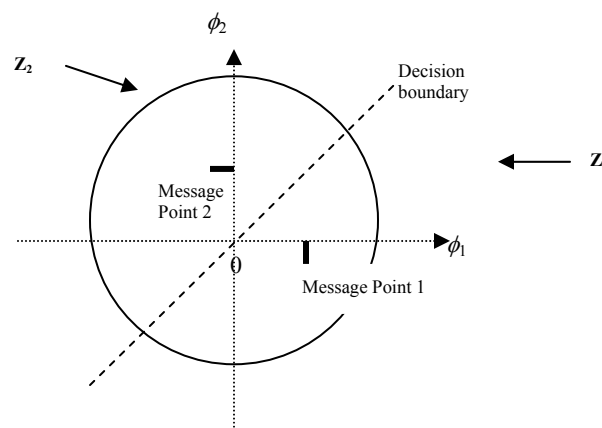


Fig 2.2: Signal Space of BFSK

The observation space is partitioned into two decision regions, labeled as Z_1 and Z_2 . Accordingly the receiver decides in favor of symbol 1 if the received signal point represented by the observation vector \mathbf{x} falls inside region Z_1 i.e. when $x_1 > x_2$ else the receiver decides in favor of symbol 0.

2.3 FSK DETECTION:

FSK detection is the process of extracting the information symbols from a modulated carrier wave. The detection process is mainly categorized into two types namely; coherent detection and non coherent detection. In the case of coherent detection, the receiver exploits the knowledge of the carrier's phase in order to detect the symbols whereas in the case of non coherent detection, the receiver does not utilize any phase reference information from the carrier. Coherent based receivers are usually complex to design but have the best BER performances. Also, coherent designs consume a lot of power. Non coherent receivers have simple design, consume less power but have reduced BER performances.

In the context of the present receiver design for deep space exploration, the receiver power is a very important issue and since the transmitter power can be elevated, power is traded for reduced BER performance.

2.3.1 Coherent binary FSK detector:

Figure 2.3 shows the block diagram of a coherent binary FSK receiver which is used commonly. As mentioned in the previous section a coherent receiver needs to be in phase synchronization with the transmitter. It consists of two correlators with a common input and which are supplied with two locally generated reference signals $\phi_1(t)$ and $\phi_2(t)$. The correlator outputs are then subtracted one from another and the resulting difference 'd' is compared with a threshold of zero volts. If $d > 0$, the receiver decides in favor of 1 else in favor of 0. The transmitted signal consists of both the frequencies f_1 and f_2 . The reference signals $\phi_1(t)$ and $\phi_2(t)$ are extracted by applying the received signal to a pair of narrow band filters, one tuned to f_1 and the other tuned to f_2 . Hence the reference signals are in phase coherence with the transmitted signals.

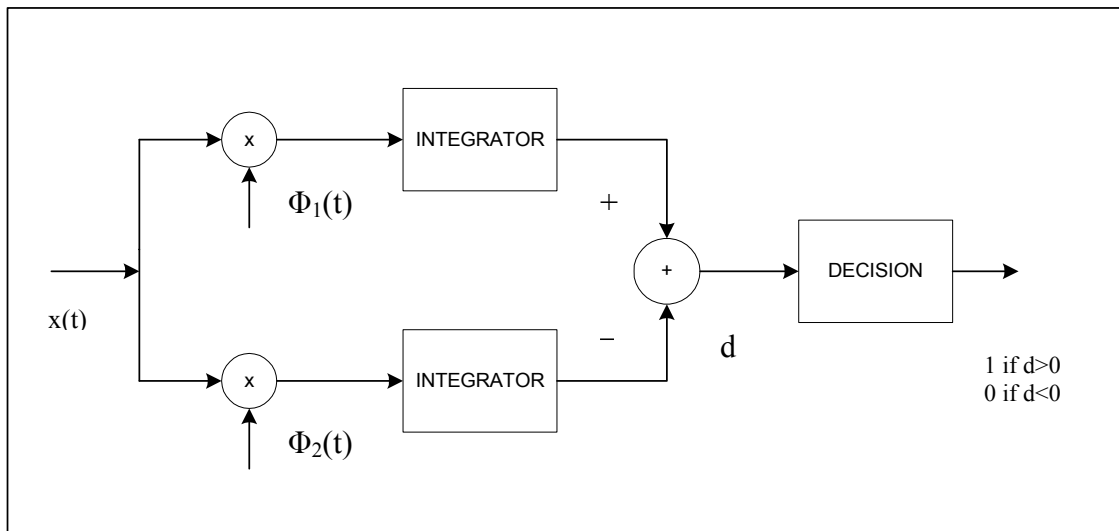


Fig 2.3: Coherent BFSK receiver

2.3.2 Non Coherent binary FSK detector:

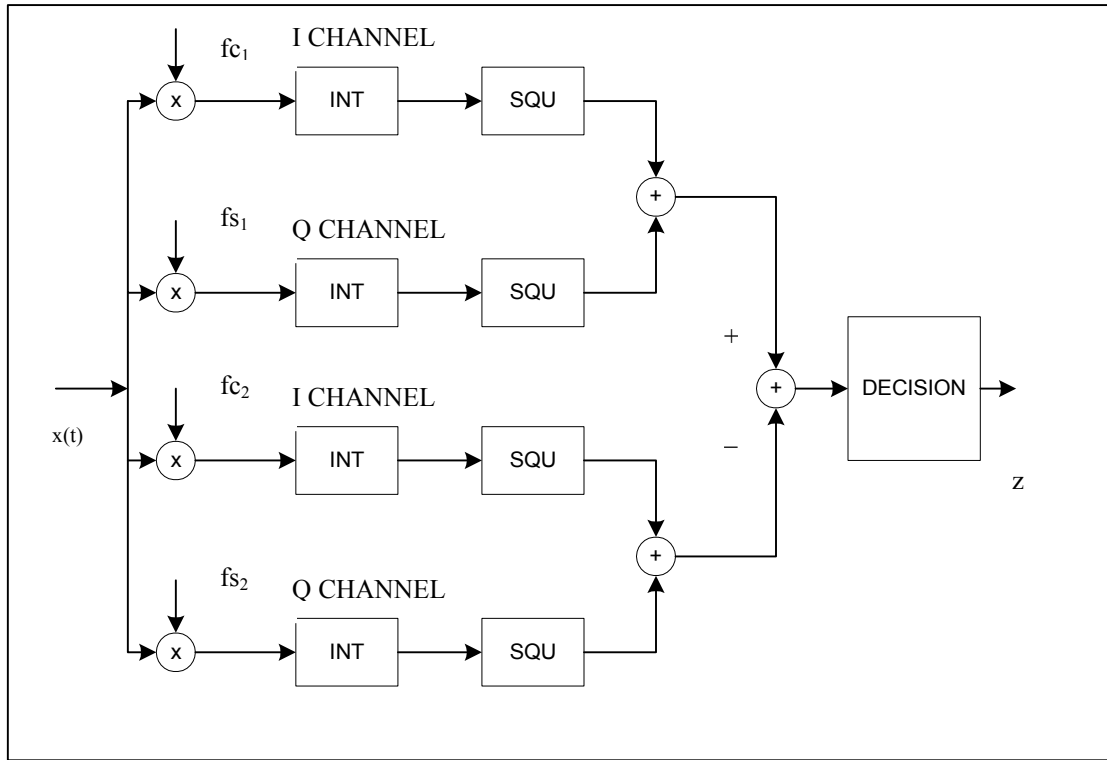


Fig 2.4: Quadrature receiver for non coherent detection

Figure 2.4 depicts the block diagram of a non coherent binary FSK detector. Since phase information of the carrier is absent, the detector is implemented as an energy detector. As we can see, the receiver consists of two channels namely; the in phase (I) channel and the quadrature phase (Q) channel. The two branches of the I channel are configured to detect the signal with frequency w_1 ; the reference signals being $\sqrt{2/T} \cos(w_1t)$ for the 'I' branch and $\sqrt{2/T} \sin(w_1t)$ for the 'Q' branch. A similar arrangement exists for the detection of signal with frequency w_2 as can be seen from the two branches of the Q channel. The blocks following the product integrators perform a squaring operation to prevent the appearance of any negative values. A difference of the energies of the channels I and Q is calculated and fed to the decision stage which decides in favor of w_1 if the difference is greater than zero else in favor of w_2 . The quadrature non coherent detector requires twice as many branches as the coherent detector and is not very power efficient.

Another common implementation for non-coherent detection is the envelope detector where band pass filters and envelope detectors are used. An envelope detector consists of a rectifier and a low pass filter. The detectors are matched to the signal envelopes rather than the signals themselves and a decision as to whether a one or a zero was transmitted is made on the basis of which two envelope detectors have the largest amplitude. Although the envelope detector has a simpler design as compared to the quadrature detector, the fact that quadrature detectors can be implemented digitally as VLSI circuits and also the use of filters and rectifiers in the envelope detectors increase their power requirement and cost than the quadrature detector.

2.3.3 Introduction to FAST FOURIER TRANSFORM (FFT) based detectors

Speaking of energy detection in non-coherent FSK systems, the Discrete Fourier Transform (DFT) based detection is another method which is gaining importance today. The DFT is a powerful tool used to perform spectrum analysis of discrete time signals. The N point DFT of a sequence $x(n)$ of length N is given by the formula,

$$X(k) = \sum_{n=0}^{N-1} x(n)W_N^{kn} \quad 0 \leq k \leq N-1$$

The sequence $X(k)$ can be thought of as a bank of N correlators, each representing the energy of the signal for a particular frequency which is used for analysis and detection. The advantage of using DFT for detection lies in its capability to handle Doppler shifts in the received signal. But, DFT computation as it is requires N^2 complex multiplications and N^2-N complex additions which make DFT impossible to implement especially for large values of N.

Fast Fourier Transform (FFT) algorithms [3] are a set of computationally efficient algorithms used to compute the DFT and have made the implementation of DFT a reality. These

algorithms work on the basis of a divide and conquer approach, by decomposing an N point DFT into successively smaller DFT computations and finally aggregating the result. The FFT algorithms bring about a phenomenal improvement in speed and computational efficiency of the DFT. For e.g. the radix 2 FFT algorithm [3] which is one of the most widely used FFT algorithms, requires a total number of $(N/2)\log_2 N$ complex multiplications and $N\log_2 N$ complex additions. The speed improvement factor by using the radix 2 FFT algorithms for sequences of size 1024 is about 200 and is better for larger sequences. The introduction of CORDIC algorithms to perform complex multiplications in FFT has improved the power efficiency of FFT computation to a very large extent and has made FFT based detection a very attractive choice for low power FSK receivers.

2.6 CO-ORDINATE ROTATION ALGORITHM (CORDIC):

The CORDIC (Co-ordinate Rotation Digital Computing) algorithm is a time and space efficient algorithm mainly used to calculate the Sine and Cosine of a given angle. The algorithm replaces multiplication/division by shift operations resulting in time and space efficiency. The only expensive operation in the computation is addition. The algorithm is commonly used in sine and cosine generation, polar-Cartesian conversions, and vector rotation.

An illustration of the CORDIC algorithm is given here. In FFT computations, a complex number is multiplied by the factor W_N^i which corresponds to a phase rotation of $2\pi i / N$. For e.g. let $A = x + jy$ and $W_N^i = e^{j26.56}$

$$\text{Therefore} \quad A e^{j26.56} = (x + jy)(\cos(26.56) + j\sin(26.56))$$

We could write the above product as,

$$A e^{j26.56} = X_1 + jY_1$$

Where

$$X_1 = \cos(26.56) (x - y \tan(26.56))$$

And

$$Y_1 = \cos(26.56) (y + x \tan(26.56))$$

But

$$\tan(26.56) \approx \frac{1}{2}$$

And

$$\cos(26.56) \approx \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \frac{1}{2^6}$$

As we can see, the “tan” and “cos” can be implemented as shift operations and the rest of the computations are simple additions. Shifters and adders are relatively simple to implement and have better space and time efficiency.

CHAPTER 3

FSK RECEIVER ARCHITECTURE

3.1 Motivation:

There are a lot of FSK detectors in the market today depending upon the application of interest. As mentioned previously, coherent receivers are the best in terms of BER performances but have complex system design and consume more power. Also, coherent designs require fine frequency tracking making them very sensitive to Doppler shifts and require a longer frequency acquisition time. The non coherent receivers currently used do not meet the power requirement and Doppler shift requirement demanded by the application of interest.

The objective of the receiver design is to have an all digital architecture. Digital designs are preferred over their analog counterparts mainly for the following reasons:

- a) CMOS digital circuits consume very less power than their analog counterparts. They can have sleep modes that allow the system to be completely shut off when no processing is done.
- b) Digital designs have no portability issues when it comes to fabricating the design using a better fabrication process that consumes lesser power and size.
- c) Digital circuits are less sensitive to changes in temperature, pressure and aging.

As mentioned earlier, the receiver is targeted for communications between an orbiting ship and a planetary landing vehicle. This scenario has important ramifications that motivate to optimize the receiver architecture and they are:

- a) The power consumption of the receiver of the planetary lander is more critical than the transmission power of the orbiting vehicle.
- b) There is no adjacent channel interference, hence the noise is additive white Gaussian.

Since power is an important concern at the receiver of the lander, the design trades off transmit power against the receiver power. Since noise is only additive white Gaussian, the design trades off BER performance to power consumption by implementing a non coherent architecture.

3.2 Overview of the receiver architecture:

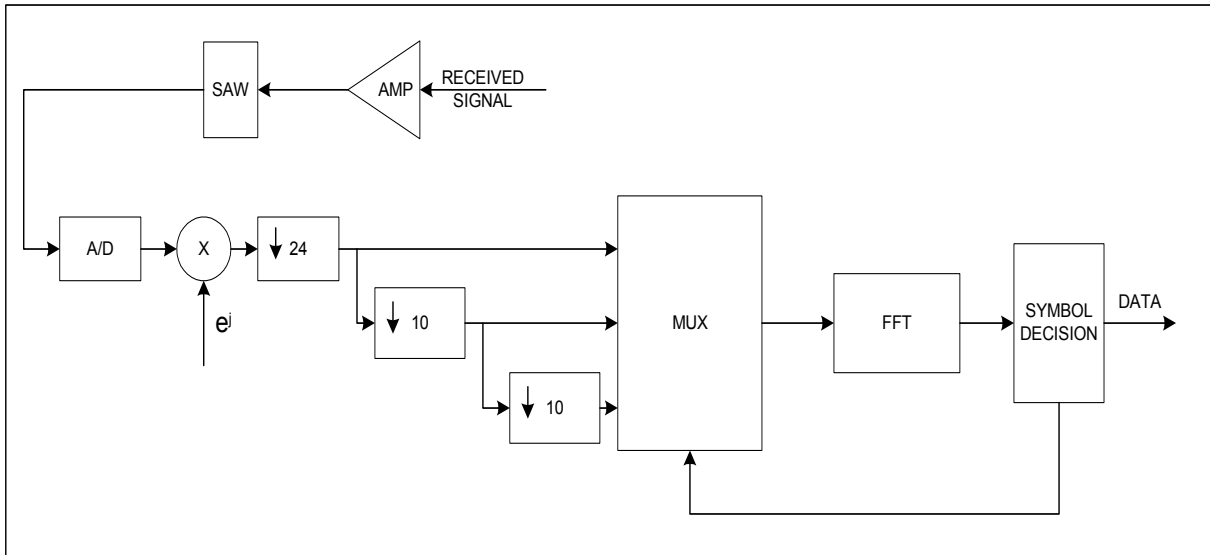


Fig 3.1: FSK receiver system diagram

Modulation type	Binary Frequency Shift Keying
Carrier Frequency	473.1 MHz
Data rates	100bps, 1kbps and 10kbps
Doppler Shift	± 10 KHz

Table 3.1: Receiver Specification

Table 3.1 shows the receiver specifications and Fig 3.1 shows the proposed receiver architecture. The received signal is amplified by a power efficient, low noise amplifier. The amplified signal is filtered with a surface acoustic wave filter. The filtered signal is sub sampled and digitized to 1-bit precision using a 1-bit A/D converter. The carrier frequency of the received signal is 473.1 MHz and this signal is subsampled at 1.2 MHz. Sub sampling is an excellent way to reduce power consumption since the circuit is made to operate at a much lower frequency even though the received signal frequency is centered at a higher value. The reason to choose a sampling frequency of 1.2MHz is dealt with in the succeeding sections. The process of 1 bit A/D conversion also leads to a simple and power efficient detector design. Moreover 1 bit quantization is a highly non linear operation which means that the preceding analog components need not be linear and no AGC circuit is needed. Non-linear amplifiers and samplers use considerably less power than their analog counter parts.

The one bit digitized signal is downconverted and decimated to baseband by first multiplying the signal with a complex exponential. The multiplication is done in order to shift the message part closer to DC before decimating it to a lower data rate so that the required information is not lost. Careful choice of the sub sampling frequency reduces the multiplication of the signal by i , 1 , $-i$ and -1 , in effect eliminating the need for a hardware multiplier. The complex multiplication process also produces the 'I' and 'Q' signals and calls for separate processing of each of these paths. The 1.2 Mbps signal is now decimated by 24 to obtain a signal rate of 50kpbs. The 50kpbs signal is further decimated by 10 to obtain data rates of 5kpbs and 500bps.

As seen from the receiver architecture block diagram, the three decimated signals available at the input of the MUX correspond to the data rates of 10kpbs, 1kpbs and 100bps. One of the three signals is selected which is appropriate with the data rate transmitted and fed into a 16-point FFT detector. The detector requires only 5 samples of the signal and the rest 11 samples are zeros. This approach eliminates one of the four stages of FFT computation reducing circuit complexity. A control block designed to take care of detecting the data rate transmitted controls the select line of the MUX. This block also analyzes the output of the FFT detector and takes care of symbol decision.

3.3 The need for Sub Sampling:

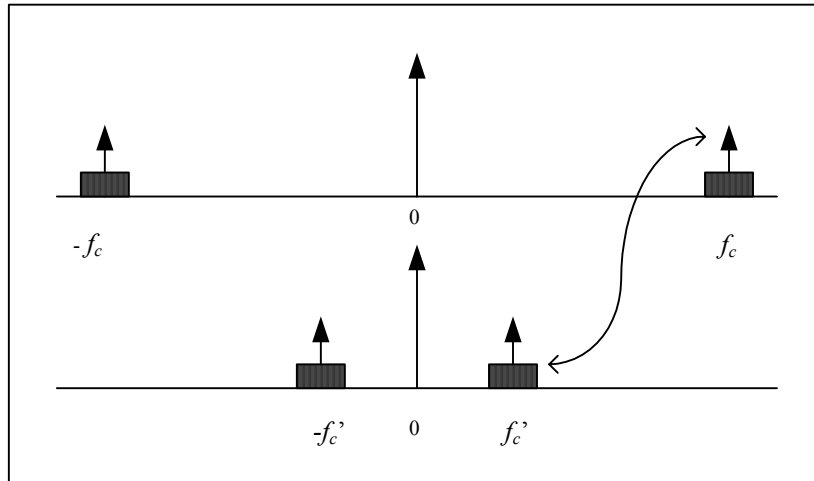


Fig 3.2: Effect of Subsampling

As mentioned in the previous section, sub sampling is an excellent way of reducing the circuit complexity and power consumption since the incoming signal is sampled at much lower rate than the highest frequency component contained in the signal which happens to be the carrier. Figure 3.2 demonstrates a received signal with carrier f_c being subsampled at a frequency f_s . Due to sub sampling, a copy of all signal frequencies will be shifted to a lower frequency. The frequency which is closest to DC (0Hz) denoted by f'_c can be utilized to extract the required baseband signal.

However there is a lower bound constraint on the sampling frequency due the fact that shifted replicas of the signal and noise will overlap with each other. The lower bound for the sampling frequency is calculated as follows:

From sub sampling theory, the frequency component f_c' is given by

$$f_c = \alpha f_c' \quad -(1/2) < \alpha < (1/2)$$

In order to prevent the out of band noise from aliasing into the signal band, band pass filtering is done after the amplifier stage. The SAW filter which serves the purpose has a bandwidth of about $f_{\text{saw}} = f_c/1000$. From the figure, consider the image at $-f_c'$. The noise within this image should be attenuated before reaching the signal band at f_c' . This constraint is satisfied by

$$f_{\text{saw}} < 2|\alpha|f_c - \Delta F \approx 2|\alpha|f_c \quad \text{where } \Delta F = hf_b \ll f_c$$

f_b : data rate of the information source

h: modulation index of FSK

$$\text{Hence } f_c > \frac{f_{\text{saw}}}{2|\alpha|}$$

It appears that F_s can be selected to down convert f_c to DC, but this is not the case. Since the signal is real valued such a down conversion would make it impossible to distinguish between $f_c + \Delta F$ and $f_c - \Delta F$ and thus prevent detection. Thus f_c is shifted to a frequency closer to DC and then downconverted to DC by multiplying the signal with a complex exponential $\exp(-imf_c'/F_s)$. If $f_c' = \pm f_s/4$, the down conversion reduces to multiplication by (i, 1, -i, -1) eliminating the need for power hungry multipliers. Further f_s has to be an integer multiple of the data rate in order to facilitate the decimation ratios and reduce power consumption. Thus f_s is chosen to be 1.2 MHz.

3.4 Noise effects due to 1 bit quantization:

One bit data processing used in the receiver allows for maximum power savings since the operation is entirely non-linear. This allows the preceding analog components also to be non-linear. Non linear analog components like amplifiers and samplers have comparatively simpler design and hence more power efficient. However the quantization process severely raises the noise floor as it introduces a large quantization error. Simulation and analytical results show that an SNR loss of 2 dB is incurred due to one bit quantization. Analytical treatment follows:

$$\begin{aligned}\text{SNR}_{\text{loss}} &= 10 \left(\log \frac{E_b}{N_0} - \log \frac{E_b}{N_0 + N_q} \right) \\ &= 10 \left(\log \frac{N_0 + N_q}{N_0} \right) \\ &= 10 \log \left(1 + \frac{N_q}{N_0} \right) \\ &\approx \frac{10}{\ln(10)} \frac{N_q}{N_0}\end{aligned}$$

The noise power introduced due to B bit quantization is given by,

$$\sigma_q^2 = \frac{2^{-2(B-1)}}{12}$$

Since B = 1 in the present case,

$$\sigma_q^2 = \frac{1}{12}$$

and

$$N_q = \frac{\sigma_q^2}{F_s} = \frac{1}{12F_s}$$

Also,
$$E_b = \int_0^{T_b} \sin^2(2\pi F_b t) dt = \frac{1}{2F_b}$$

Therefore
$$\frac{N_q}{N_0} = \frac{\frac{1}{2F_b}}{\frac{1}{6F_s} \frac{E_b}{N_0}} = \frac{F_b E_b}{6F_s N_0}$$

Finally,

$$\text{SNR}_{\text{loss}} = \frac{10}{\ln(10)} \frac{F_b E_b}{6F_s N_0}$$

This shows that the SNR loss is significant for small over sampling ratios and large SNRs. For an over sampling ratio (F_s/F_b) of 120 and SNR of 15, the SNR is loss is about 0.2 dB.

3.5 Detection mechanism:

A 16 point DFT is used to detect the binary FSK tones. The advantage of using a DFT detector is listed as follows:

- a) Capability of handling great frequency offsets without having to down convert the signal exactly to 0 Hz.
- b) A frequency tracking algorithm allows the DFT based receiver to be immune to Doppler shifts.
- c) An FFT algorithm is used to compute the DFT and is done in relatively fewer operations leading to significant power savings.

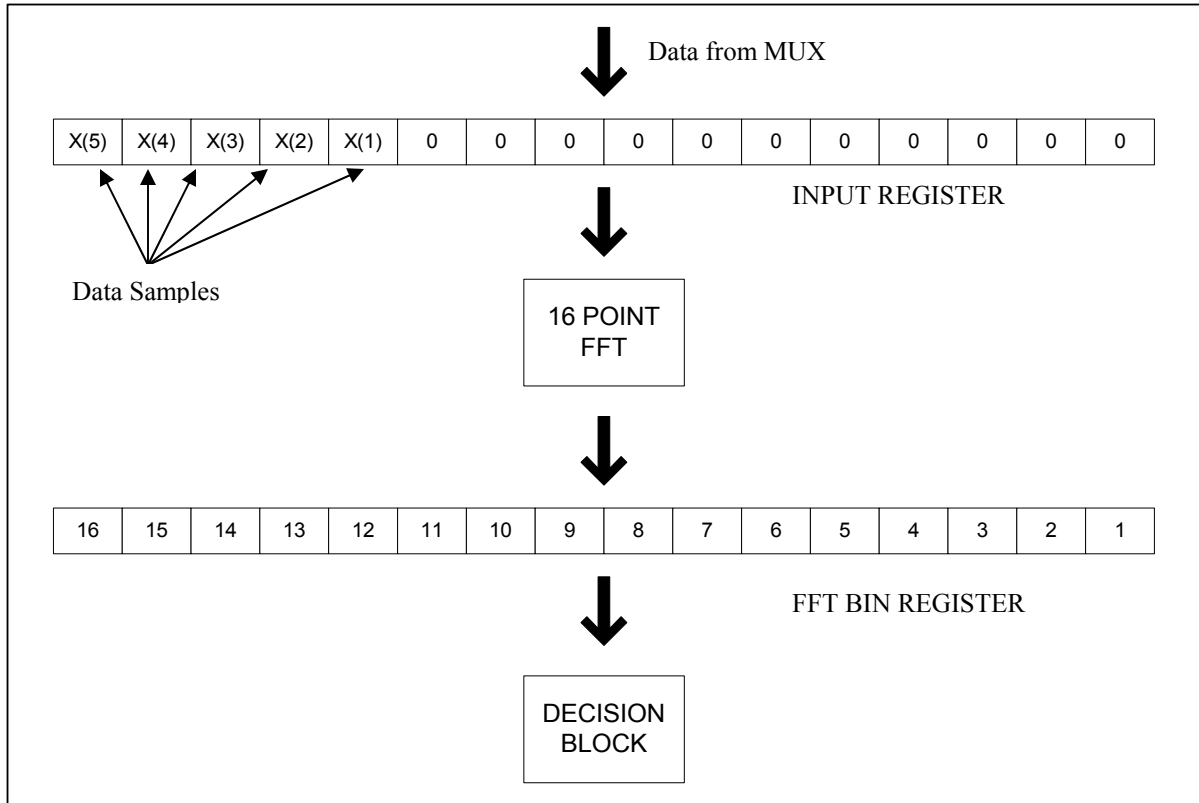


Fig 3.3: FFT Detector

Figure 3.3 shows a block diagram implementation of the FFT detector. The input register to the FFT engine stores 5 samples from the signal and 11 zeros. It has been proved in [1] that 5 signal samples are sufficient to keep the performance loss below 0.25 dB. The contents of the register are then fed into the FFT engine. The output of the FFT is a bank of 16 values referred to as ‘bins’. Each of these bins represents the energy content of the signal in different frequency intervals. Data detection is done by analyzing the 16 bins. One out of the 16 bins is regarded to be the ‘decision bin’. The output of the decision bin is compared with a known threshold value using a comparator circuit. Decision is in favor of symbol 1 if the value of the ‘decision bin’ is greater than the threshold value; else decision is in favor of symbol 0.

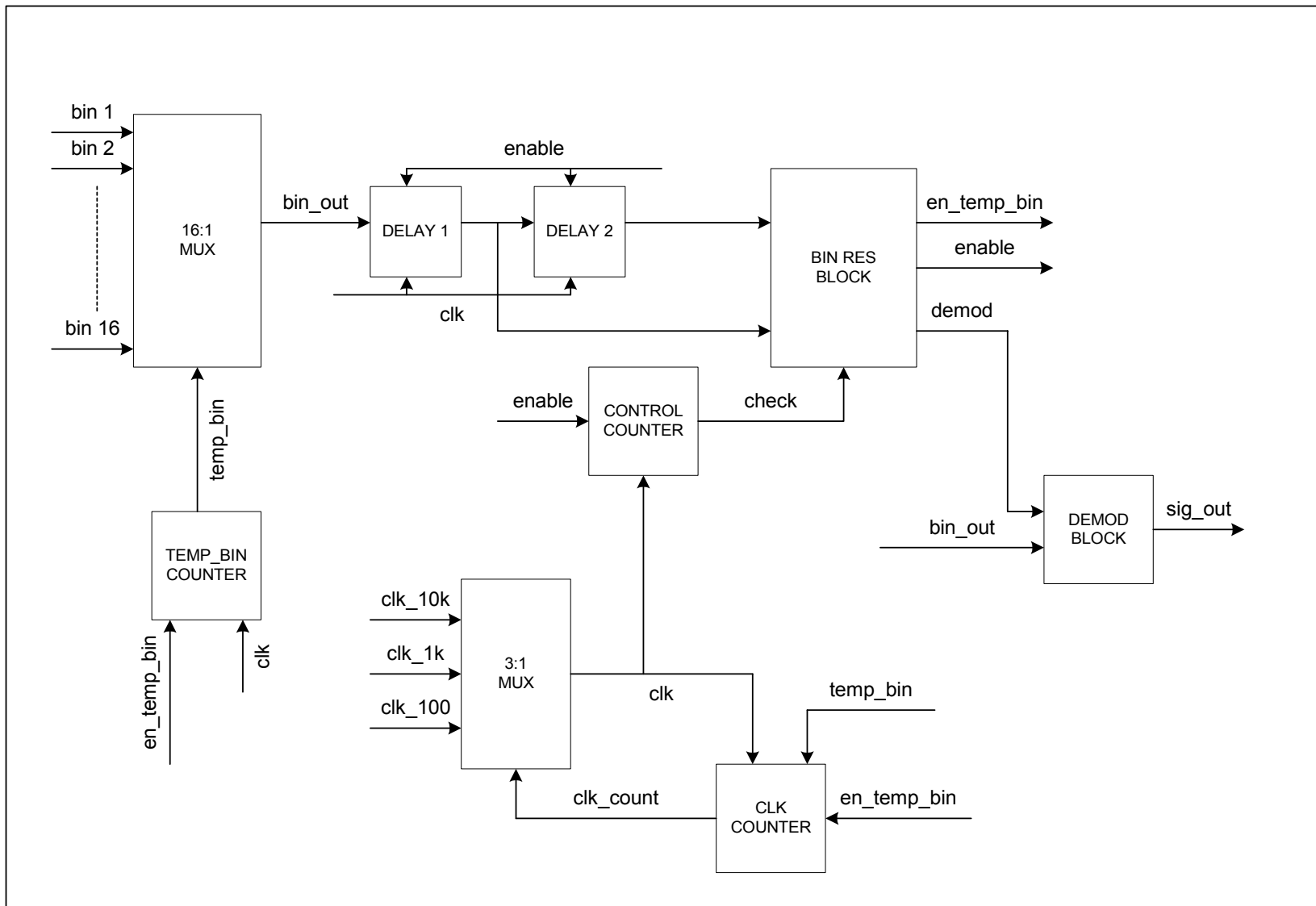


Fig 3.4: Control System block diagram

3.6 Control System:

Figure 3.4 depicts the block diagram of the control circuit. The output of the DFT detector is captured by a 16 to 1 multiplexer. The purpose of the control circuit is to determine the “decision bin” out of the 16 bins and to decide the symbol rate. In order to facilitate bin resolution and data detection a pilot signal is first transmitted from the transmitter which consists of a series of alternate ones and zeros. To start with, the very first bin is selected and the data rate is assumed to be 10kbps. The output of the 16:1 MUX is passed through two registers each serving the purpose of delaying the data by one clock cycle. This is done so that two subsequent symbols can be compared with each other. The bin resolution block compares the values of the registers DELAY1 and DELAY2 with a threshold value. The following decision algorithm is used:

$$\text{Current bin} = \text{Decision bin if } \text{DELAY1} < \text{Threshold value} < \text{DELAY2 or} \\ \text{DELAY2} < \text{Threshold value} < \text{DELAY1}$$

The threshold value in the bin resolution can be adjusted allowing for variations in the output of the DFT block. If decision fails on the current bin then the next bin is selected by incrementing the ‘temp_bin’ line. This process is repeated until a decision bin is found with the present clock rate. Once the value of ‘temp_bin’ reaches 16 and still a “decision bin” hasn’t been found, it implies that the data rate is different from the one assumed. Hence the clock rate is reduced to 1kbps and then the process is repeated starting with the first bin. The ‘CONTROL COUNTER’ block is used to assert the ‘check’ signal which enables the “BIN_RES BLOCK’. After obtaining the right decision bin, control is transferred to the demodulation block which takes care of converting the output of the DFT to binary symbols.

CHAPTER 4

SIMULINK MODEL

4.1 Introduction to SIMULINK:

MATLAB or “Matrix laboratory” is one of the most popular technical computing environments today that provides mathematical and engineering functions for system simulations, data analysis and algorithm development. MATLAB operates as an interactive programming environment and has support for graphical output to supplement numerical results. SIMULINK is a simulation and prototyping environment, part of MATLAB for modeling, simulating and analyzing dynamic systems. SIMULINK provides a block diagram interface that is built on the core MATLAB numeric, graphics, and programming functionality. MATLAB has a collection of highly optimized application specific functions called “toolboxes”. Toolbox functions are built in MATLAB language and can be easily incorporated into a MATLAB program, viewed and modified. “Block sets” are collections of application specific blocks built on the functionality of toolboxes and can be directly included in SIMULINK models.

SIMULINK uses a graphical user interface (GUI) for solving process simulations. Instead of writing MATLAB code, we simply connect the necessary “icons” together to construct the block diagram. SIMULINK is an icon-driven state of the art dynamic simulation package that allows the user to specify a block diagram representation of a dynamic process. Assorted sections of the block diagram are represented by icons which are available via various "windows" that the user opens (through double clicking on the icon). The block diagram is composed of icons representing different sections of the process (inputs, state-space models, transfer functions, outputs, etc.) and connections between the icons (which are made by "drawing" a line connecting the icons). Once the block diagram is "built", one has to specify the parameters in the various blocks, for example the gain of a transfer function. Once these parameters are specified, then the user can simulate the model.

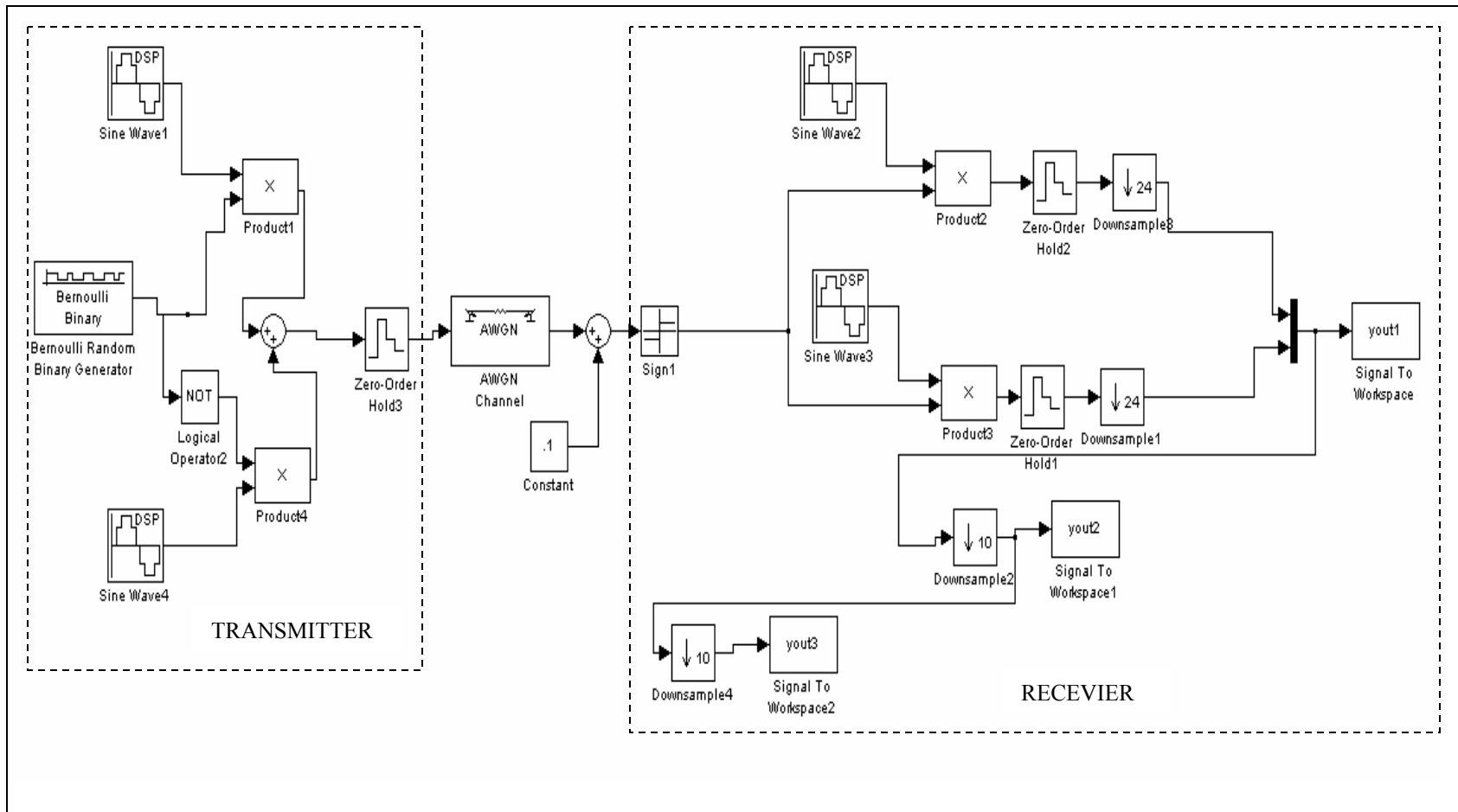


Fig 4.1: SIMULINK model of the FSK receiver

4.2 SIMULINK model of the receiver:

Fig 4.1 shows the block diagram of the FSK receiver modeled in SIMULINK. Obviously a receiver cannot be tested without a transmitter indicating the presence of a transmitter and an AWGN channel in the block diagram. The transmitter is modeled with a Bernoulli random number generator as its information source. The random generator is configured to output either a one or a zero with a specific probability and at a rate of 10kbps. There are two signal sources acting as the two carriers of BFSK. One of the sources operates with a frequency of 437.1 MHz while the other operates at 437.12 MHz. The tone separation is thus 20 KHz. Two product modulators are used, the upper one for modulating symbol 1 and the lower one for symbol zero. Finally outputs of the modulators are summed to simulate a BFSK signal with an information rate of 10kbps. The signal is passed through an additive white Gaussian noise channel (AWGN) to add white noise to the transmitted signal. This completes modeling the transmitter and the channel.

The receiver part of the block diagram starts with a sign block that basically functions like a 1-bit A/D converter. The sign block outputs a one if the input value is greater than zero else a negative one if the input is less than zero. The convention is, symbol one is represented by value one while symbol zero with value negative one. This is done in order to distinguish symbol zero from the value zero. The sign block is operated at a sampling rate of 1.2 MHz. The output of the sign block is down converted to base band by multiplying the signal with a complex exponential. As we have discussed before, complex multiplication is reduced to multiplication with 1, i , -1 and $-i$ by proper choice of sampling frequencies. 1 and -1 represents the real part while i and $-i$ represents the imaginary part. Since the quantities are complex in nature, the real part and the imaginary part should be processed separately. Consequently the data path this point onwards branches out to two paths; the real path and the imaginary part as witnessed in the diagram. The upper branch denotes the real part with the received signal being multiplied by $\cos(\Pi n/2N)$ and the lower branch is the imaginary part being multiplied by $\sin(\Pi n/2N)$. The processing blocks for real data and imaginary data are the same. The down converted signal is now decimated by 24 to reduce the data rate to

50kbps. We now have a signal that can be processed by the FFT detector. As we have discussed before, the FFT block uses only 5 samples of the signal for DFT computations. The rest 11 inputs to the detector are zeros. This process results in an additional decimation of the data rate by 5, bringing down the rate to 10kbps which should be the final data rate. As we can see there is an inherent timing synchronization in the design resulting from proper choice of the sampling frequency of the A/D converter and the decimation ratios. For lesser data rates such as 1kpbs and 100bps, additional stages of decimation are required. For instance, for a data rate of 1kpbs, the 50kpbs signal is decimated by 10 to reduce the rate to 5kpbs. This signal incurs an additional decimation of 5 from FFT processing finally yielding a data rate of 1kpbs.

The SIMULINK model of the receiver does not include the FFT detector block as well as the control circuit block. We found it more convenient to capture the output of the decimated signal to a workspace (which basically stores all the data values as a matrix) and then writing a MATLAB script to apply the FFT on the captured data. The program also does the additional task of stripping the first five bits from the data and padding the bits with eleven zeros and feeding them to the FFT algorithm. The MATLAB script is included in the Appendix for reference. Generally, it is very difficult to model a control circuit in SIMULINK. Hence we decided that the easiest way was to write a VERILOG or VHDL program capturing the functional or gate level description of the control circuit and then simulating it. Since the final objective is to reduce the entire receiver model to hardware, this method saves an additional step of converting the SIMULINK model to a VHDL/VERILOG model. The control block which was explained in the previous chapter is written in VHDL and is included in the Appendix for reference.

4.3 SIMULATIONS

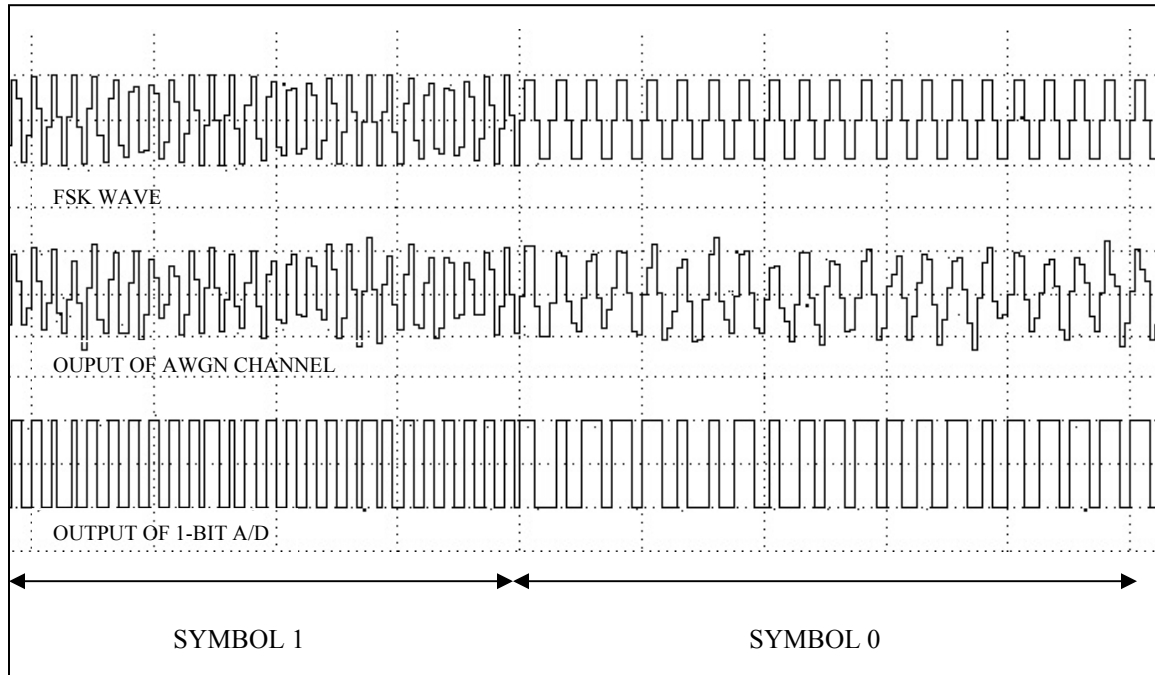


Fig 4.2: Transmitted waveform and Received Digitized waveform

We simulated the SIMULINK model for all the three data rates and found that the model was performing as expected. The wave forms obtained at various points in the design when the model is run with a bit rate of 10kpbs are indicated in this section. The simulation is run for 0.02 seconds so that 200 symbols are emitted by the Bernoulli source. Figure 4.2 shows a section of three different waveforms. The first waveform is the output of the FSK transmitter. The first half of the waveform represents symbol 1 and the second half represents symbol 0. The frequency of the signal associated with symbol 1 is 473.12 MHz and the frequency of symbol 0 is 473.1 MHz. The second waveform is the result of the FSK waveform being passed through the additive white Gaussian channel with an SNR of 5db and a noise power of 100mW. As we can see, the transmitted signal is highly corrupted by noise in the channel. This signal is input to the 1-bit A/D converter of the receiver which basically converts the received signal to a rectangular waveform as witnessed in waveform 3. We can also see a clear distinction between symbol 0 and symbol 1 in their frequency representations.

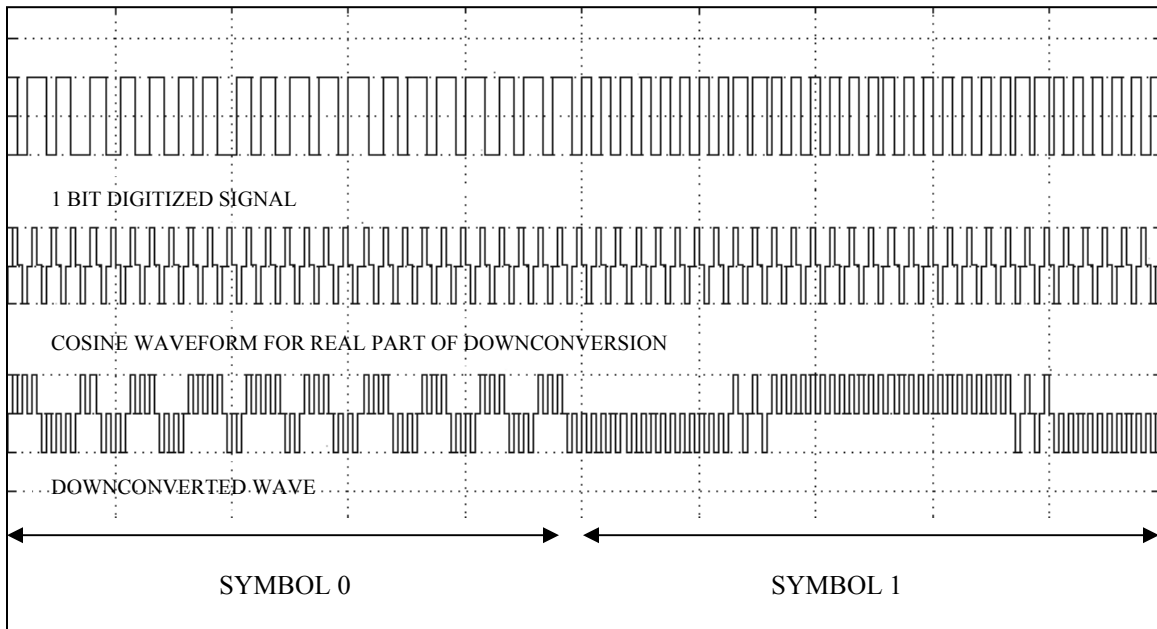


Fig 4.3: Down conversion waveforms

Figure 4.3 shows the waveforms resulting from the down conversion operation. These waveforms are specific to data processing in the real path. The first waveform is the 1 bit digitized waveform from the A/D converter. The second waveform is the cosine waveform that alternates between 1 and -1 with 0 interspersed. The cosine signal serves the purpose of the in-phase function required for real part multiplication. The third waveform is real part of the down converted wave which is the product of the first and the second waveforms.

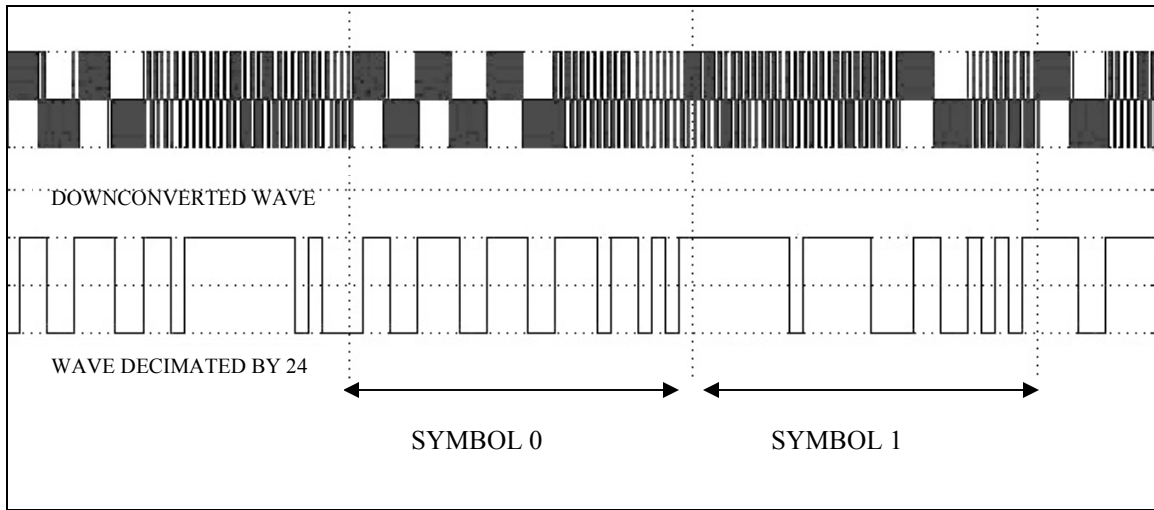


Fig 4.4: Decimated waveform

Figure 4.4 depicts the results of data rate decimation. The first waveform is the down converted wave which we have seen before, and the second waveform is the result of decimation by the order 24. We can see that the decimated waveform has a clear distinction between the symbols 0 and 1.

The screenshot shows the MATLAB Array Editor window for a variable named 'val'. The window title is 'Array Editor: val'. The menu bar includes File, Edit, View, Web, Window, and Help. Below the menu bar, there are icons for copy, paste, and save, followed by a numeric format dropdown set to 'shortG', and size input fields showing 'Size: 16 by 200'. The main area displays a 16x6 matrix. The first five rows contain complex numbers in scientific notation, while the remaining eleven rows contain the value '0'.

	1	2	3	4	5	6
1	1 + 1.592e-015i	1 + 8.9396e-015i	1 + 1.6287e-014i	1 + 2.3635e-014i	1 + 3.0983e-014i	1 + 3.833e-014i
2	1 + 3.0615e-015i	1 + 1.0409e-014i	1 + 1.7757e-014i	1 + 2.5104e-014i	1 + 3.2452e-014i	1 + 3.98e-014i
3	-1 - 4.531e-015i	-1 - 1.1879e-014i	1 + 1.9226e-014i	1 + 2.6574e-014i	-1 - 3.3922e-014i	-1 - 4.1269e-014i
4	-1 - 6.0006e-015i	-1 - 1.3348e-014i	1 + 2.0696e-014i	1 + 2.8043e-014i	-1 - 3.5391e-014i	-1 - 4.2739e-014i
5	1 + 7.4701e-015i	1 + 1.4818e-014i	1 + 2.2165e-014i	1 + 2.9513e-014i	1 + 3.6861e-014i	1 + 4.4208e-014i
6	0	0	0	0	0	0
7	0	0	0	0	0	0
8	0	0	0	0	0	0
9	0	0	0	0	0	0
10	0	0	0	0	0	0
11	0	0	0	0	0	0
12	0	0	0	0	0	0
13	0	0	0	0	0	0
14	0	0	0	0	0	0
15	0	0	0	0	0	0
16	0	0	0	0	0	0

Fig 4.5: Input data matrix to the FFT detector

The data rate is now reduced to 50kbps. Since the transmitted data rate is 10kbps, the decimated wave seen above can be directly fed to the FFT detector for further processing. The wave is captured to a matrix named “yout1” as indicated in Fig 4.1. The MATLAB accesses “yout1” and converts it to a 16 by 200 matrix form which can be fed into the FFT detector. This matrix is referred as “val” in the MATLAB script. The first 6 values of this matrix are displayed in Fig 4.5. As we can see, only the first five values are data in complex form and the rest 11 values are zeros.

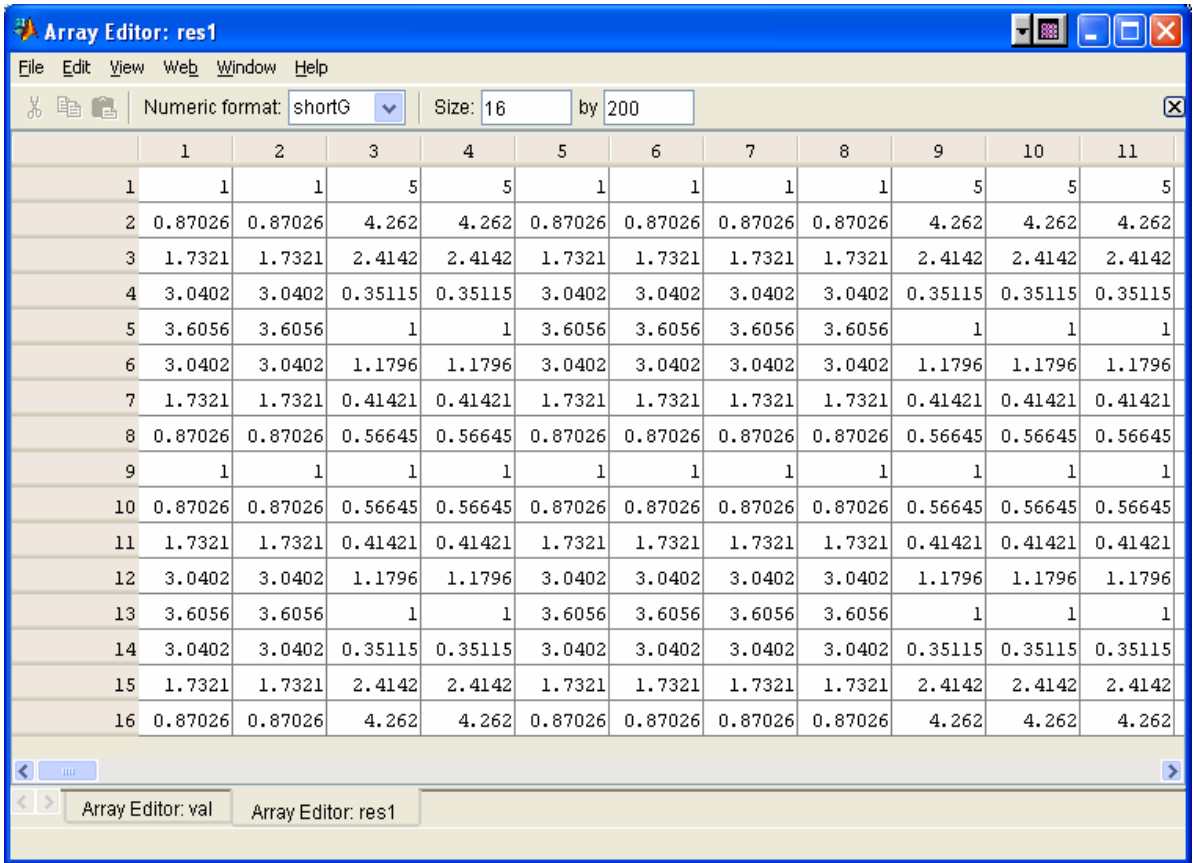


Fig 4.6: Output data matrix after FFT computation

The formatted data as seen in the matrix “val” is fed to the FFT detector which is basically implemented by invoking the MATLAB “fft” inbuilt function. Fig 4.6 displays the absolute value of the output of the FFT operation stored in a matrix named “res1”. The column numbers represent the symbol instants and the rows represent the 16 bin output for each symbol. The first eleven symbols transmitted by the Bernoulli source are 1, 1, 0, 0, 1, 1, 1, 1, 0, 0 and 0. With these symbols in view, we can see from fig 4.6 that there are quite a few bins which can be regarded as a “decision bin” for symbol detection. We select bin number 5 to be our decision bin and set a threshold value of 2. Hence the decision algorithm now becomes,

$$\begin{aligned} \text{Symbol} &= 1 \text{ if bin } (5) > 2 \\ &= 0 \text{ if bin } (5) < 2 \end{aligned}$$

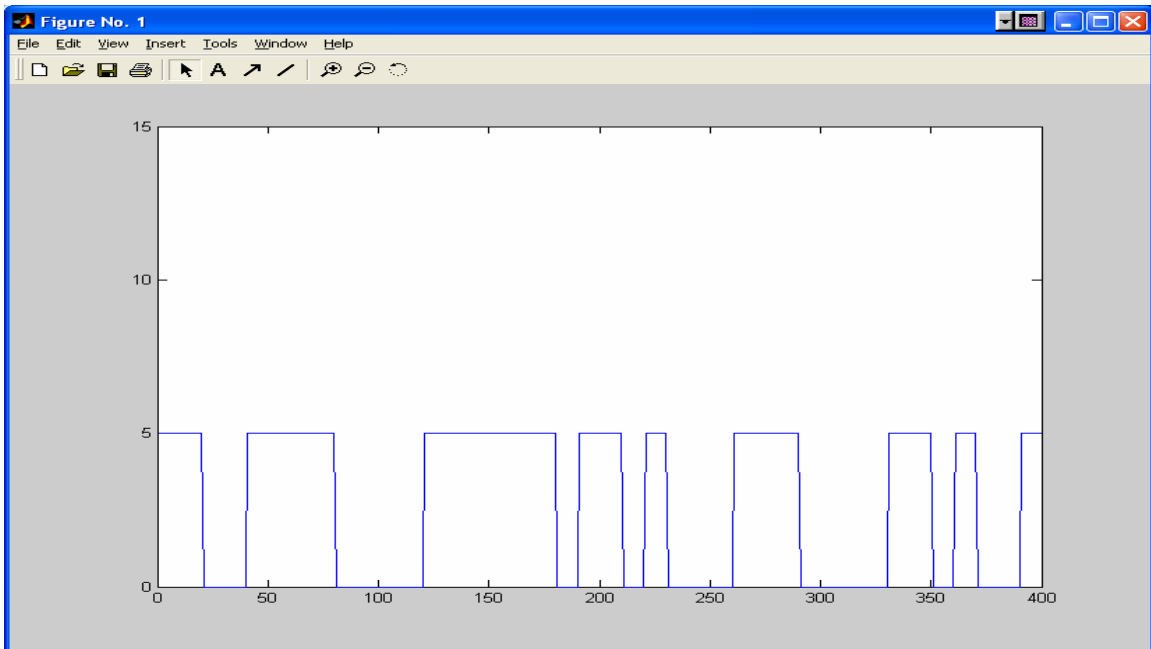


Fig 4.7: Receiver output after symbol detection

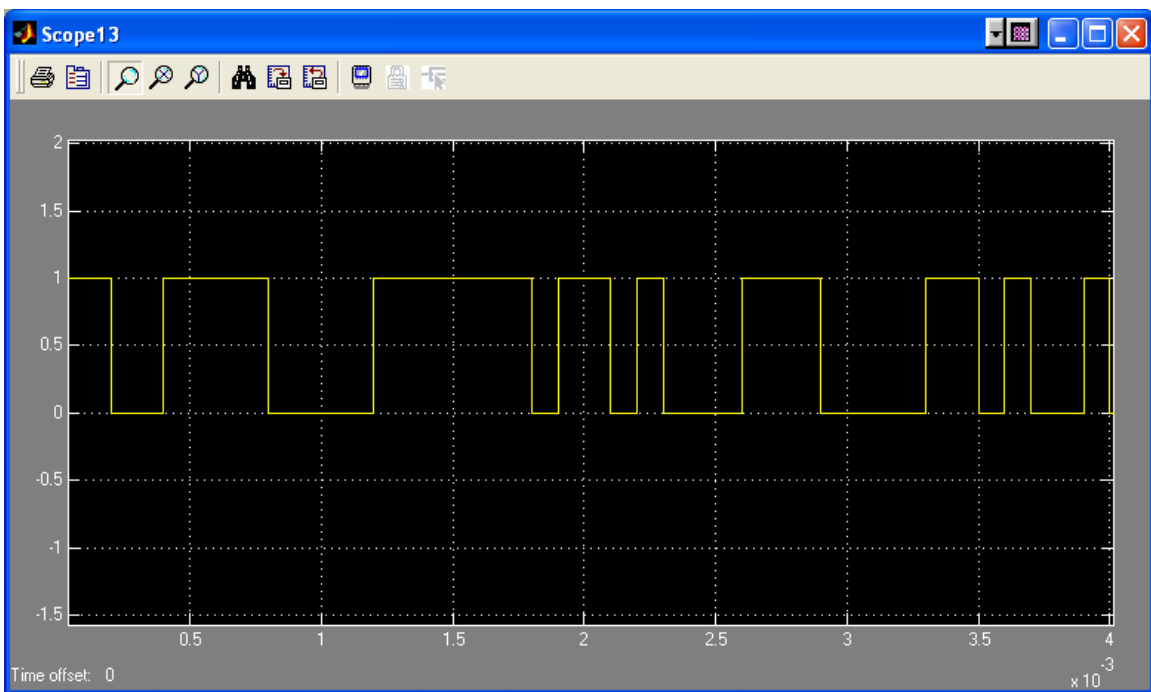


Fig 4.8: Output of the Bernoulli transmitter

Fig 4.7 shows the final detected waveform plotted in MATLAB and fig 4.8 shows the input waveform. As we can see, the transmitted waveform and the detected waveform match with each other.

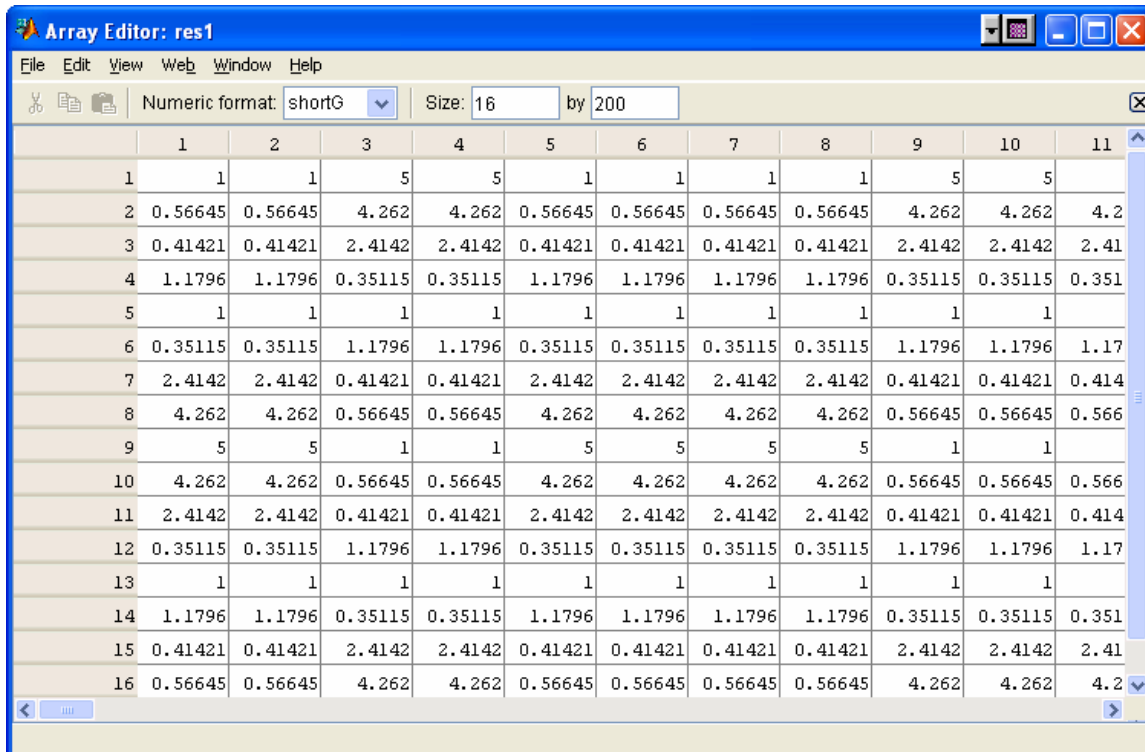


Fig 4.9: FFT detector output after Doppler shift of 5 KHz

To test the receiver for Doppler invariance, we increased the carrier frequencies of the transmitter by 5 KHz and ran the model. Fig 4.9 displays the output of the FFT detector for the first eleven time instants. As we can see, the decision bin is no longer bin 5 and is displaced to a different bin. Then, the task is to change the decision bin from bin 5 to another suitable bin. In this case we choose, bin 8. A frequency tracking algorithm will help keep track of the changes in magnitude of the decision bin. As we see a decrease in the magnitude of the decision bin, we also see a proportional increase in the magnitude of the bin adjacent to the decision bin. Thus the function of the frequency tracking algorithm is to increment/decrement the bin number when the decision bin magnitude falls below a certain level.

4.4 VERIFICATION

In order to test whether the receiver was working, we sent a string of 10 bits from the transmitter and observed the bit string at the receiver after detection. The test case is give below,

TEST CASE FOR 10KBPS DATA RATE

TRANSMITTED BIT SEQUENCE : 1,0,1,1,1,0,0,0,0,1
CARRIER FREQUENCY 1 : 473.12MHZ
CARRIER FREQUENCY 2 : 473.1MHZ
INPUT SIGNAL : 100mW
SNR : 15dB

DATA OBSERVED AT THE RECEIVER

RECEIVED BIT SEQUENCE : 1,0,1,1,1,0,0,0,0,1
DECISION BIN : BIN 7
MAXIMUM VALUE (BIT 1) : 3.17
MINIMUM VALUE (BIT 0) : 0.566
THRESHOLD VALUE : 2

These results imply that the receiver is working as expected. Similar tests were conducted for data rates of 1kbps and 100bps and found that the receiver was working properly.

4.4.1 Receiver Performance to Doppler Shifts

We tested the receiver for Doppler changes in frequency by varying the frequency of the transmitted signal by different proportions. We found that the receiver was working satisfactorily for Doppler shifts up to 10 KHz. Table 4.1 shows the simulation results.

Transmitted data rate : 10kbps
Decision bin without Doppler shift : Bin 8

CHANGE IN FREQUENCY	100HZ	200HZ	500HZ	1KHZ	1.5KHZ	3KHZ
DECISION BIN	8	8	7	7	6	6

Table 4.1: Performance of the receiver to Doppler Shift

Similar tests were conducted for data rates of 1kbps and 100bps and found satisfactory performance.

4.4.2 Receiver BER Performance

SNR (dB)	10KBPS		1KBPS		100BPS	
	DETECTION ERRORS	BER	DETECTION ERRORS	BER	DETECTION ERRORS	BER
1	290	0.29	135	0.135	130	0.13
5	250	0.25	110	0.11	108	0.108
10	120	0.12	85	0.085	80	0.08
15	1	0.001	0	10e-5	0	10e-5
20	0	≈0	0	≈0	0	≈0
25	0	≈0	0	≈0	0	≈0

Table 4.2: BER performance of the receiver

We tested the model for a variety of noise conditions by varying the SNR of the transmitted signal in the AWGN channel. We set the input signal power at a constant 100mW. Table 4.2 displays the results obtained for different values of SNR. The BER was measured by transmitting 1000 information symbols at the transmitter end and measured the no of

symbols that were detected erroneously. After comparing these results with the BER performance of an optimal un-coded non coherent FSK receiver, we found that the FFT based receiver has a performance degradation of approximately 2.5 db at a BER of 10^{-3} . The difference in performance is lesser for better BER. The results also indicate consistency in the performance of the receiver to the three data rates.

Figure 4.10 displays a logarithmic plot of BER v/s SNR. The y axis corresponds to BER values and is in logarithmic scale while the x axis corresponds to SNR values (dB) and is in linear scale.

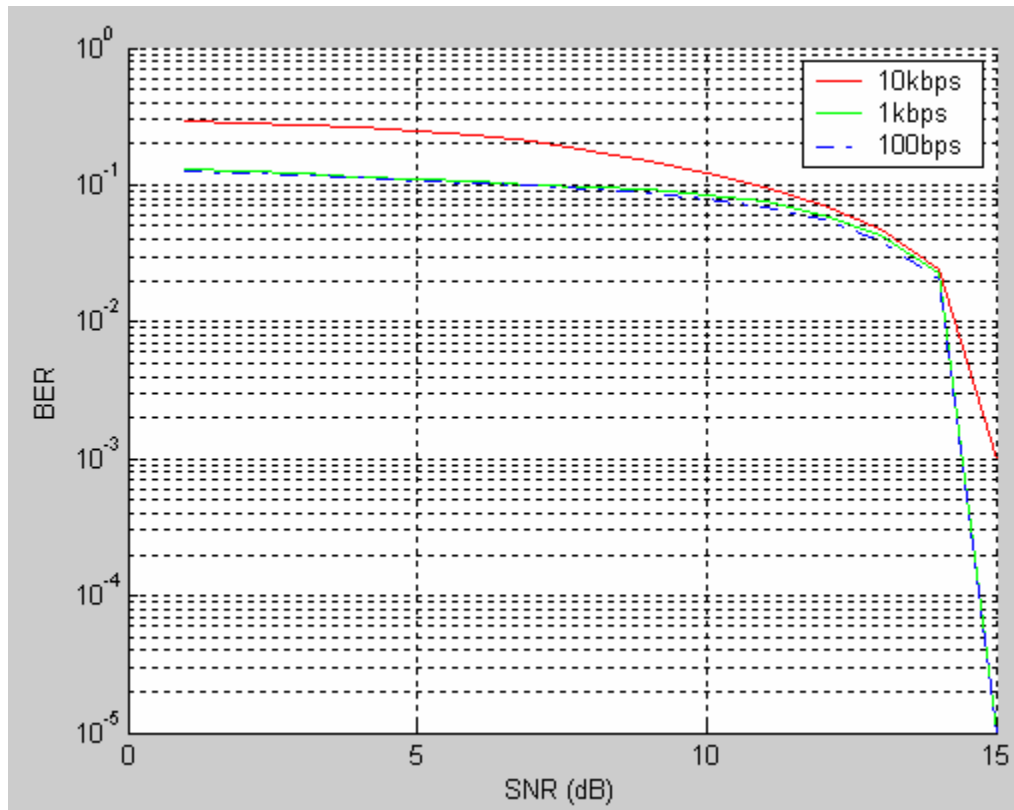


Fig 4.10: BER plot for the three data rates

4.4.3 Receiver performance to variations in A/D clock

Original Clock Frequency : 1.2 MHz
Data rate : 10 kbps
SNR : 15 dB

Frequency Variation (%)	BER
0.1	0.008
0.2	0.012
0.3	0.017
0.4	0.024
0.5	0.036

Table 4.3: Receiver performance to clock variation at A/D converter

We tested the receiver by varying the clock frequency by small amounts at the A/D converter. Table 4.3 indicates the simulation results obtained. Such frequency variations are restricted to $\pm 0.5\%$ of the original clock rate. As we can see, the performance of the receiver degrades as the variation in clock frequency increases and is highest at 0.5% variation.

CHAPTER 5

XILINX IMPLEMENTATION OF THE RECEIVER

5.1 Introduction to System Generation in XILINX

The receiver model developed in SIMULINK is useful to validate the functionality of the receiver design at a system level. In order to get a power estimate of the receiver, the SIMULINK model has to be reduced to hardware. As mentioned before, SIMULINK's XILINX block set allows us to develop a XILINX hardware model of the receiver using the XILINX building blocks. This process basically reduces to translation of the SIMULINK model to a XILINX model provided a one to one correspondence exists between each and every block. The hardware model is developed and tested in SIMULINK and the system generator tools of XILINX is used to synthesize the model by generating .bit file targeted to a particular XILINX FPGA. A .bit file contains all the configuration information defining all the internal logic and interconnections in the FPGA.

The System Generator in XILINX is a very convenient method for electronic designs to be created, tested, and translated into hardware for XILINX FPGAs. The tool extends SIMULINK to support bit and cycle accurate system level simulation, and automatic code generation for XILINX FPGAs. System Generator co-simulation interfaces extend SIMULINK to incorporate FPGA hardware and HDL simulation into the system-level environment as naturally as other library blocks. System Generator presents a high level and abstract view of the design, but also exposes key features in the underlying silicon, making it possible to build extremely high-performance FPGA implementations.

System Generator designs are built and simulated within the SIMULINK block editor. Each block produces results that make sense for the setting in which it is used. For example, a multiplier whose inputs are signed fixed point numbers produces a signed result having an appropriate width and binary point position. Signal types are propagated automatically, so when one block is updated, System Generator adjusts downstream blocks accordingly.

5.1.1 System Generation DESIGN FLOW

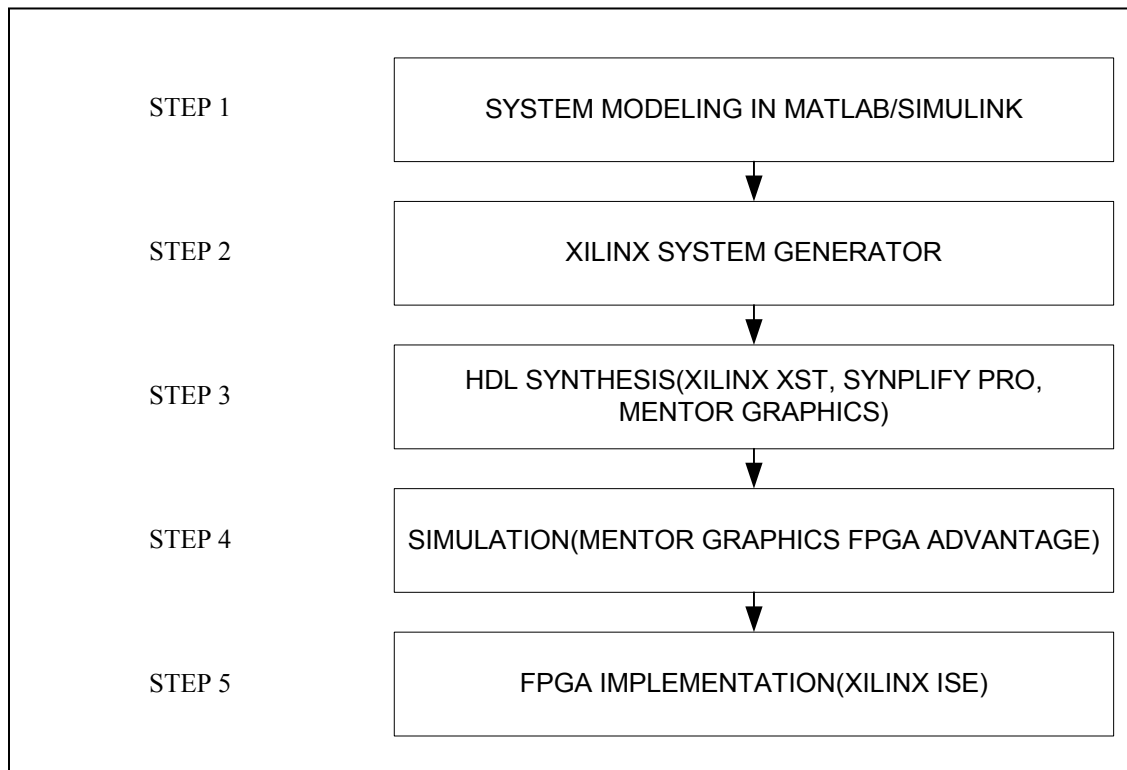


Fig 5.1: XILINX System Generation Design Flow

Figure 5.1 illustrates the various processes involved in transforming a high level design created in SIMULINK to a low level FGPA implementation. A brief description of all the steps follows:

STEP1: A high level system design of the model is developed and tested in MATLAB/SIMULINK using the XILINX block set provided in SIMULINK.

STEP2: System Generation is invoked in SIMULINK using the “XILINX System Generation” icon in the SIMULINK model. This process generates VHDL code for all the XILINX blocks in the SIMULINK design. FPGA designs are generated using XILINX’s LogiCOREs to produce the most efficient implementation.

STEP3: The VHDL design is synthesized to FPGA using one of the three most popular synthesis tools namely XILINX’s XST, SYNPLICITY’s SYNPLIFY PRO and MENTOR GRAPHICS’s FPGA Advantage.

STEP4: This step is optional and can be used to simulate the VHDL design using MENTOR GRAPHICS’s FPGA Advantage. A test bench and data vectors can be created using the System Generator. The data vectors represent the input and the expected outputs as simulated in the SIMULINK design.

STEP5: The synthesized design is loaded into a XILINX FPGA using place and route tools of XILINX’s ISE.

5.2 XILINX Model: Top level system

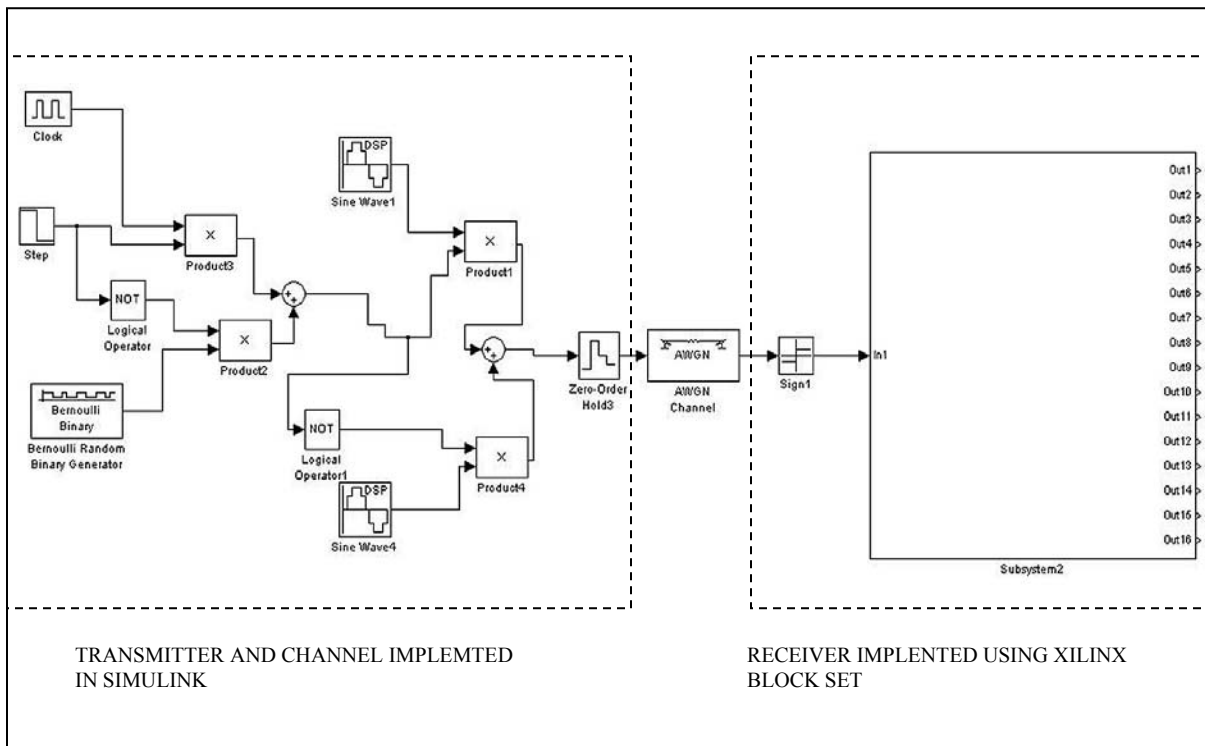


Fig 5.2: XILINX Model top level system diagram

The XLINX model looks pretty much alike the SIMULINK model as we can see from fig 5.2. The transmitter and channel blocks are modeled using the SIMULINK block set while the receiver is modeled using the XILINX block set and included in “Subsystem2”. A provision is made to generate the pilot sequence for an initial period of 0.01 sec in the transmitter block. As mentioned before, the pilot sequence consists of a series of alternating 0s and 1s and is used to facilitate the control system of the receiver to detect the transmitted data rate and to configure one of the FFT bins as the “decision bin”. The pilot signal needs to be transmitted every time the data rate changes, as this is the only way the receiver can detect a change in the transmitted data rate.

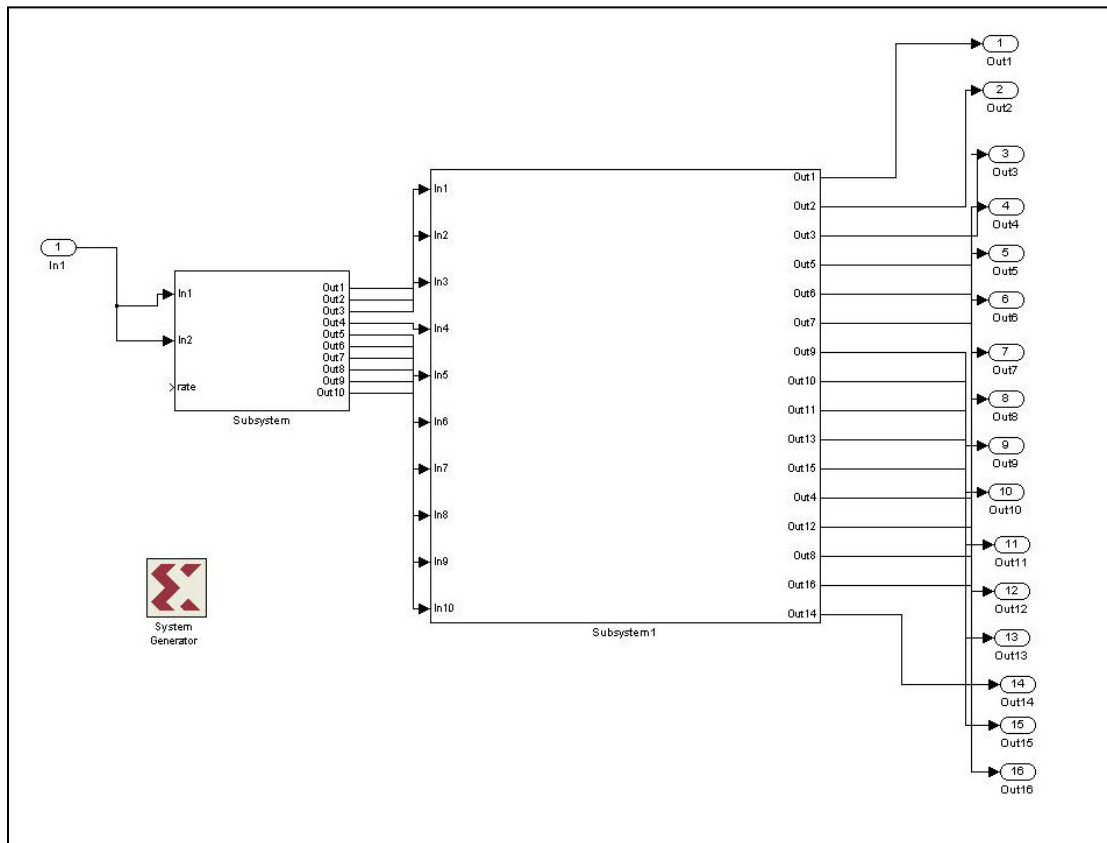


Fig 5.3: Receiver Model implemented in XILINX

The subsystem2 seen in Fig 5.2 is composed to two subsystems demarcated mainly due to their functionalities. The first subsystem takes care of down conversion of the digitized signal and decimation. The second subsystem takes care of FFT detection. As we can see from Fig 5.3, the red block named “System Generator” is used to translate the XILINX design to XILINX hardware targeted to a particular FPGA. The System Generator block has various parameters that can be set to generate XILINX hardware for a specific device and speed. Some of these parameters are:

- a) Product Family. E.g. SPARTAN, VIRTEX, VIRTEX2 etc
- b) Package. E.g. fg676, bg575 etc
- c) Synthesis tool. E.g. XST, SYNPLIFY etc
- d) FPGA System clock period

5.3 XILINX MODEL: Down conversion

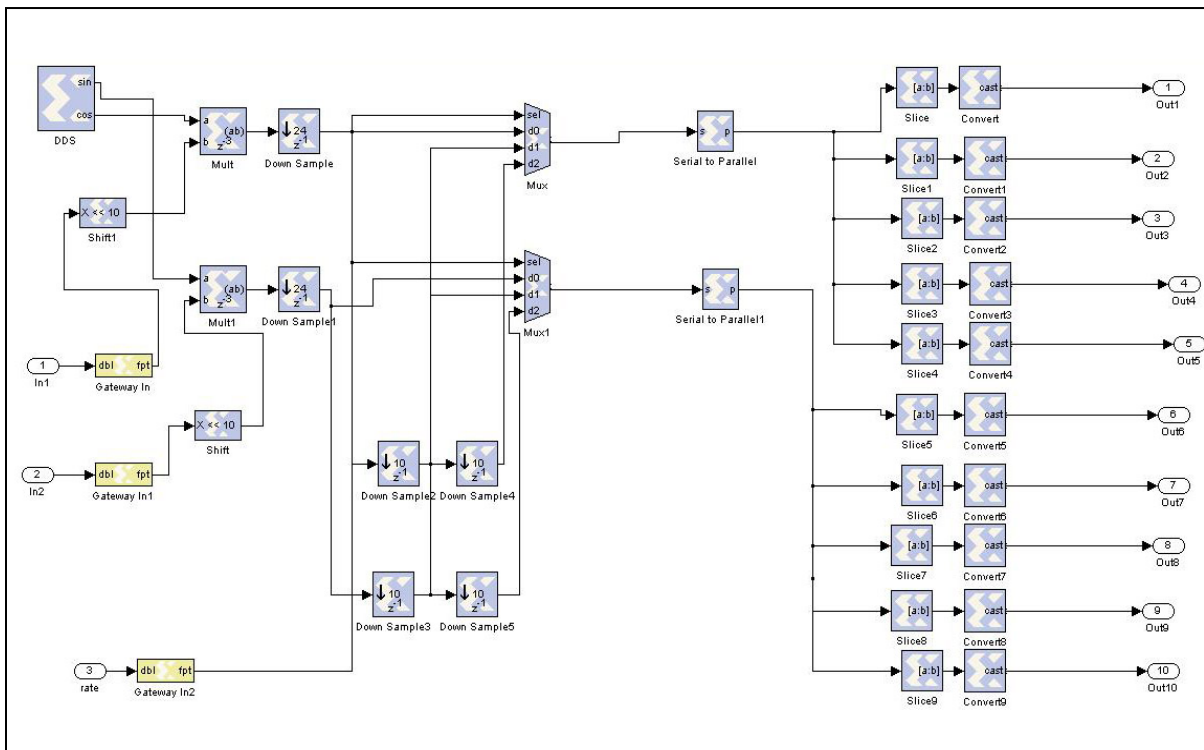


Fig 5.4: XILINX hardware model of the Down conversion operation

Figure 5.4 depicts the hardware design of the down conversion sub system of the receiver. All the blocks used in the design are provided in the XILINX block set and can be readily synthesized to XILINX hardware. The input signal to the block is the 1 bit digitized signal from the A/D converter. The input signal has to pass through the “Gateway In” block that converts values of type “double” to the “XILINX fixed point” type. The number of bits for each data value is 20 and the data type is signed (2s complement). The binary point of the data is located at 0. As we can see, there exist two identical data paths in the design. The first one represents the real path and the second one represents the imaginary part. A direct digital synthesizer (DDS) is used to generate the required sine and cosine waveforms for down conversion. Then, the signal is down sampled by 24, 10 and 10 and all the outputs are fed into a 3:1 MUX. The select line of this MUX is controlled by the control system as mentioned before. The output of the MUX is passed to a serial to parallel converter which takes 5 serial 20 bit data values and converts it into one data value of bit length 100 which is basically a concatenation of all the data values. This is done in order to stack five signal samples per symbol for FFT detection. The parallel bit is sliced back into 20 bits each using the “slice” blocks. Finally the output of the “slice” block is type converted to signed (2s complement) data type and fed into the FFT detector.

5.4 XILINX Model: FFT Detector

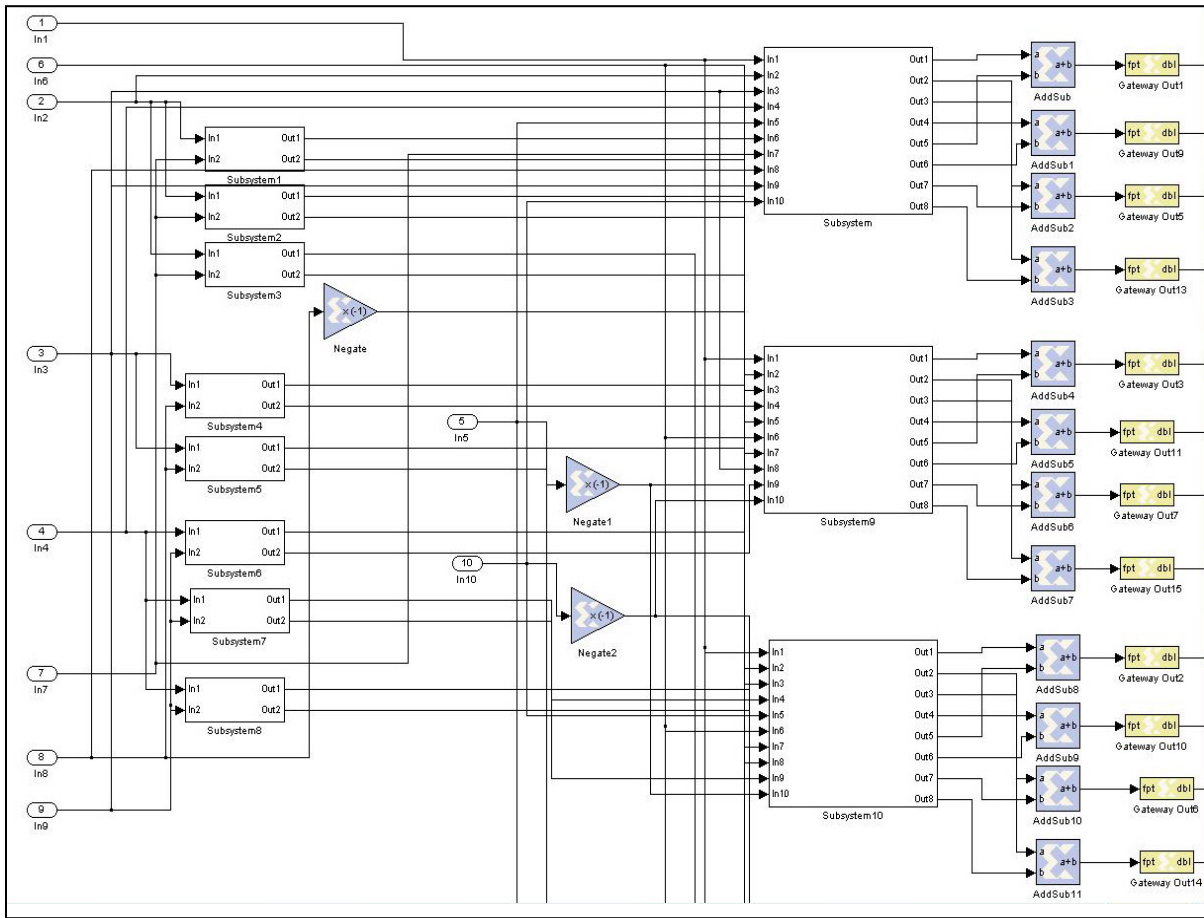


Fig 5.5: XILINX Hardware Model of the FFT Detector

As mentioned before, the FFT detector is modeled based on the algorithm proposed by Bertazzoni [2]. Figure 5.5 depicts the XILINX hardware model of the FFT detector which consists of various interconnected subsystems. Each subsystem has two kinds of inputs; real and imaginary. The purpose of these subsystems is to add and shift the complex data according to the FFT algorithm and thus implementing the CORDIC algorithm.

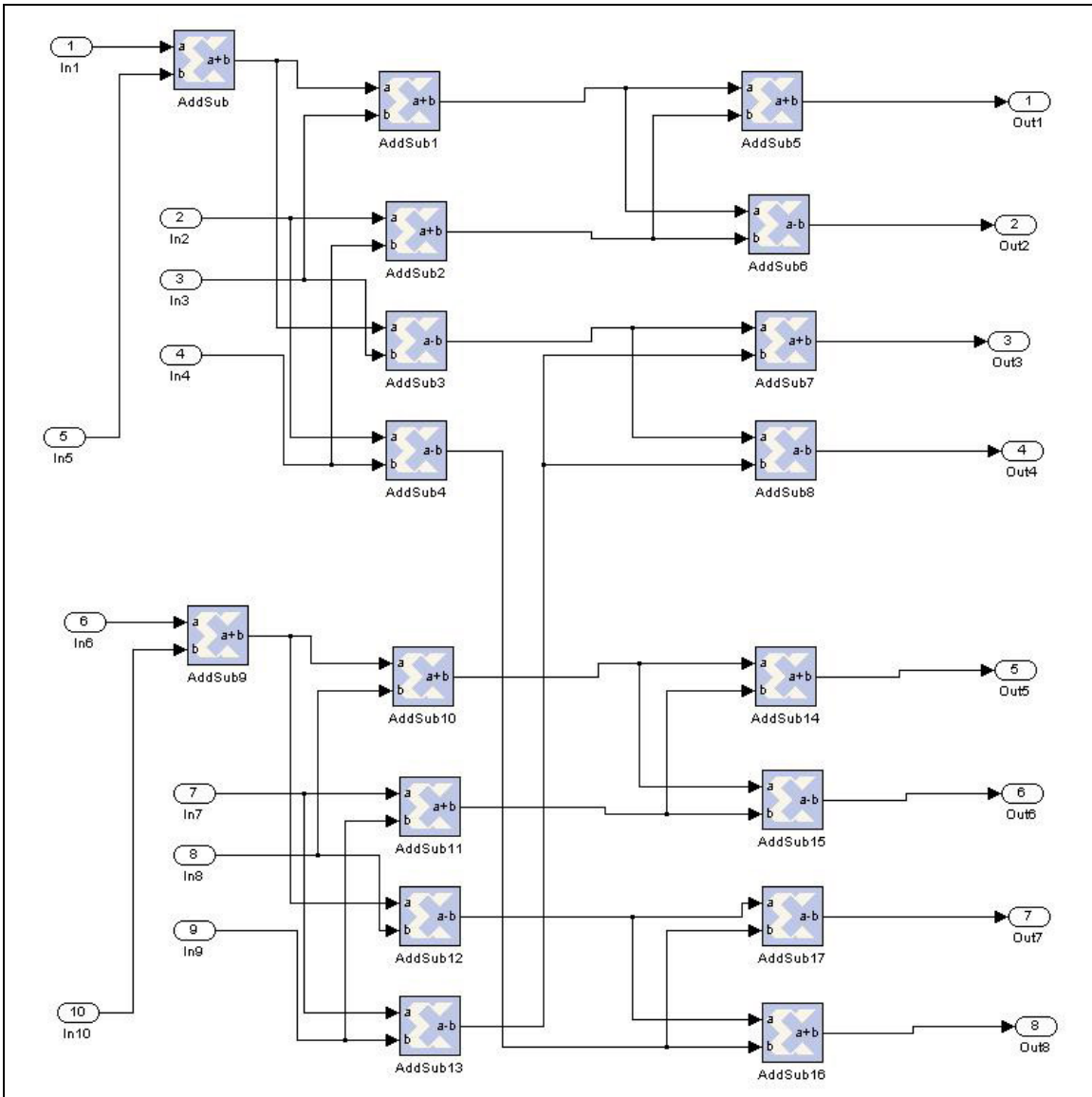


Fig 5.6: Subsystem to implement the sum of real and imaginary parts for FFT computation

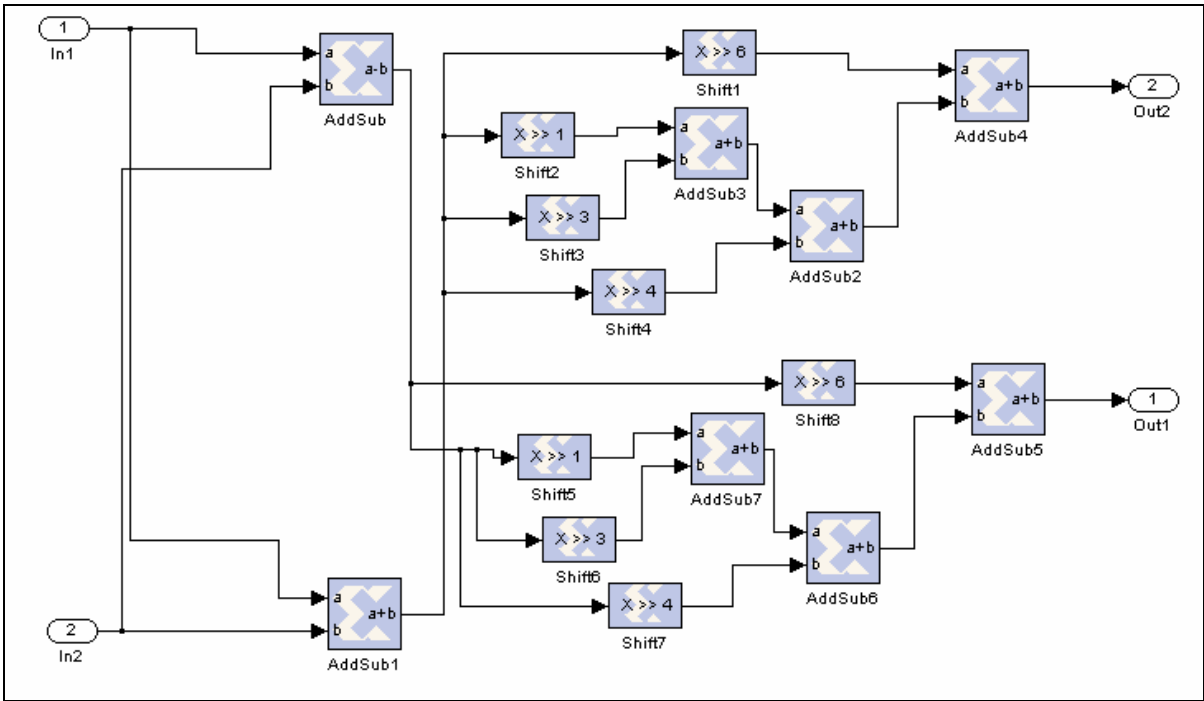


Fig 5.7: Subsystem to implement a rotation of 45° for FFT computation

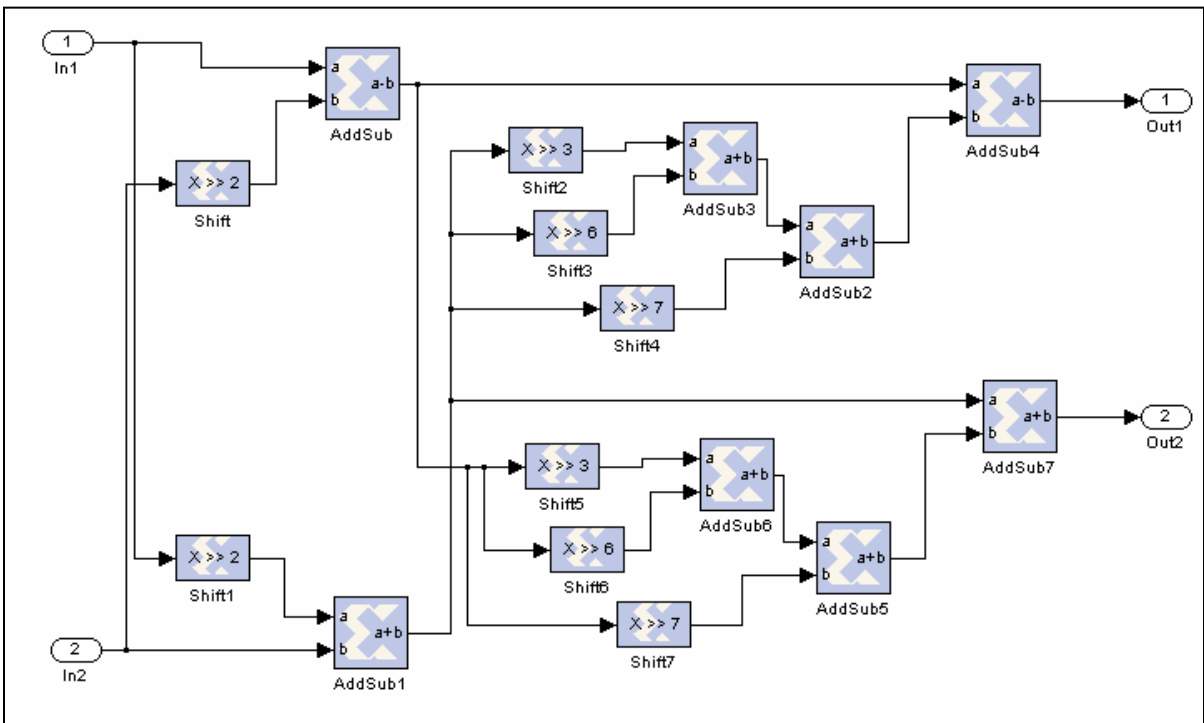


Fig 5.8: Subsystem to implement a rotation of 22.5° for FFT computation

Figures 5.6, 5.7 and 5.8 represent the internal hardware block diagram of the subsystems used in the FFT detector based on the CORDIC algorithm. Figure 5.6 shows the hardware block used for summing the real and imaginary parts of complex input data. The hardware depicted in figures 5.7 and 5.8 are used to rotate a complex vector by angles 45° and 22.5° respectively as proposed in [2].

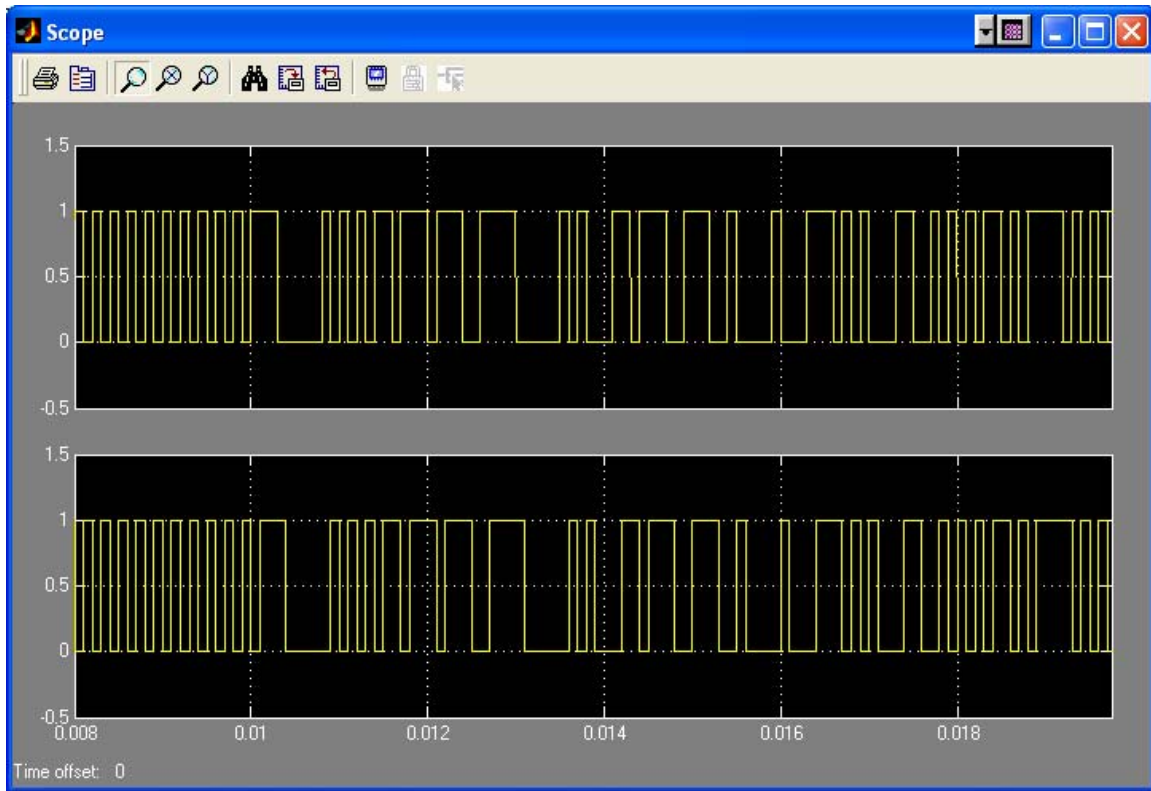


Fig 5.9: Waveforms displayed after symbol detection

The output of the FFT detector is fed to the control system that takes care of symbol decision based on the threshold value. The XILINX model was tested in SIMULINK for a data rate of 10kbps in presence of the AWGN channel. Figure 5.9 displays the results of the detected waveform. The top waveform is the transmitted data from the Bernoulli random generator. The bottom wave is the detected wave by the receiver. The transmitted and the received waves match with each other indicating successful operation of the XILINX hardware model of the receiver. Note a delay of one clock cycle in the received waveform.

5.5 Synthesis to XILINX FPGA

We synthesized the XILINX hardware model to a XILINX FPGA using the system generator tool. The product family used was Virtex2, device used was xc2v1500 (anticipating around 1000 million gates) and the XILINX system clock period was set to 100ns. The model was synthesized successfully and following is timing report as indicated in the synthesis report of XILINX:

Timing Summary:

Speed Grade: -6

Minimum period: 6.841ns (Maximum Frequency: 146.178MHz)

Minimum input arrival time before clock (Critical Path Delay): 4.282ns

Following is the MAP report obtained from XILINX for the receiver model indicating the total gate count and number of slices used in the FPGA.

Design Summary

Number of Slices: 2,633 out of 7,680 34%

Total equivalent gate count for design: 85,456

We ran XPOWER utility of XILINX and found that the total power usage of the receiver is 280mW.

CHAPTER 6

CONCLUSION AND FUTURE WORK

We have successfully designed and simulated a low power BFSK receiver intended for future deep space missions. The receiver is implemented with a 16 point FFT detector for Doppler invariance and tests show that frequency shifts of up to 10 KHz are tolerated by the receiver. We have tested the receiver for data rates of 10kbps, 1kbps and 100bps. The worst case BER performance of the receiver is about 2.5db less than the optimal non coherent FSK receiver at a BER of $10E-3$ and data rate of 10kbps. We have successfully understood the design flow of XILINX system generation. The SIMULINK model of the receiver is used to develop a XILINX model of the receiver and synthesized to VIRTEX-2 FPGA using system generation and XILINX ISE tools. Power estimation of the receiver as per the XPOWER utility of XILINX is 280mW.

6.1 Future Work

The power consumption of the receiver can be further reduced by making a few design modifications. The FFT Detector can be implemented using a radix-4 FFT algorithm instead of the existing radix-2 algorithm for better power and space efficiency. The hardware multiplier and the digital frequency synthesizer at the down conversion stage could be substituted by simpler circuits. A frequency tracking circuit can be implemented in the control system to track the change in decision bins due to Doppler shifts.

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APPENDIX

1. MATLAB script for FFT computation and symbol decision

```
% Strip 5 data values from the received signal
compute = 1
if compute == 1
n_symbols = 1000
count = 1
for n = 1:n_symbols
    for j = 1:5
        val(j,n) = complex(yout1(count+j,2),yout1(count+j,1))
    end
    count = count + 5
end

%Pad the remaining 11 values with zeros
for n = 1:n_symbols
    for j = 6:16
        val(j,n) = 0
    end
end

% Compute the FFT
res = fft(val,16);
res1 = abs(res);

end

% Symbol decision
threshold = 2
decision_bin = 7
for n = 1:n_symbols
    if res1(decision_bin,n) > threshold
        wave(n) = 1
    else
        wave(n) = 0
    end
end
end
```

```
%Compute error for BER analysis
error = 0
for n = 1:n_symbols
    if wave(n) ~= yout4(n)
        error = error + 1
    end
end
end
```

2. VHDL code implementing the control system for bin resolution and rate detection

```
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;

-- Definition of entity called control
Entity control is
port(bin1,bin2,bin3,bin4,bin5,bin6,bin7,bin8,bin9,bin10,bin11,bin12,bin13,bin14,bin15,
Bin 16 : in std_logic_vector(19 downto 0); clk_10k, clk_1k, clk_100, rst : in std_logic; rate :
out std_logic_vector(0 to 1); sig_out : out std_logic);
end control;

-- Architecture definition of the entity control
architecture structure of control is
    type states is (binresolution, demodulation);
    signal currentstate, nextstate : states;
    signal bin_val1, bin_val2, bin_out : std_logic_vector(19 downto 0);
    signal count, count_clk : unsigned(0 to 1) := "00";
    signal temp_bin : unsigned(0 to 3) := "0000";
    signal clk : std_logic := clk_10k;
        signal demod, enable, en_temp_bin, check : std_logic;
begin

    -- Select one of the three clocks
    SELECTCLK : process(clk_10k, clk_1k, clk_100)
    begin
        case count_clk is
            when "00" =>
                rate <= "00";
                clk <= clk_10k;
            when "01" =>
                rate <= "01";
                clk <= clk_1k;
            when "10" =>
                rate <= "10";
                clk <= clk_100;
            when others =>
                rate <= "00";
                clk <= clk_10k;
        end case;
    end process;
end structure;
```

```

-- State register
STREG : process(clk, rst)
begin
    if rst = '1' then
        currentstate <= binresolution;
    elsif rising_edge(clk) then
        currentstate <= nextstate;
    end if;
end process;

-- Select one of the 16 bins
BINMUX : process(temp_bin, bin1, bin2, bin3, bin4, bin5, bin6, bin7, bin8, bin9, bin10,
bin11, bin12, bin13, bin14, bin15, bin16)
begin
    case temp_bin is
        when "0000" =>
            bin_out <= bin1;
        when "0001" =>
            bin_out <= bin2;
        when "0010" =>
            bin_out <= bin3;
        when "0011" =>
            bin_out <= bin4;
        when "0100" =>
            bin_out <= bin5;
        when "0101" =>
            bin_out <= bin6;
        when "0110" =>
            bin_out <= bin7;
        when "0111" =>
            bin_out <= bin8;
        when "1000" =>
            bin_out <= bin9;
        when "1001" =>
            bin_out <= bin10;
        when "1010" =>
            bin_out <= bin11;
        when "1011" =>
            bin_out <= bin12;
        when "1100" =>
            bin_out <= bin13;
        when "1101" =>
            bin_out <= bin14;
    end case;
end process;

```

```

when "1110" =>
  bin_out <= bin15;
when "1111" =>
  bin_out <= bin16;
when others =>
  bin_out <= bin_out;
end case;
end process;

-- Bin decision
STTRANS : process(currentstate, check)
begin
  case currentstate is
  when binresolution =>
    demod <= '0';
    enable <= '1';
    en_temp_bin <= '0';
    if check = '1' then
      if ((signed(bin_val1) > 7 and signed(bin_val2) < -7 ) or (signed(bin_val2) > 7 and
signed(bin_val1) < -7 )) then
        nextstate <= demodulation;
        enable <= '0';
        en_temp_bin <= '0';
      else
        enable <= '1';
        en_temp_bin <= '1';
      end if;
    end if;
  end if;

  when demodulation =>
    demod <= '1';
  end case;
end process;

-- count register
MYCOUNTER : process(clk, enable, rst)
begin
  if rst = '1' then
    count <= "00";
  elsif rising_edge(clk) and enable = '1' then
    count <= count + 1;
  else
    count <= count;
  end if;
end process;

```

-- Registers for storing two successive samples of a particular bin
BINVAL : process(clk, enable, rst)

```
begin
  if rst = '1' then
    bin_val1 <= "00000000000000000000";
    bin_val2 <= "00000000000000000000";
  elsif rising_edge(clk) and enable = '1' then
    bin_val1 <= bin_out;
    bin_val2 <= bin_val1;
  else
    bin_val1 <= bin_val1;
    bin_val2 <= bin_val2;
  end if;
end process;
```

-- The *check* signal
CHECKSIG : process(clk, rst, enable, count)

```
begin
  if rst = '1' then
    check <= '0';
  elsif rising_edge(clk) and count = "11" then
    check <= '1';
  else
    check <= check;
  end if;
end process;
```

-- The *temp_bin* register for the select line of 16:1 Mux
TEMPBIN : process(clk, en_temp_bin, rst)

```
begin
  if rst = '1' then
    temp_bin <= "0000";
    count_clk <= "00";
  elsif rising_edge(clk) and en_temp_bin = '1' then
    if temp_bin = "1111" then
      count_clk <= count_clk + 1;
    end if;
    temp_bin <= temp_bin + 1;
  end if;
end process;
```



```
-- The demodulation proces
STDEMOD : process(clk, demod)
begin
  if rising_edge(clk) and demod = '1' then
    if signed(bin_out) > 7 then
      sig_out <= '1';
    else
      sig_out <= '0';
    end if;
  end if;
end process;

end structure;
```